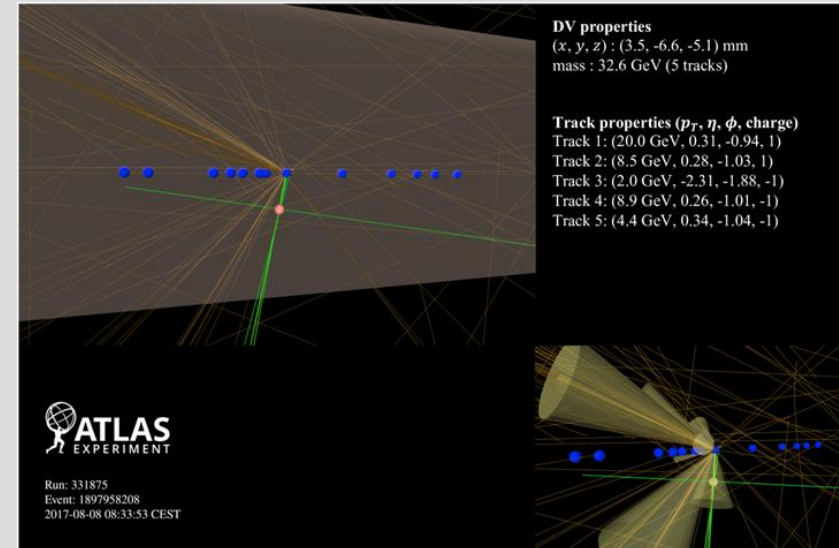
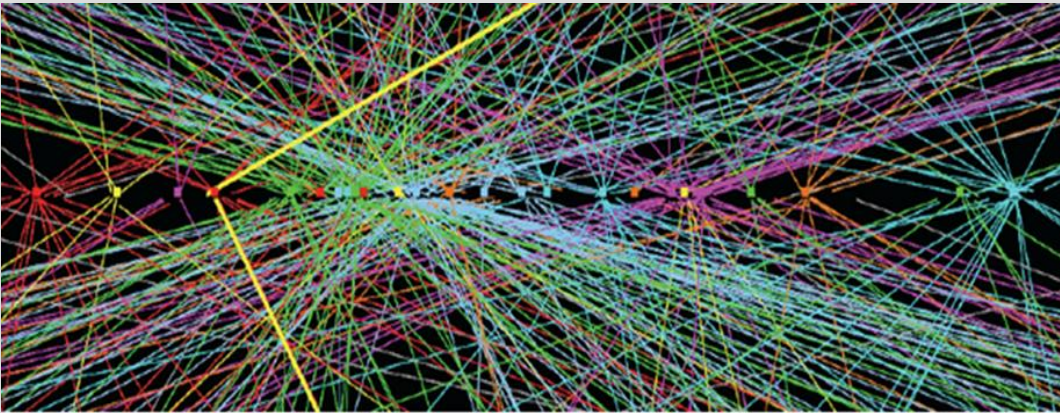


TrackOpt vertex project update

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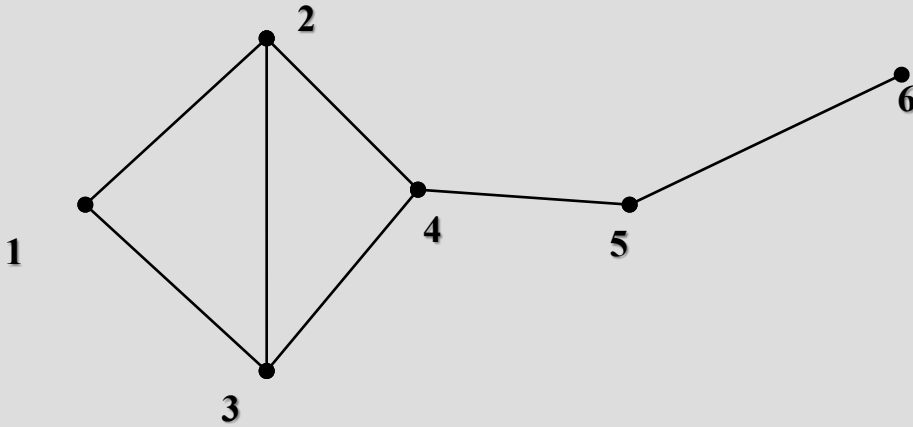


Problem:

Having a set of tracks find all vertices (track production points)

Solution idea:

1. Create a track-track compatibility graph using a priori physics knowledge, i.e. explicitly calculate a point of closest approach of the 2 tracks in 3D space and the track/vertex parameters at this point.
2. Based on this information, estimate a probability that a given 2-track vertex is real
3. Use LMC algorithm to partition this graph with weighted edges



Example:

6 tracks (nodes)

7 possible 2-track vertices (edges)

Node vector of features(track parameters): `td0, tZ, tPhi, tEta, tQoP, tTheta, tChi2, tNDoF, tCovD0, tCovZ, tCovD0Z, tSignif`

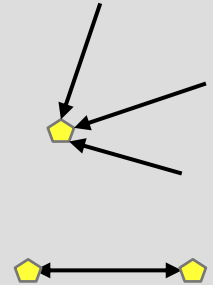
Edge vector of features(2-track vertex): `vChi2, vX, vY, vZ, vcovXX, vcovXY, vcovYY, vcovXZ, vcovYZ, vcovZZ, vsumPt, vEta, vPhi, vDZ, massPiPi, vtrue, vCharge, isGamma, isKs, isLambda + truth_label`

Prepared graphs saved in ROOT format (~1.5mb/ev, ~1400nodes/ev, ~26k edges/ev)

For the moment, to save CPU, for tracks closer that 3σ to the beamline no real vertex fit is done.
Compatibility is calculated based on Z track position on the beamline (1D fit, like in the PV finding paper).

Edge weights estimation is implemented in DGL

- 1) $\text{Node_hidden_state} = \text{NN}\{\text{Concat}(\text{Node_features}, \text{Mean}(\text{Edge_features}))\}$
- 2) $\text{Edge_weight} = \text{NN}\{\text{Concat}(\text{Node_hidden_state}_i, \text{Edge_features}, \text{Node_hidden_state}_j)\}$
- 3) $\text{Node_hidden_state} = \text{NN}\{\text{Concat}(\text{Node_features}, \text{Weighted_Mean}(\text{Edge_features}))\}$
- 4) $\text{Upd_Edge_weight} = \text{NN}\{\text{Concat}(\text{Node_hidden_state}_i, \text{Edge_features}, \text{Node_hidden_state}_j)\}$

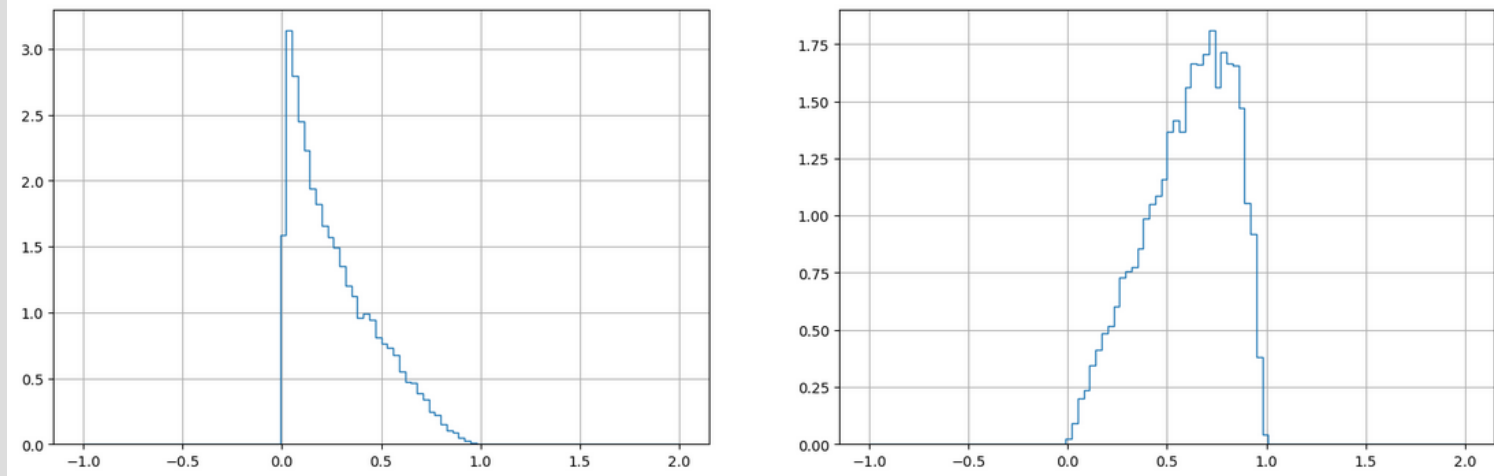


Steps (3),(4) happened to be not needed, final weights are practically the same.

Loss – binary cross-entropy (classification)

Activations – Mish + Sigmoid to get probability

DGL results (very preliminary)



AUC ~ 0.84 for both primary and secondary edges(aka. 2-track vertices)

For comparison - XGBoost classification of edges based on the same edge features: AUC ~ 0.75

Next steps

- 1) Save training results and run LMC on weighted graphs
- 2) Implement metrics for comparison
- 3) Play with DGL
 - ✓ More graphs for training (currently batch of 50)
 - ✓ Different layers – LSTM, Transformers, etc,
 - ✓ Different reduction functions
 - ✓
- 4) More into the future – try edge prediction approach based on node(track) features only. This will allow to estimate a performance gain due to a priory knowledge injected as edge features
 - Similarity to foundation model