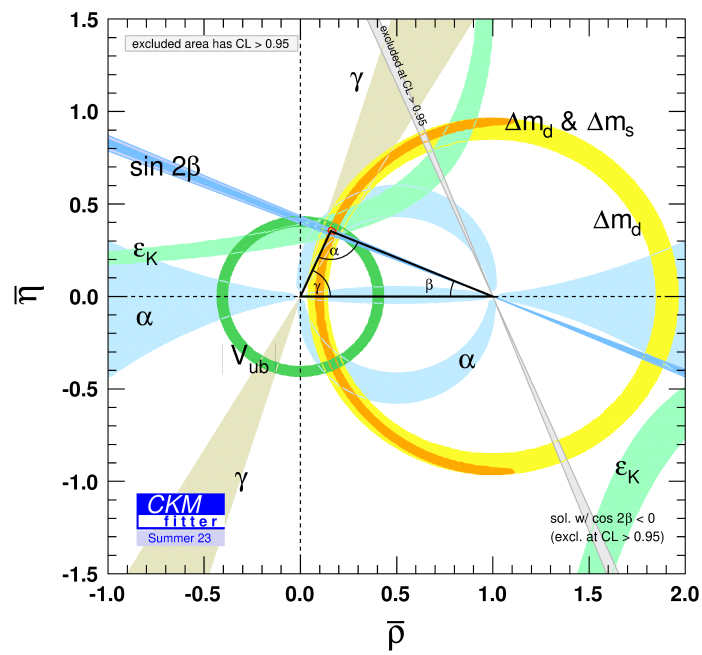
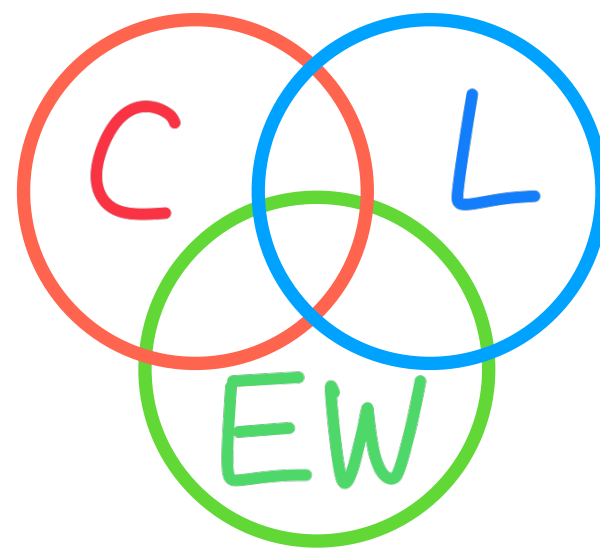


# CKM: Fitting SMEFT with a CLEW



Tom Tong



Co-directed by

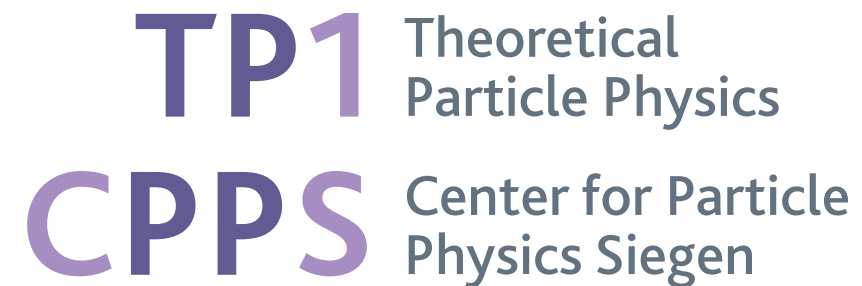
*Vincenzo Cirigliano*

*Wouter Dekens*

*Jordy de Vries*

*Emanuele Mereghetti*

2311.00021 JHEP 03 (2024) 033

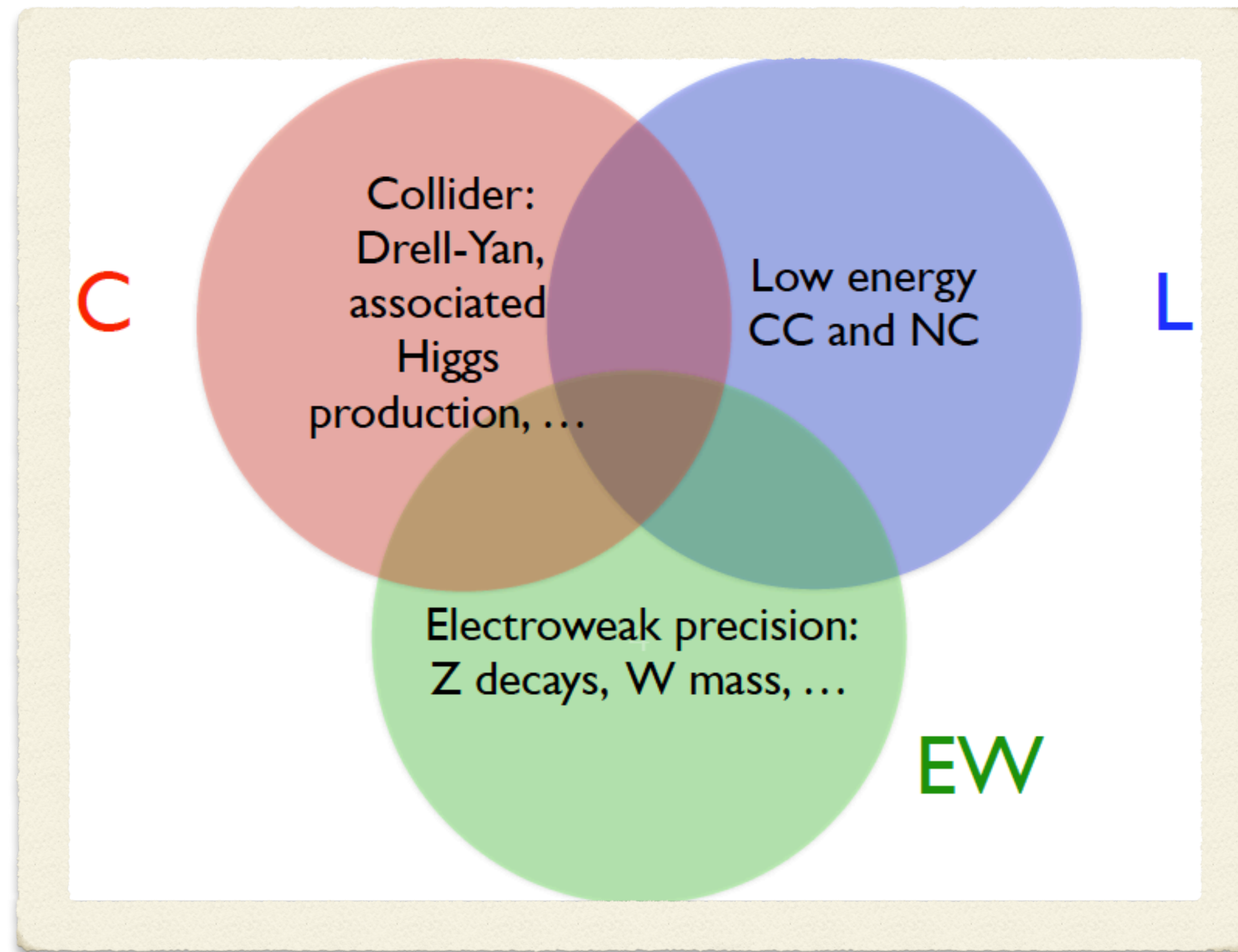




# Abstract for the impatient

SMEFT global-fits: two major challenges

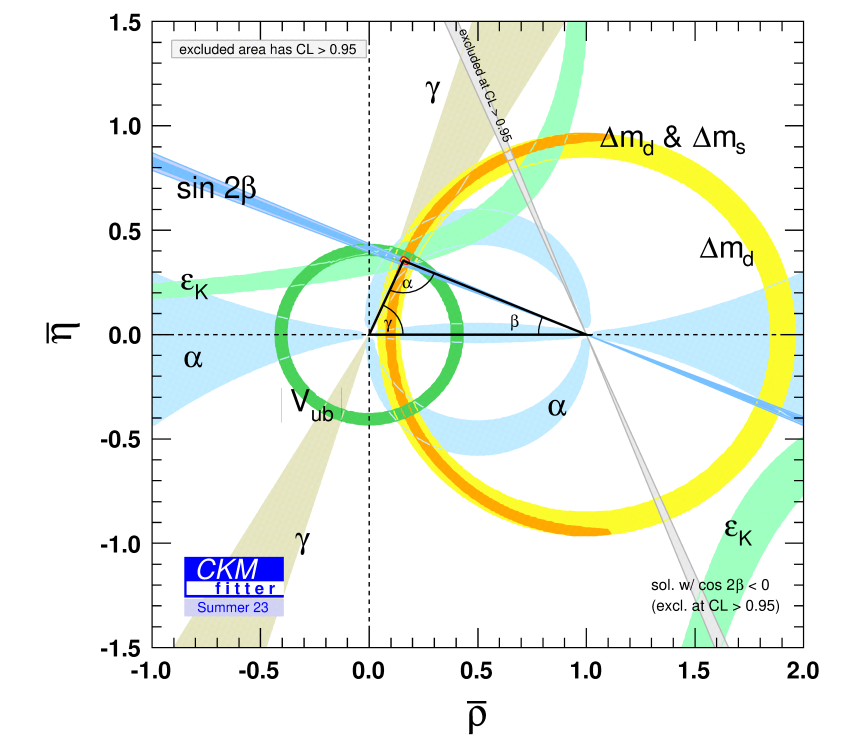
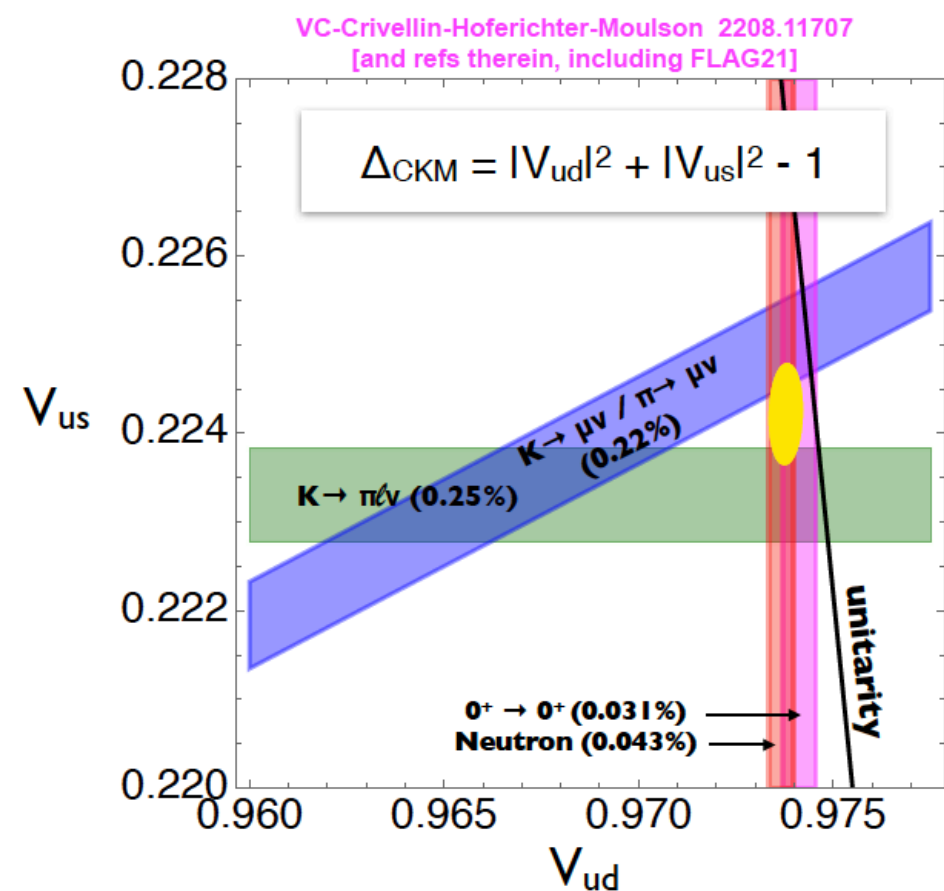
## The CLEW framework



Incomplete observables

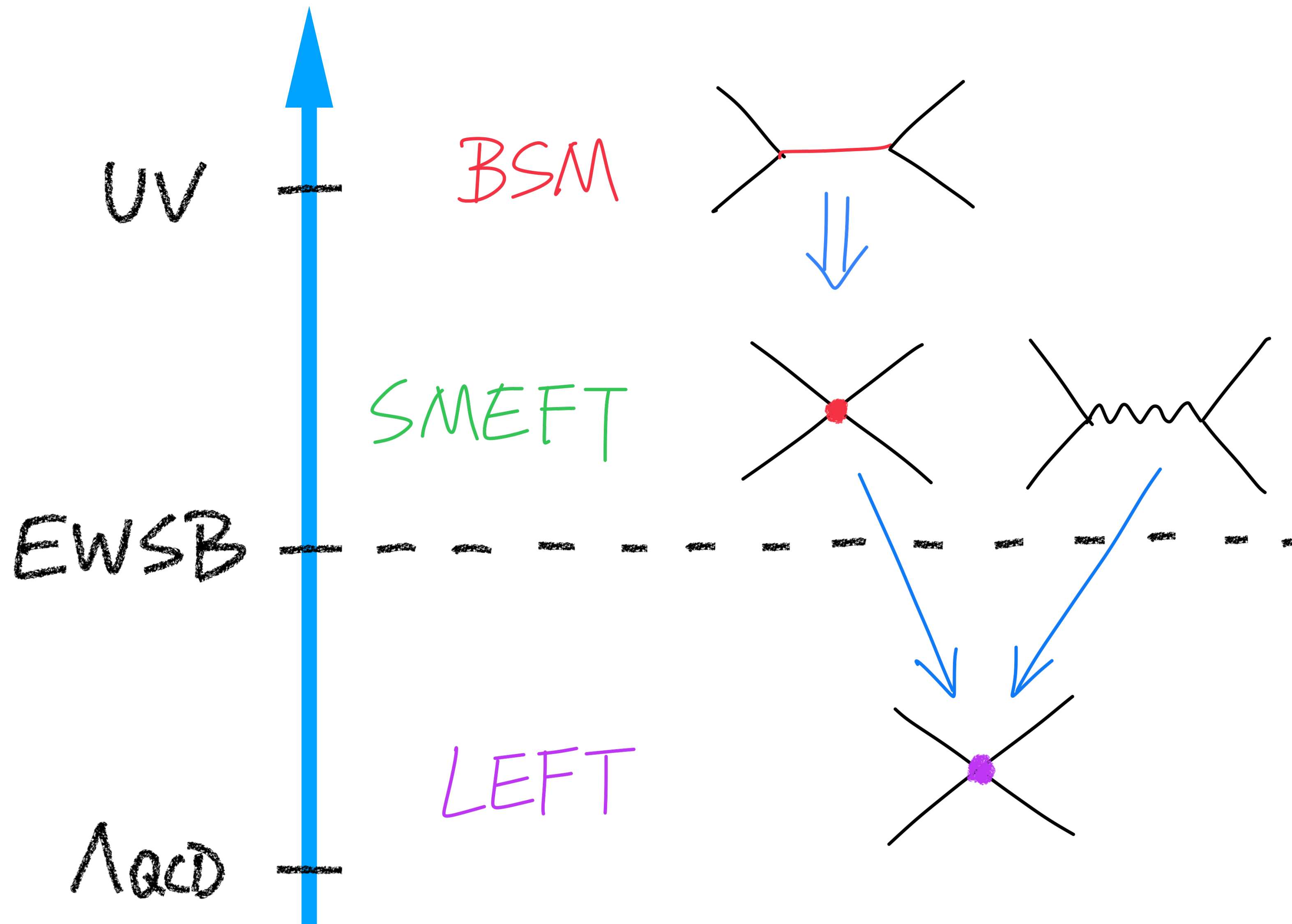


Flavor assumptions



Flavor-assumption-free

# SMEFT in a nutshell

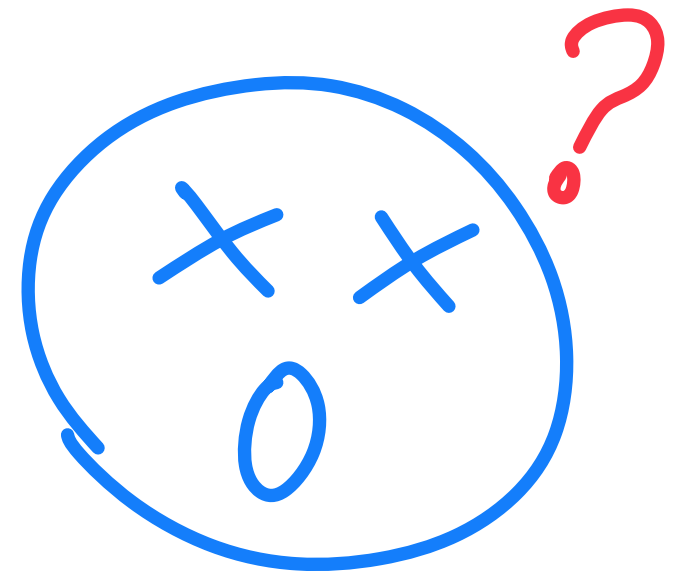




# SMEFT at work

$$\mathcal{L}_{\text{SMEFT}}^{\text{dim-6}} = \mathcal{L}_{\text{SM}} + \sum_i^{2499} c_i \mathcal{O}_i^{\text{dim-6}}$$

Too many operators!



Simplify!



Make flavor-symmetry assumptions

Handpick observables and operators

$U(3)^5$ , MFV,  $U(2)^5$ , top...



EWPO + Higgs + top + some flavor...



# Casefile: $U(3)^5 + \text{EWPO}$



$$U(3)_q \times U(3)_u \times U(3)_d \times U(3)_l \times U(3)_e$$

Fitting *without* a **CLEW**

	EW
$\hat{C}_{Hl}^{(1)}$	$0.0026 \pm 0.011$
$\hat{C}_{Hl}^{(3)}$	$-0.019 \pm 0.016$
$\hat{C}_{He}$	$-0.0011 \pm 0.0092$
$\hat{C}_{Hq}^{(1)}$	$-0.033 \pm 0.043$
$\hat{C}_{Hq}^{(3)}$	$-0.056 \pm 0.033$
$\hat{C}_{Hu}$	$-0.02 \pm 0.12$
$\hat{C}_{Hd}$	$-0.54 \pm 0.25$
$C_\Delta$	$-0.11 \pm 0.069$

$$\Delta_{CKM}^{exp} \approx -0.15\%$$

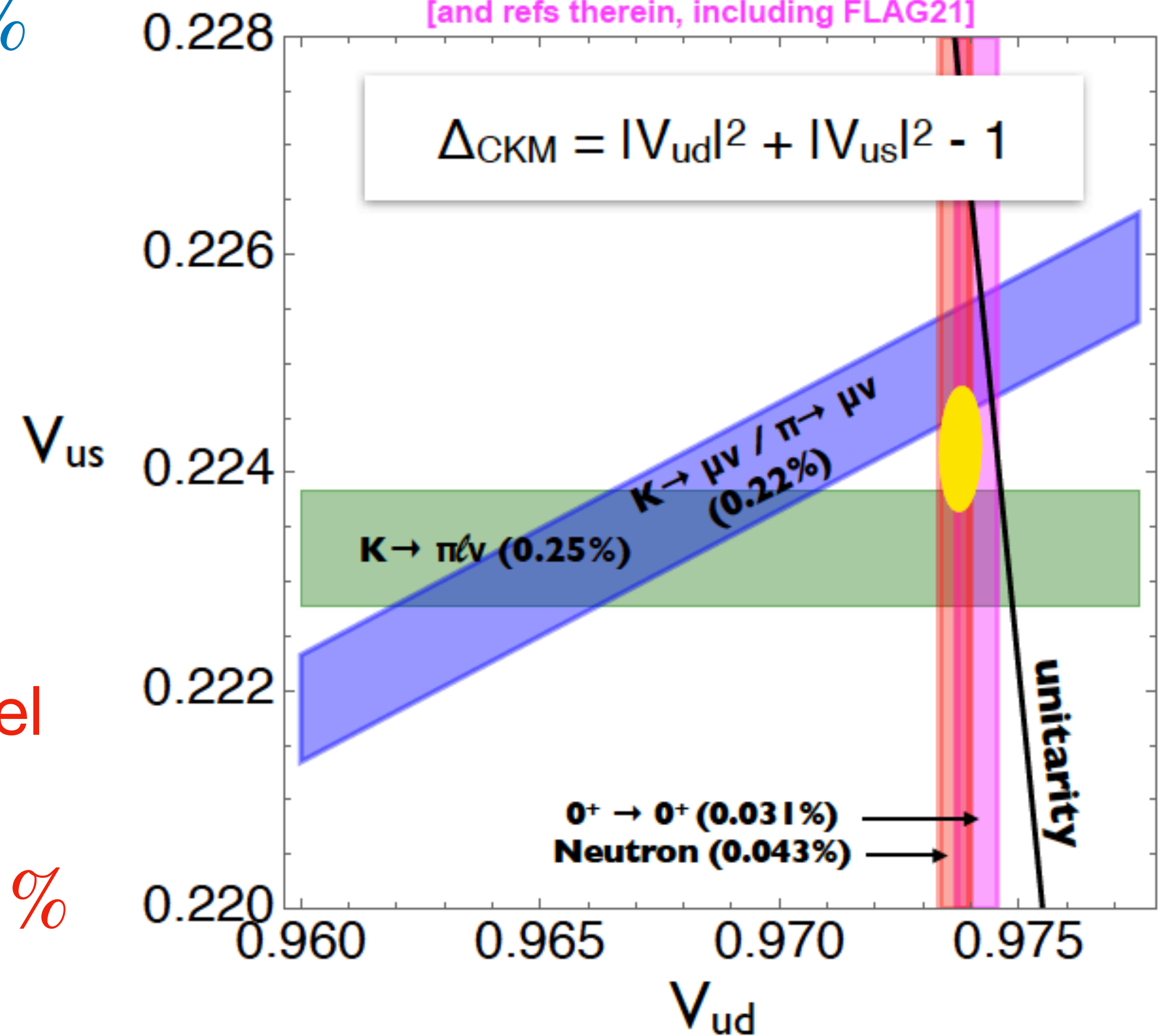
$\sim 3\sigma$  at permil level



$\sim 2\sigma$  at percent level

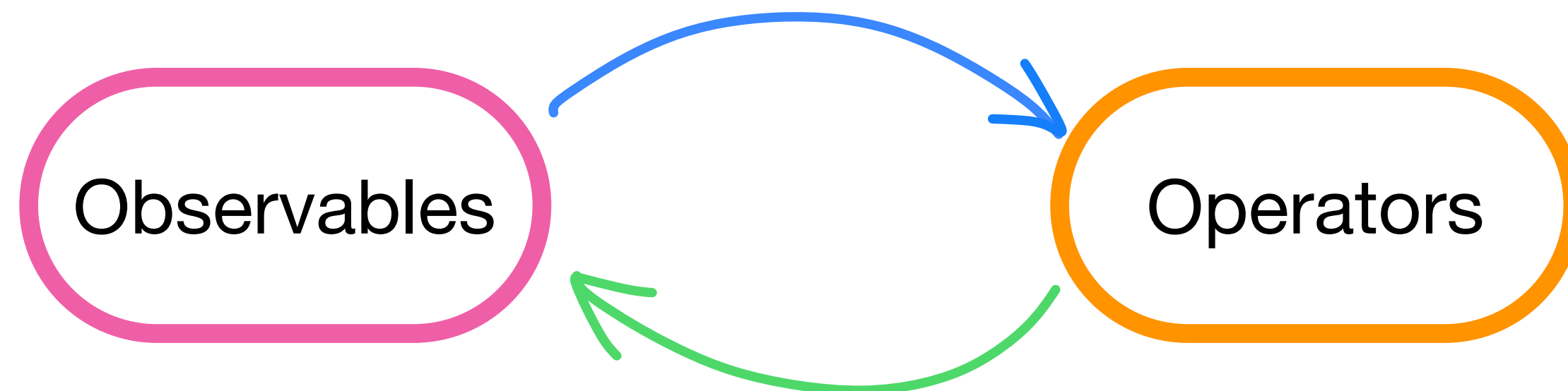
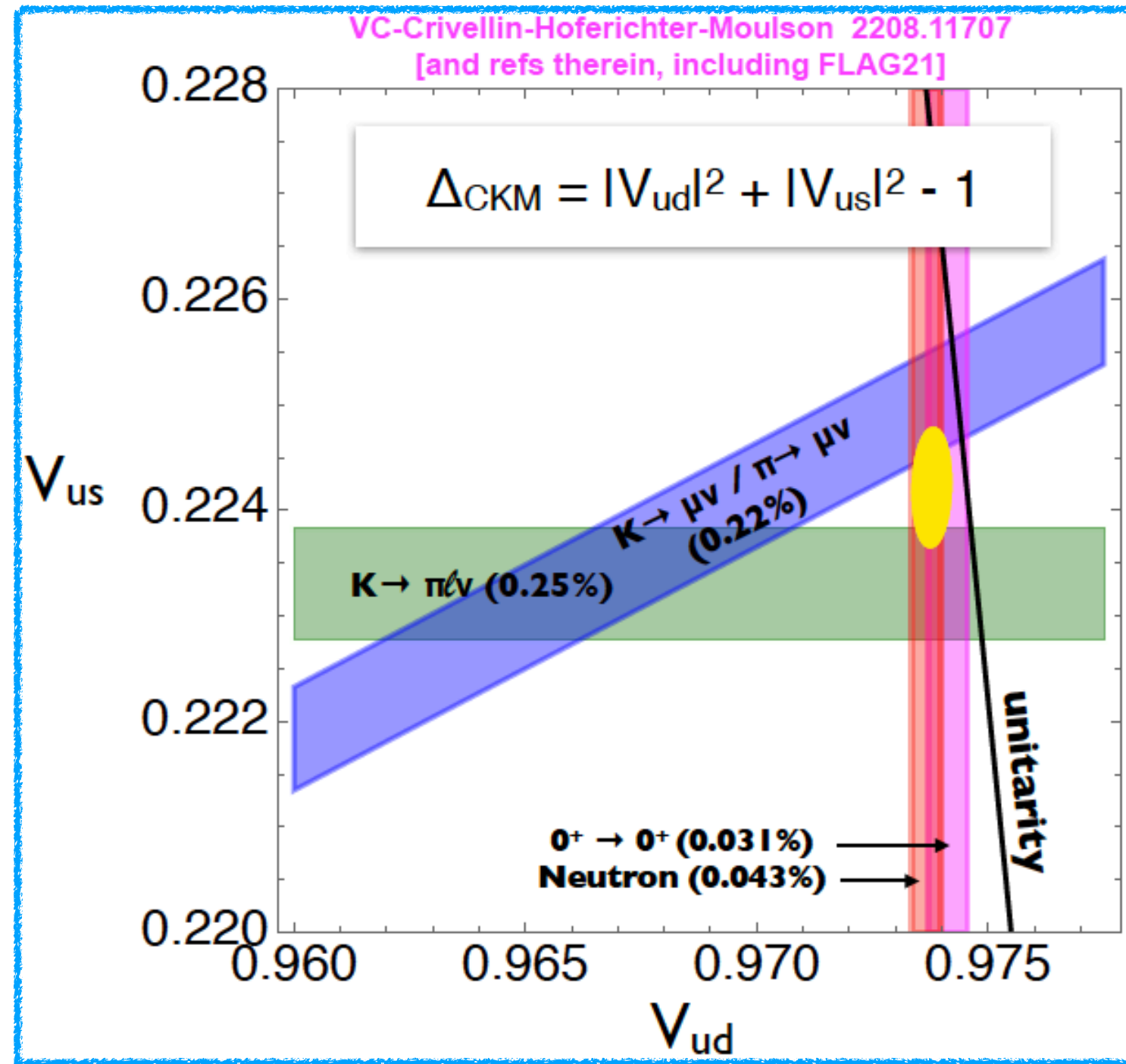
$$2v^2 \left[ C_{Hq}^{(3)} - C_{Hl}^{(3)} + C_{ll} - \cancel{C_{lq}^{(3)}} \right] = \Delta_{CKM}^{fit} \approx -0.67\%$$

VC-Crivellin-Hoferichter-Moulson 2208.11707  
[and refs therein, including FLAG21]



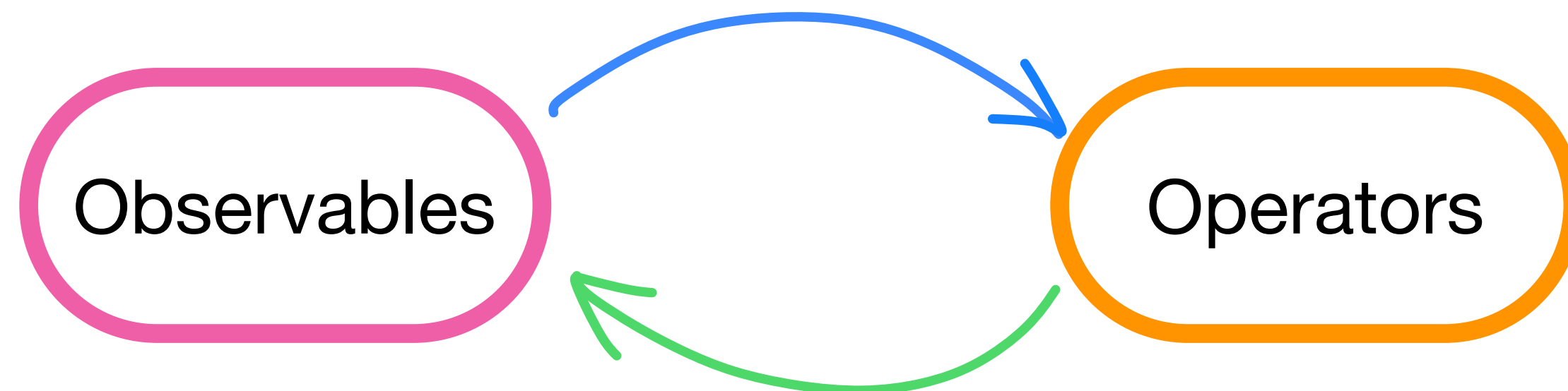
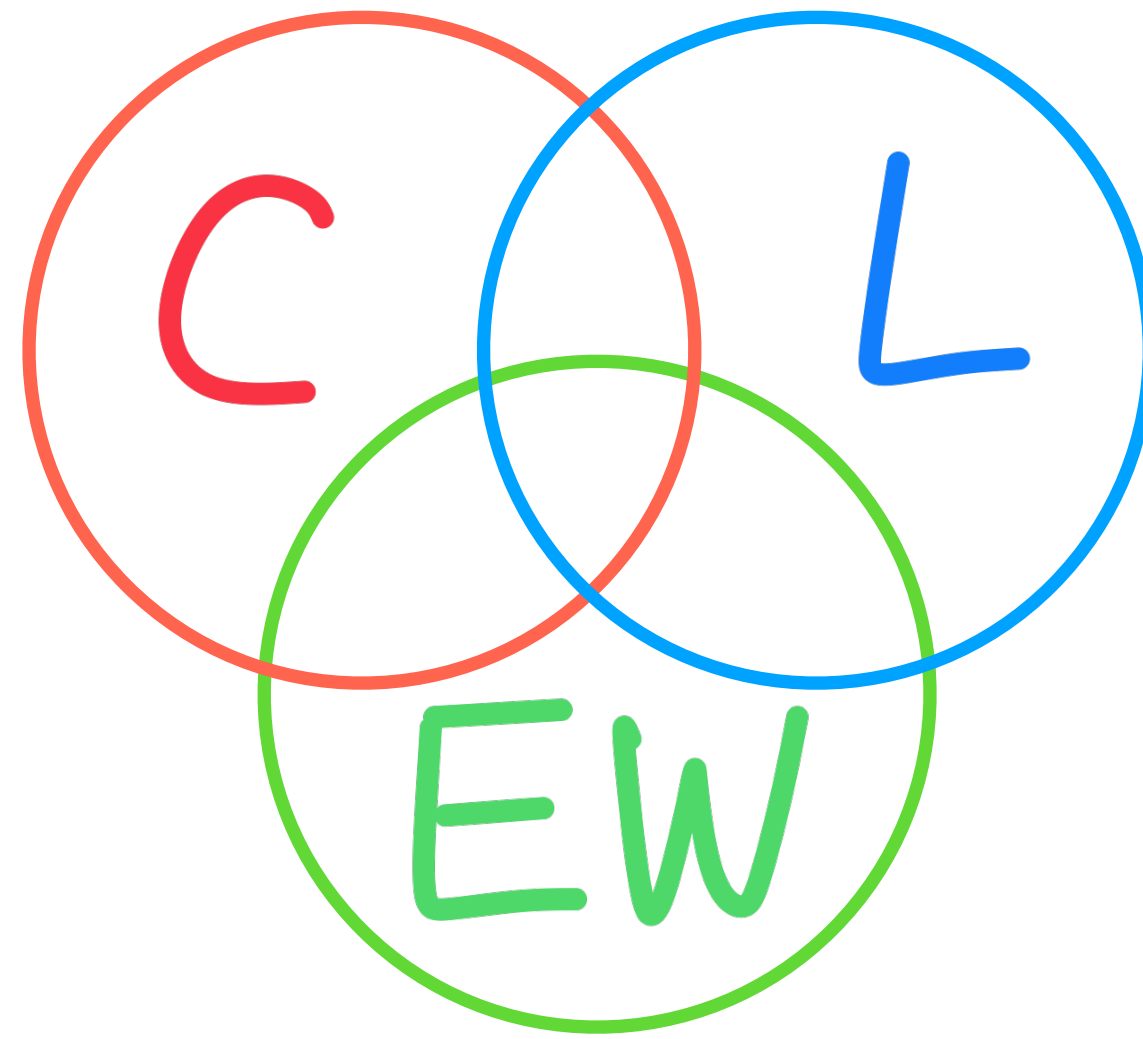
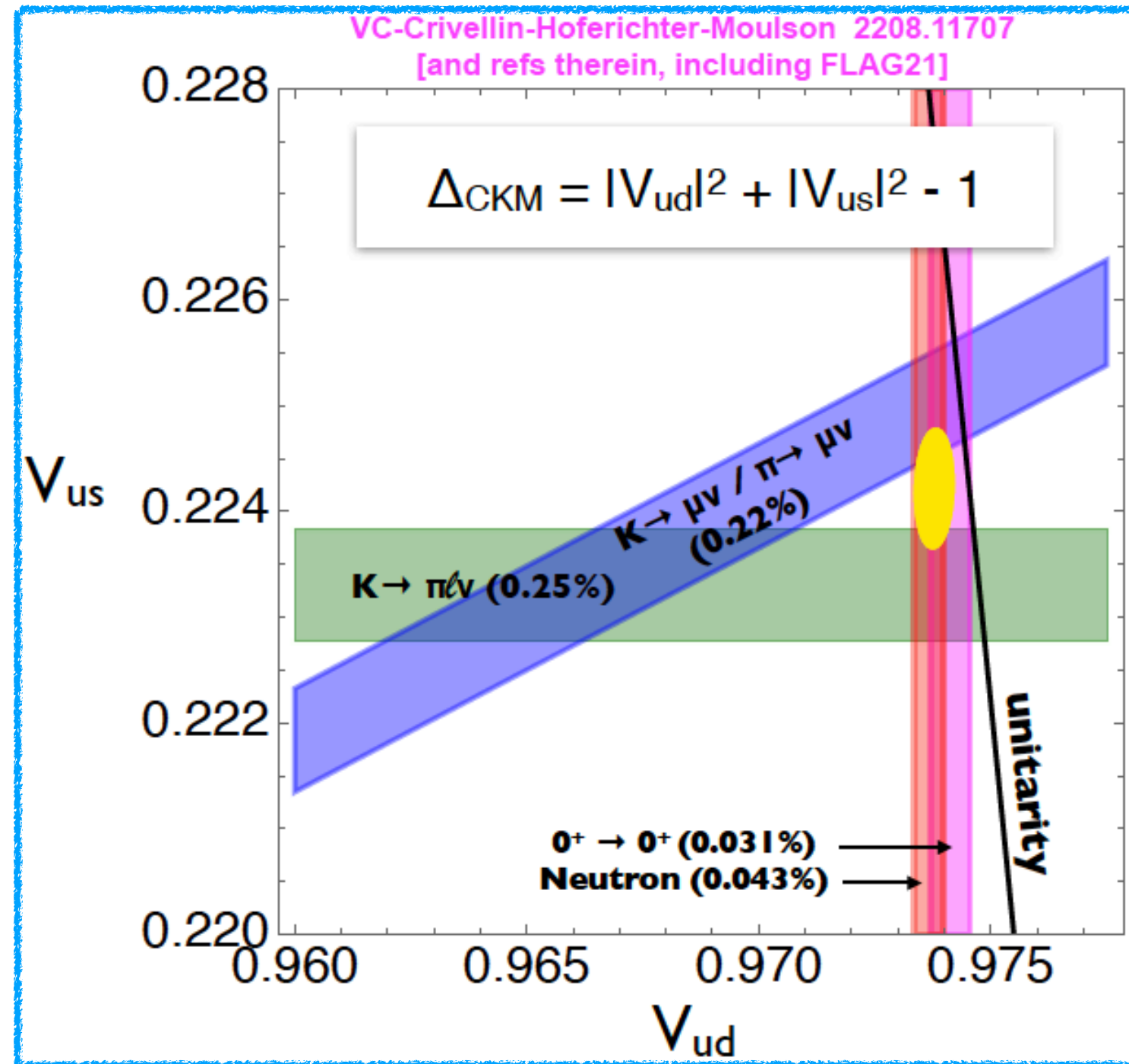


# List all the relevant operators



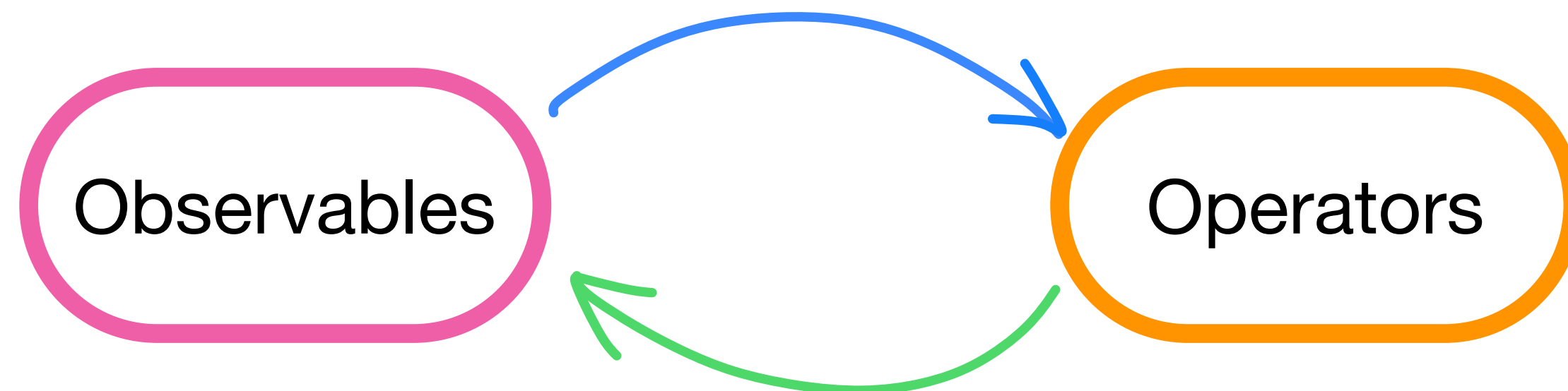
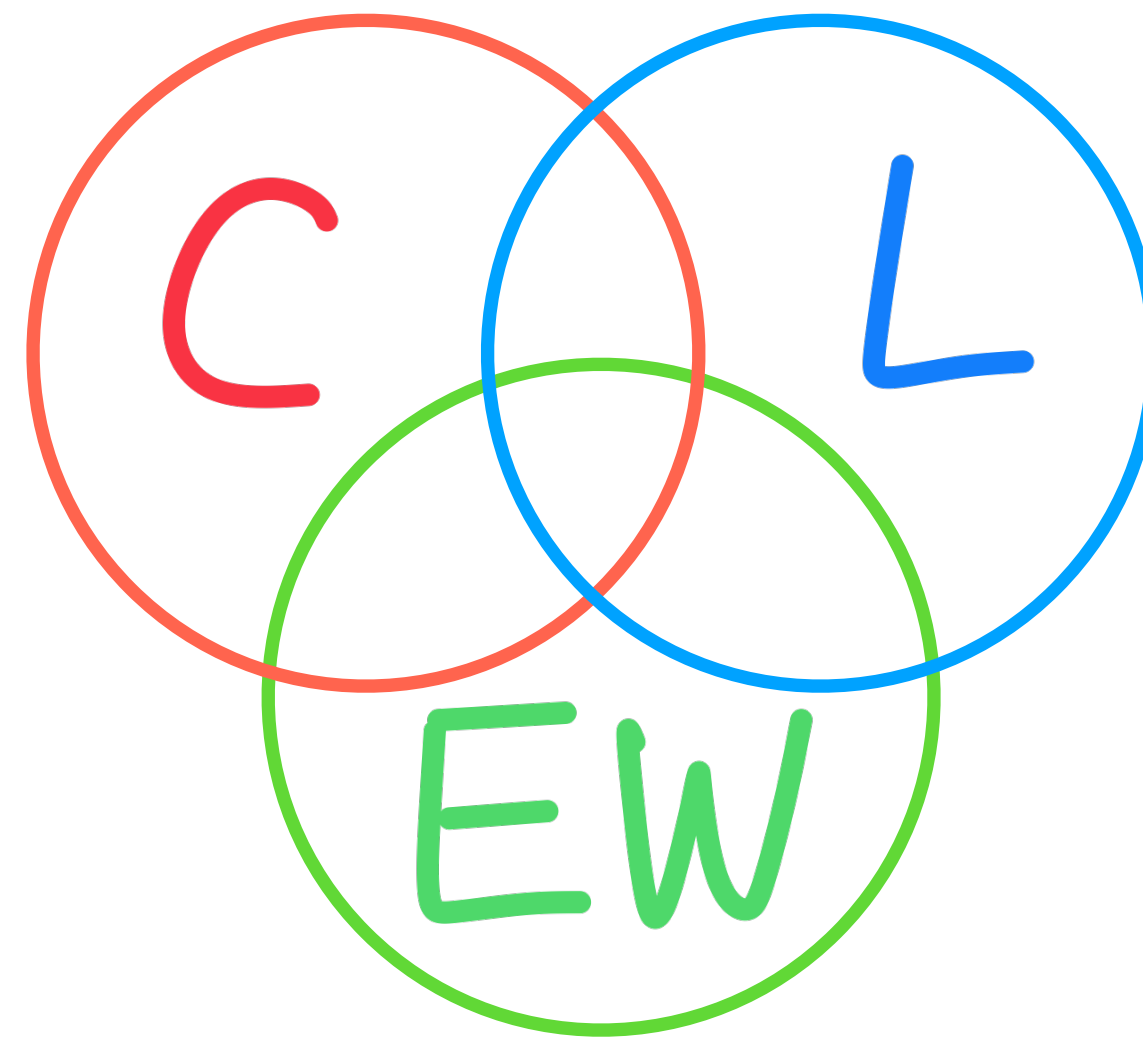
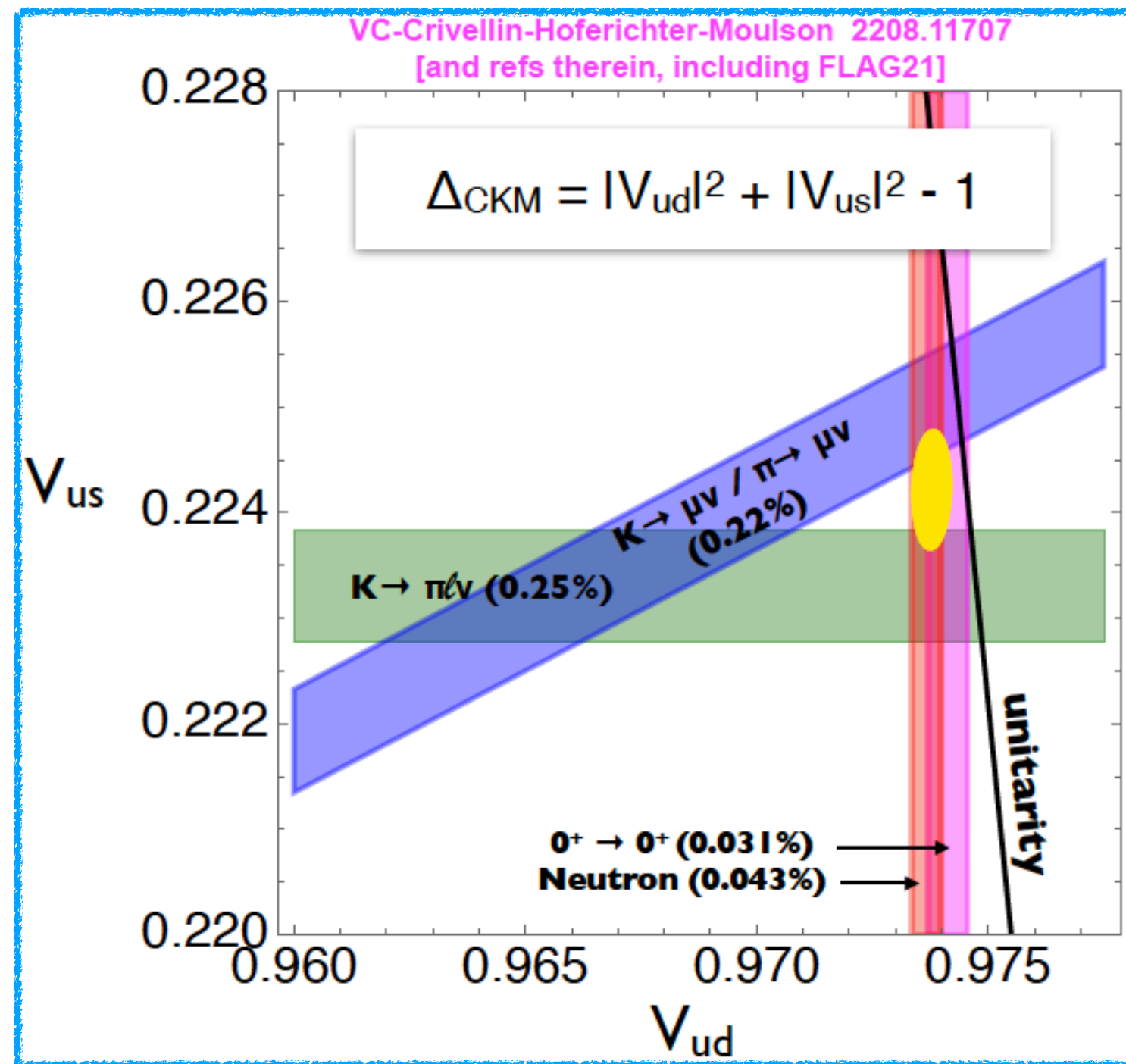


# List all the relevant operators





# List all the relevant operators

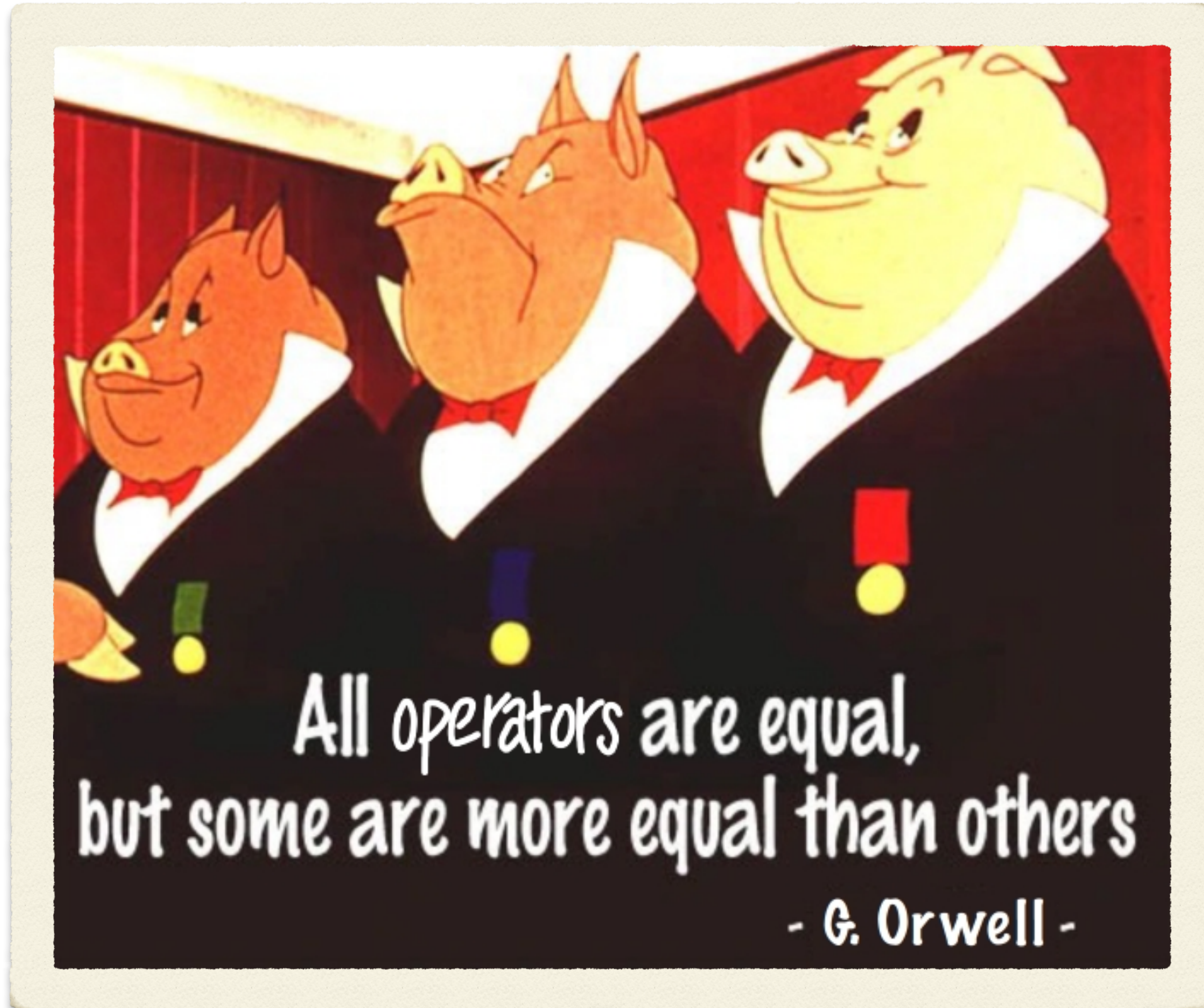


Operators		Low energy CC	EWPO	LHC
$H^4 D^2$				
$Q_{HD}$	$(H^\dagger D^\mu H)^* (H^\dagger D_\mu H)$	parameter shift ( $m_Z$ )		
$X^2 H^2$				
$Q_{HWB}$	$H^\dagger \tau^I H W_{\mu\nu}^I B^{\mu\nu}$			
		x	✓	✓
	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{l}_p \tau^I \gamma^\mu l_r)$	✓	✓	✓
$Q_{He}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{e}_p \gamma^\mu e_r)$	x	✓	✓
$Q_{Hq}^{(1)}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{q}_p \gamma^\mu q_r)$	x	✓	✓
$Q_{Hq}^{(3)}$	$(H^\dagger i \overleftrightarrow{D}_\mu^I H)(\bar{q}_p \tau^I \gamma^\mu q_r)$	✓	✓	✓
$Q_{Hu}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{u}_p \gamma^\mu u_r)$	x	✓	✓
$Q_{Hd}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{d}_p \gamma^\mu d_r)$	x	✓	✓
$Q_{Hud} + \text{h.c.}$	$i(\tilde{H}^\dagger D_\mu H)(\bar{u}_p \gamma^\mu d_r)$	✓	x	✓
$(\bar{L}L)(\bar{L}L)$				
$Q_u$	$(\bar{l}_p \gamma^\mu l_r)(\bar{l}_s \gamma_\mu l_t)$	parameter shift ( $G_F^{(\mu)}$ )		
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma^\mu l_r)(\bar{q}_s \gamma_\mu q_t)$	x	x	✓
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma^\mu \tau^I l_r)(\bar{q}_s \gamma_\mu \tau^I q_t)$	✓	x	✓
$(\bar{L}R)(\bar{R}L) + \text{h.c.}$				
$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s q_t^j)$	✓	x	✓
$(\bar{L}R)(\bar{L}R) + \text{h.c.}$				
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \epsilon_{jk} (\bar{q}_s^k u_t)$	✓	x	✓
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \epsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$	✓	x	✓

With all flavor indices



# All operators are equal, but...

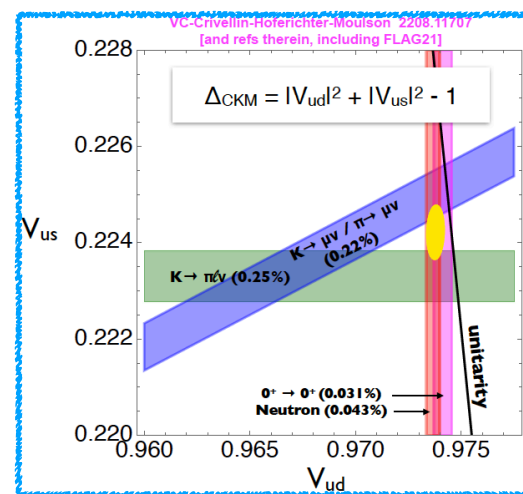


Operators		Low energy CC	EWPO	LHC
$H^4 D^2$				
$Q_{HD}$	$(H^\dagger D^\mu H)^* (H^\dagger D_\mu H)$	parameter shift ( $m_Z$ )		
$X^2 H^2$				
$Q_{HWB}$	$H^\dagger \tau^I H W_{\mu\nu}^I B^{\mu\nu}$			
		X	✓	✓
	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{l}_p \tau^I \gamma^\mu l_r)$	✓	✓	✓
$Q_{He}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{e}_p \gamma^\mu e_r)$	X	✓	✓
$Q_{Hq}^{(1)}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{q}_p \gamma^\mu q_r)$	X	✓	✓
$Q_{Hq}^{(3)}$	$(H^\dagger i \overleftrightarrow{D}_\mu^I H)(\bar{q}_p \tau^I \gamma^\mu q_r)$	✓	✓	✓
$Q_{Hu}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{u}_p \gamma^\mu u_r)$	X	✓	✓
$Q_{Hd}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{d}_p \gamma^\mu d_r)$	X	✓	✓
$Q_{Hud} + \text{h.c.}$	$i(\tilde{H}^\dagger D_\mu H)(\bar{u}_p \gamma^\mu d_r)$	✓	X	✓
$(\bar{L}L)(\bar{L}L)$				
$Q_u$	$(\bar{l}_p \gamma^\mu l_r)(\bar{l}_s \gamma_\mu l_t)$	parameter shift ( $G_F^{(\mu)}$ )		
$Q_{la}^{(1)}$	$(\bar{l}_p \gamma^\mu l_r)(\bar{q}_s \gamma_\mu q_t)$	X	X	✓
$Q_{la}^{(3)}$	$(\bar{l}_p \gamma^\mu \tau^I l_r)(\bar{q}_s \gamma_\mu \tau^I q_t)$	✓	X	✓
$(\bar{L}R)(\bar{R}L) + \text{h.c.}$				
$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s q_{tj})$	✓	X	✓
$(\bar{L}R)(\bar{L}R) + \text{h.c.}$				
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \epsilon_{jk} (\bar{q}_s^k u_t)$	✓	X	✓
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \epsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$	✓	X	✓

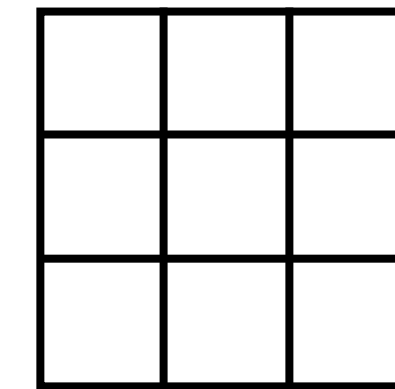
With all flavor indices



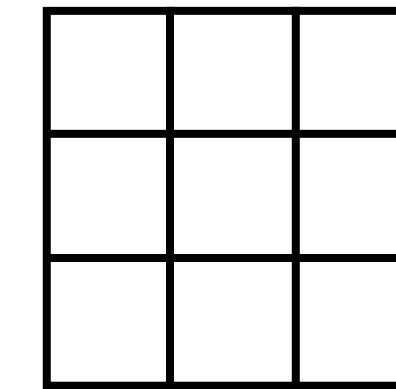
# All operators are equal, but...



$C_{Hg}^{(1)}$   
 $3 \times 3$

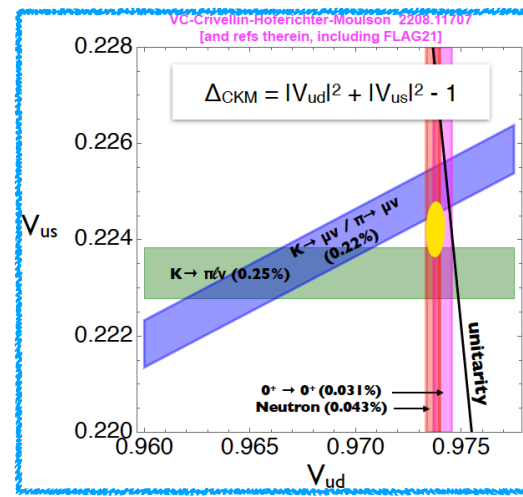


$C_{Hg}^{(3)}$   
 $3 \times 3$





# All operators are equal, but...

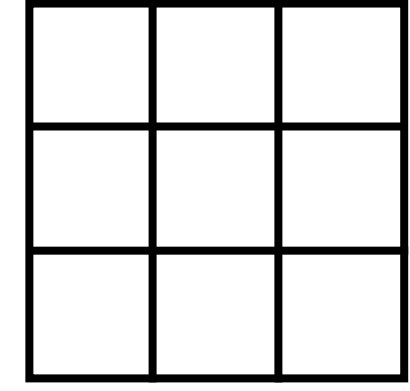


**Basis rotation**

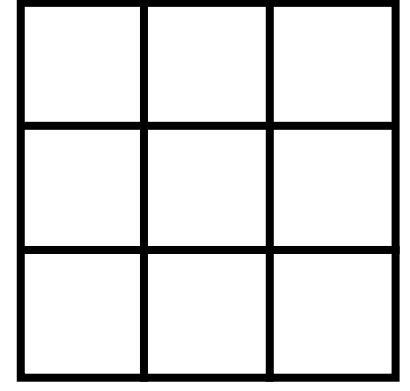


$$C_{Hq}^{(u)} = V \left[ C_{Hq}^{(1)} - C_{Hq}^{(3)} \right] V^\dagger, \quad C_{Hq}^{(d)} = C_{Hq}^{(1)} + C_{Hq}^{(3)}$$

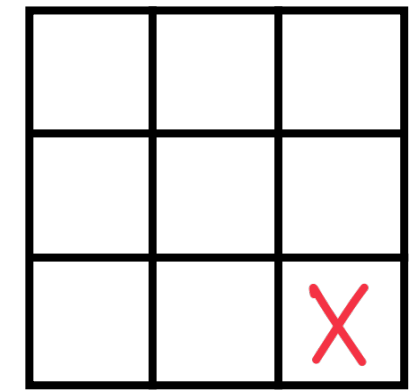
$C_{Hq}^{(1)}$   
3x3



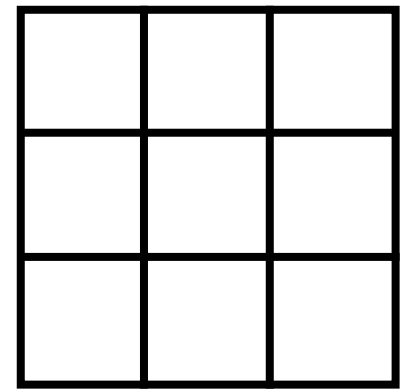
$C_{Hq}^{(3)}$   
3x3



$C_{Hq}^{(u)}$   
3x3

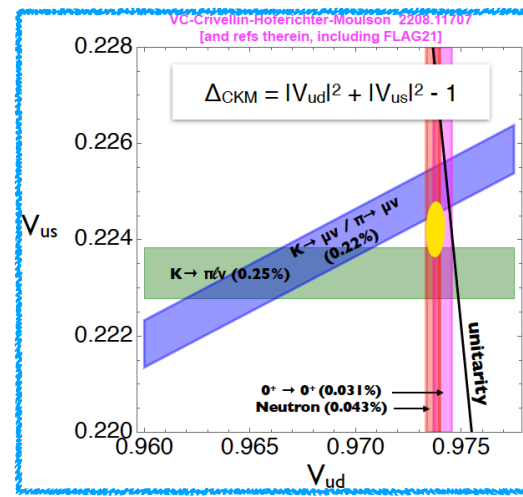


$C_{Hq}^{(d)}$   
3x3





# All operators are equal, but...

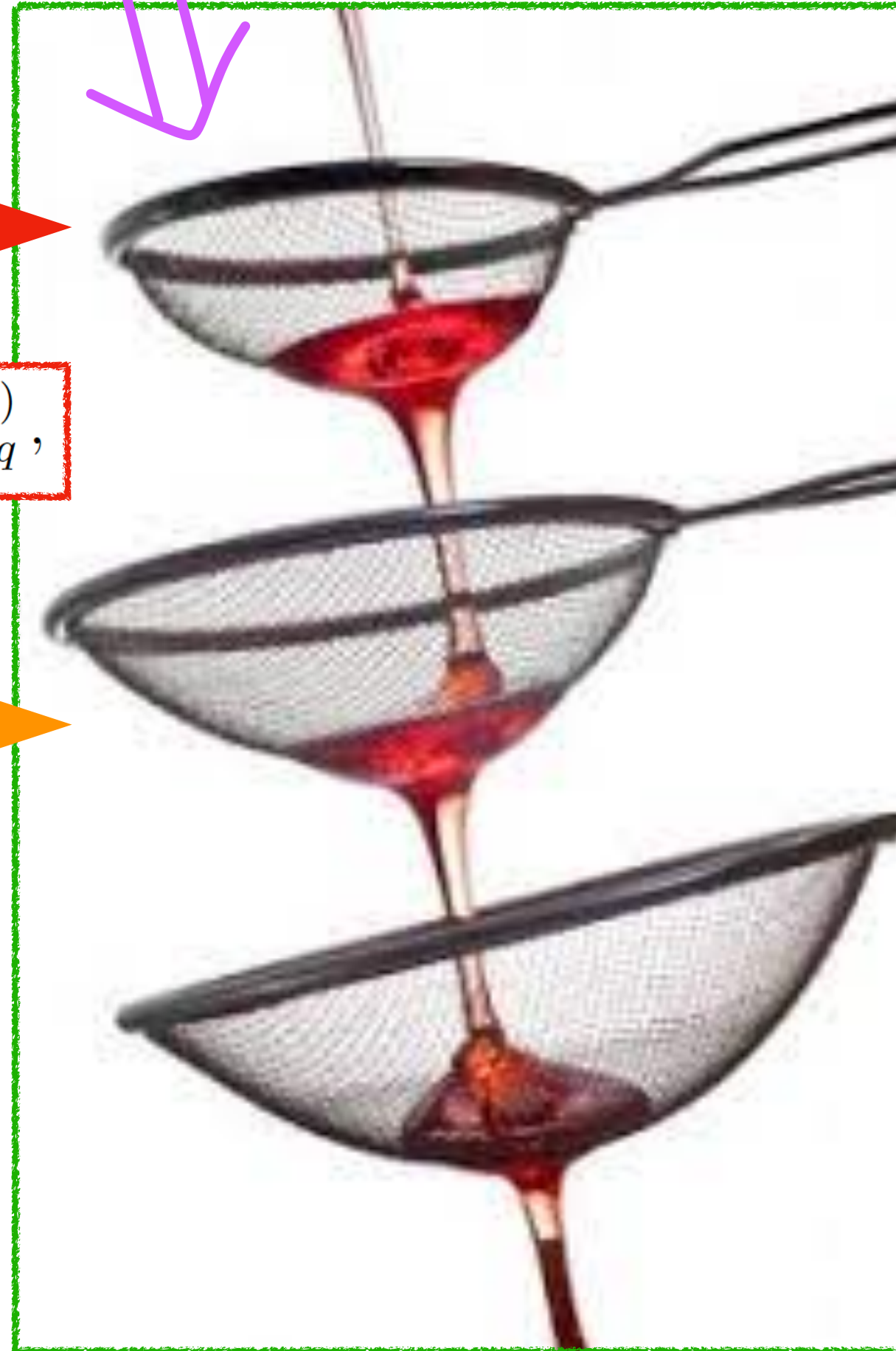


**Basis rotation**

$$C_{Hq}^{(u)} = V \left[ C_{Hq}^{(1)} - C_{Hq}^{(3)} \right] V^\dagger, \quad C_{Hq}^{(d)} = C_{Hq}^{(1)} + C_{Hq}^{(3)}$$

**Relative contribution**

Suppressed by  $|V_{us}|^2$  or  $(V_{ts}/V_{us})$



$C_{Hq}^{(1)}$   
3x3


$C_{Hq}^{(3)}$   
3x3


$C_{Hq}^{(u)}$   
3x3

		X

$C_{Hq}^{(d)}$   
3x3


$C_{Hq}^{(u)}$   
3x3

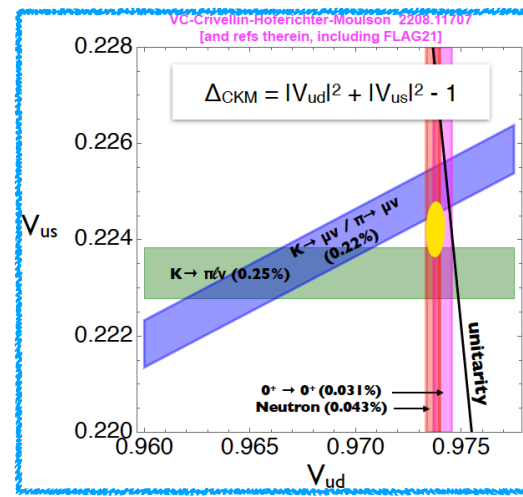
		X
X		X
X	X	X

$C_{Hq}^{(d)}$   
3x3

		X
		X



# All operators are equal, but...



**Basis rotation**

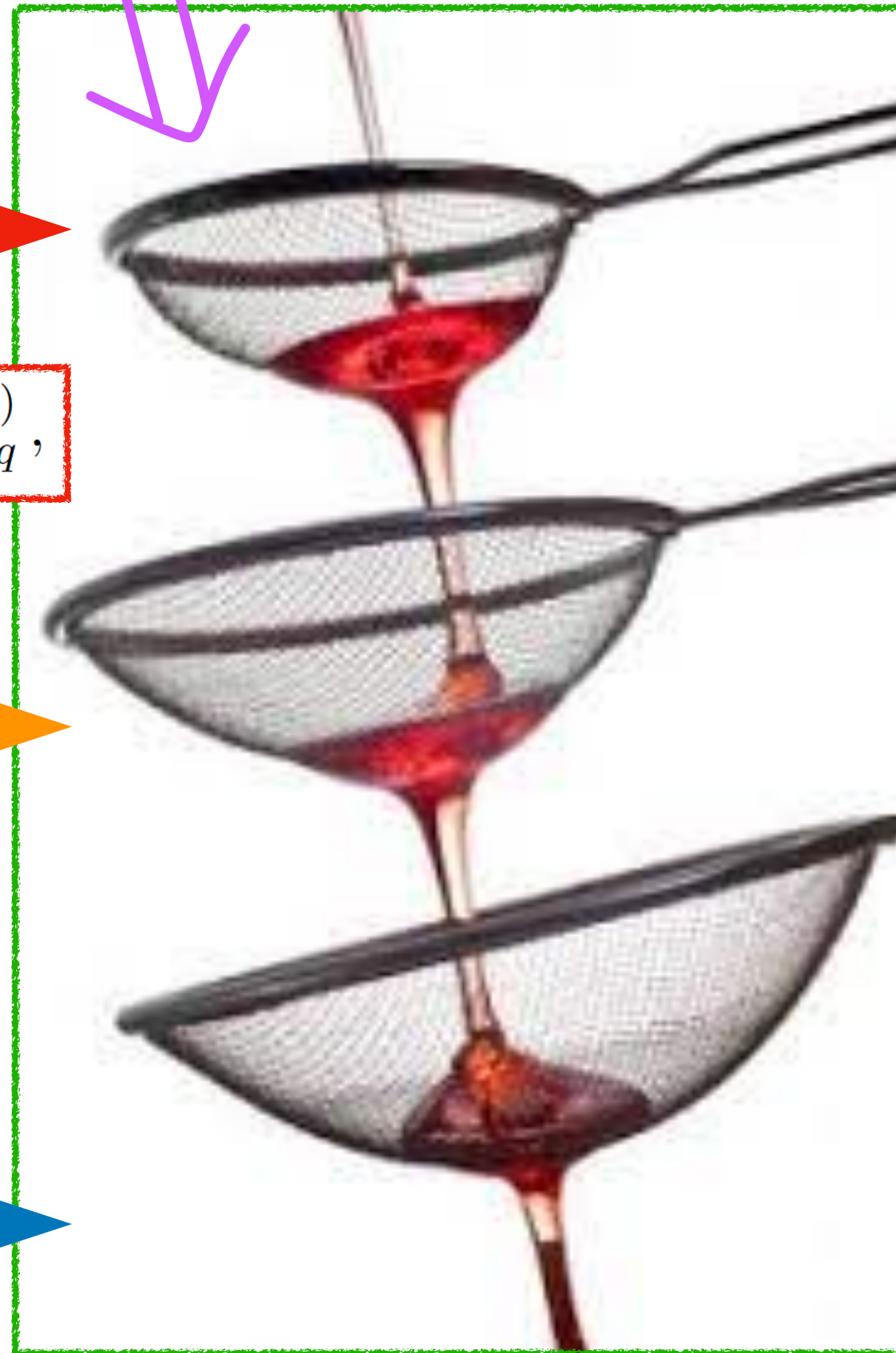
$$C_{Hq}^{(u)} = V \left[ C_{Hq}^{(1)} - C_{Hq}^{(3)} \right] V^\dagger, \quad C_{Hq}^{(d)} = C_{Hq}^{(1)} + C_{Hq}^{(3)}$$

**Relative contribution**

Suppressed by  $|V_{us}|^2$  or  $(V_{ts}/V_{us})$

**Pheno constraints**

FCNC decays of  $B$ ,  $D$  and  $K$  mesons



$C_{Hq}^{(1)}$   
3x3


$C_{Hq}^{(3)}$   
3x3


$C_{Hq}^{(u)}$   
3x3

		X

$C_{Hq}^{(d)}$   
3x3


$C_{Hq}^{(u)}$   
3x3

		X
X		X
X	X	X

$C_{Hq}^{(d)}$   
3x3

		X
		X

$C_{Hq}^{(u)}$   
3x3

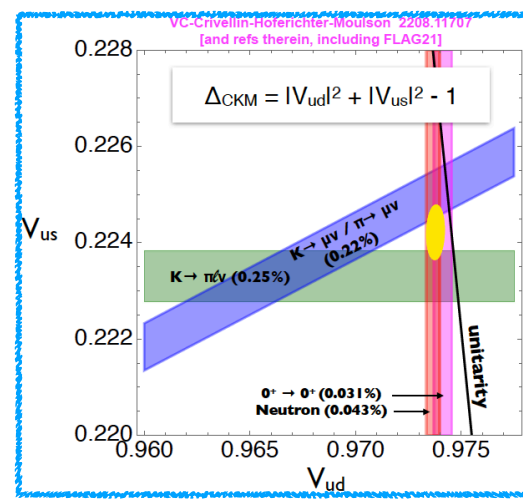
✓	X	X
X	✓	X
X	X	X

$C_{Hq}^{(d)}$   
3x3

✓	X	X
X	✓	X
X	X	✓



# All operators are equal, but...



**Basis rotation**

$$C_{Hq}^{(u)} = V \left[ C_{Hq}^{(1)} - C_{Hq}^{(3)} \right] V^\dagger, \quad C_{Hq}^{(d)} = C_{Hq}^{(1)} + C_{Hq}^{(3)}$$

**Relative contribution**

Suppressed by  $|V_{us}|^2$  or  $(V_{ts}/V_{us})$

**Pheno constraints**

FCNC decays of  $B$ ,  $D$  and  $K$  mesons



"More-equal" operators



$C_{Hq}^{(1)}$   
3x3


$C_{Hq}^{(3)}$   
3x3


$C_{Hq}^{(u)}$   
3x3

		X

$C_{Hq}^{(d)}$   
3x3


$C_{Hq}^{(u)}$   
3x3

		X
X		X
X	X	X

$C_{Hq}^{(d)}$   
3x3

		X
		X

$C_{Hq}^{(u)}$   
3x3

✓	X	X
X	✓	X
X	X	X

$C_{Hq}^{(d)}$   
3x3

✓	X	X
X	✓	X
X	X	✓

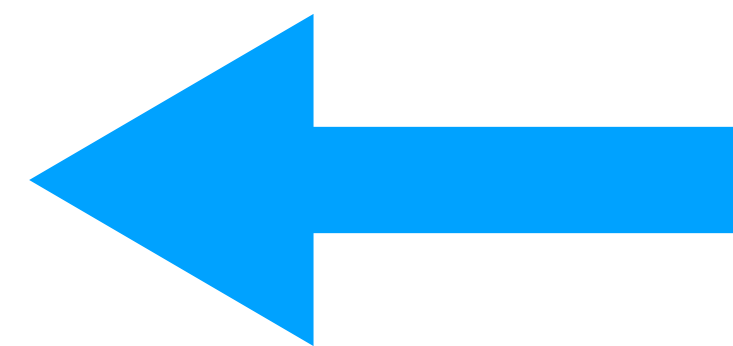


# 37 operators are "more equal"

Global analysis	Indices
$C_{Hl}^{(1,3)}_{pr}, C_{He}_{pr}$	$pr \in \{ee, \mu\mu, \tau\tau\}$
$C_{Hq}^{(d)}_{pr}, C_{Hd}_{pr}$	$pr \in \{11, 22, 33\}$
$C_{Hq}^{(u)}_{pr}, C_{Hu}_{pr}$	$pr \in \{11, 22\}$
$C_{Hud}_{pr}$	$pr \in \{11, 12\}$
$C_{lq}^{(d)}_{llpr}, C_{ledq}_{llpr}$	$l \in \{e, \mu\}, pr \in \{11, 22\}$
$C_{lq}^{(u)}_{ll11}, \bar{C}_{lequ}_{ll11}^{(1,3)}$	$l \in \{e, \mu\}$
$C_{HD}, C_{HWB}$	
$C_{ll}^{2112}$	



**37 in total**



Fit!

Operators		Low energy CC	EWPO	LHC
$H^4 D^2$				
$Q_{HD}$	$(H^\dagger D^\mu H)^* (H^\dagger D_\mu H)$	parameter shift ( $m_Z$ )		
$X^2 H^2$				
$Q_{HWB}$	$H^\dagger \tau^I H W_{\mu\nu}^I B^{\mu\nu}$			
		x	✓	✓
		✓	✓	✓
$Q_{He}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{e}_p \gamma^\mu e_r)$	x	✓	✓
$Q_{Hq}^{(1)}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{q}_p \gamma^\mu q_r)$	x	✓	✓
$Q_{Hq}^{(3)}$	$(H^\dagger i \overleftrightarrow{D}_\mu^I H)(\bar{q}_p \tau^I \gamma^\mu q_r)$	✓	✓	✓
$Q_{Hu}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{u}_p \gamma^\mu u_r)$	x	✓	✓
$Q_{Hd}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{d}_p \gamma^\mu d_r)$	x	✓	✓
$Q_{Hud} + \text{h.c.}$	$i(\tilde{H}^\dagger D_\mu H)(\bar{u}_p \gamma^\mu d_r)$	✓	x	✓
$(\bar{L}L)(\bar{L}L)$				
$Qu$	$(\bar{l}_p \gamma^\mu l_r)(\bar{l}_s \gamma_\mu l_t)$	parameter shift ( $G_F^{(\mu)}$ )		
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma^\mu l_r)(\bar{q}_s \gamma_\mu q_t)$	x	x	✓
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma^\mu \tau^I l_r)(\bar{q}_s \gamma_\mu \tau^I q_t)$	✓	x	✓
$(\bar{L}R)(\bar{R}L) + \text{h.c.}$				
$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s^k q_t^j)$	✓	x	✓
$(\bar{L}R)(\bar{L}R) + \text{h.c.}$				
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \epsilon_{jk} (\bar{q}_s^k u_t)$	✓	x	✓
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \epsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$	✓	x	✓

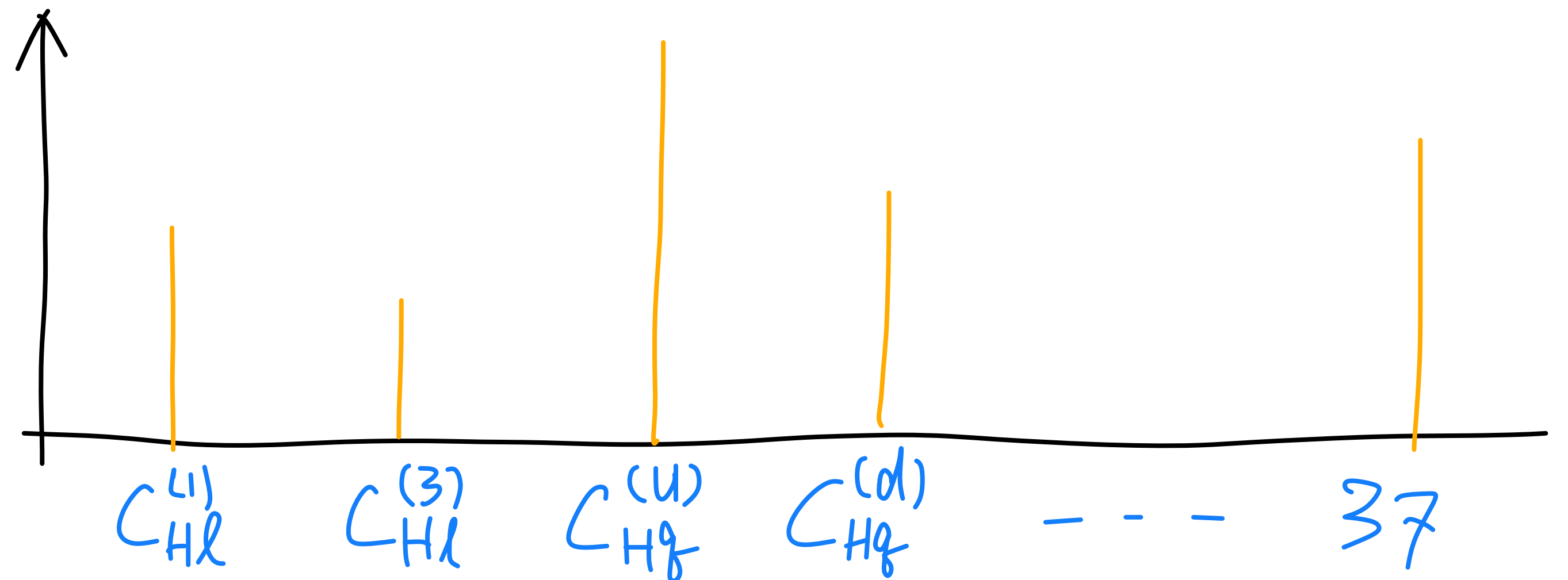
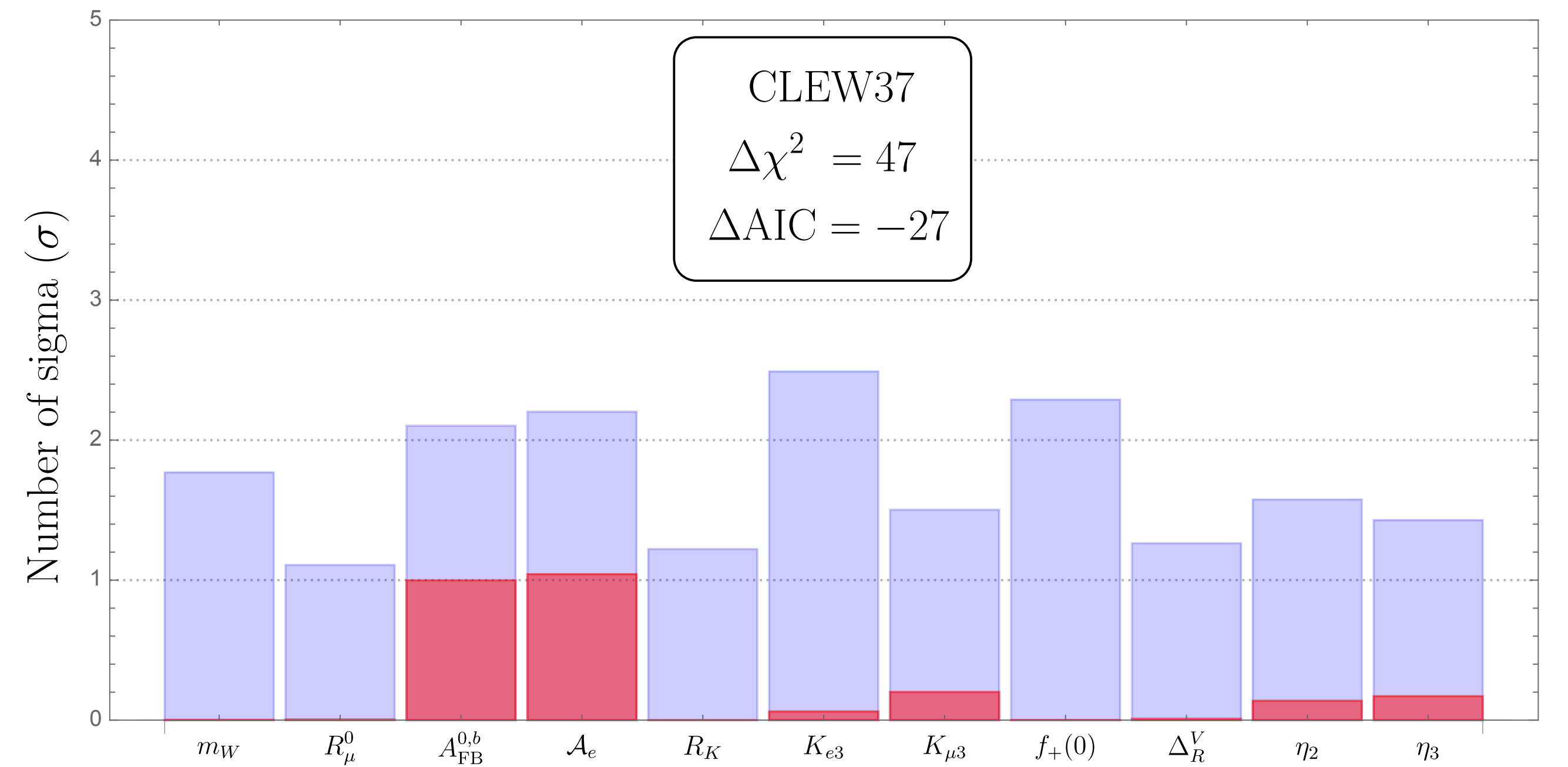
With all flavor indices

# Conclusion

Global analysis	Indices
$C_{Hl}^{(1,3)}$ , $C_{He}^{pr}$	$pr \in \{ee, \mu\mu, \tau\tau\}$
$C_{Hq}^{(d)}$ , $C_{Hd}^{pr}$	$pr \in \{11, 22, 33\}$
$C_{Hq}^{(u)}$ , $C_{Hu}^{pr}$	$pr \in \{11, 22\}$
$C_{Hud}^{pr}$	$pr \in \{11, 12\}$
$C_{lq}^{(d)}$ , $C_{ledq}^{llpr}$	$l \in \{e, \mu\}$ , $pr \in \{11, 22\}$
$C_{lq}^{(u)}$ , $\bar{C}_{lequ}^{(1,3)}$	$l \in \{e, \mu\}$
$C_{HD}$ , $C_{HWB}$	
$C_{ll}^{2112}$	



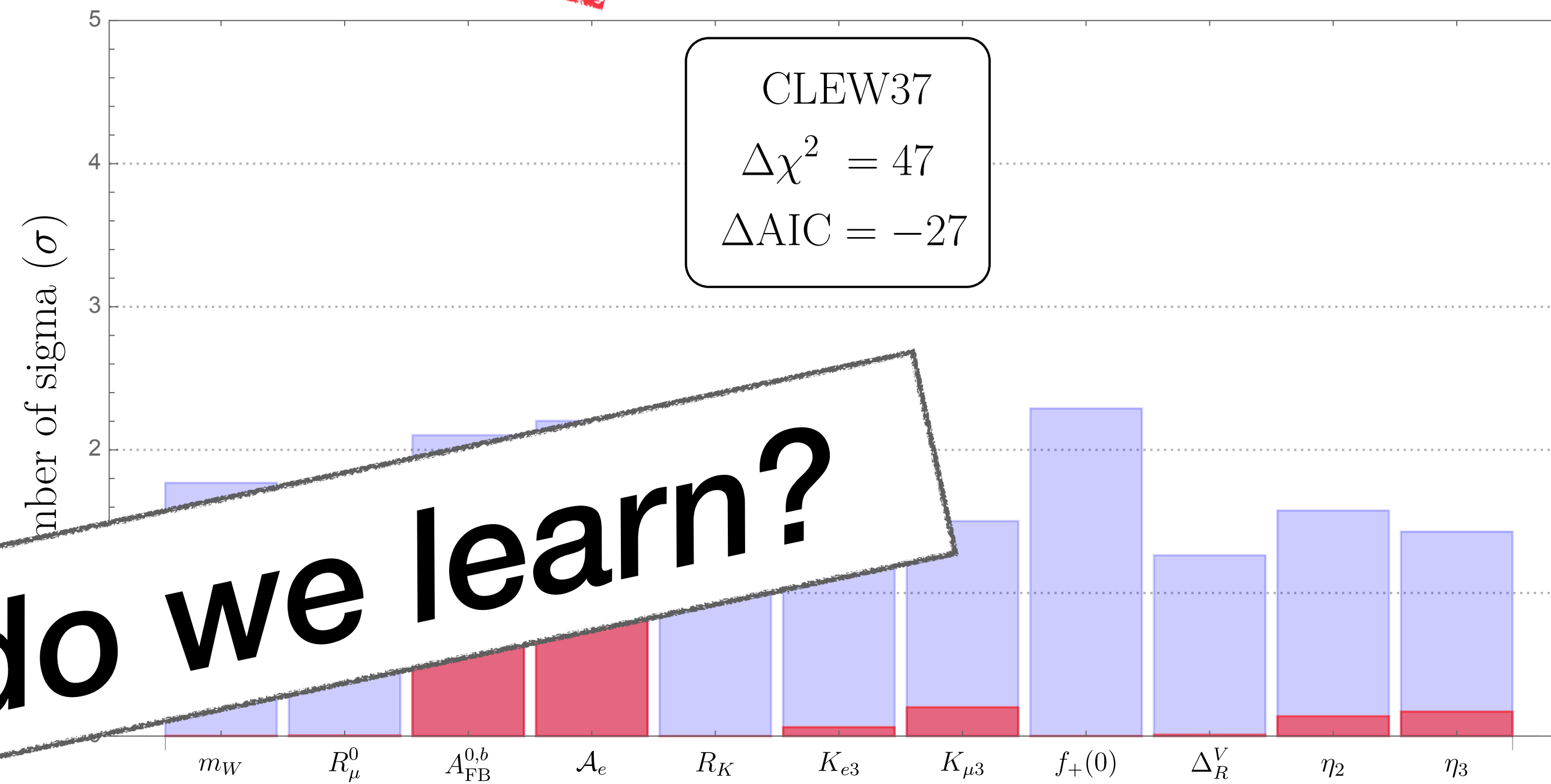
37 in total





# ~~Conclusion~~

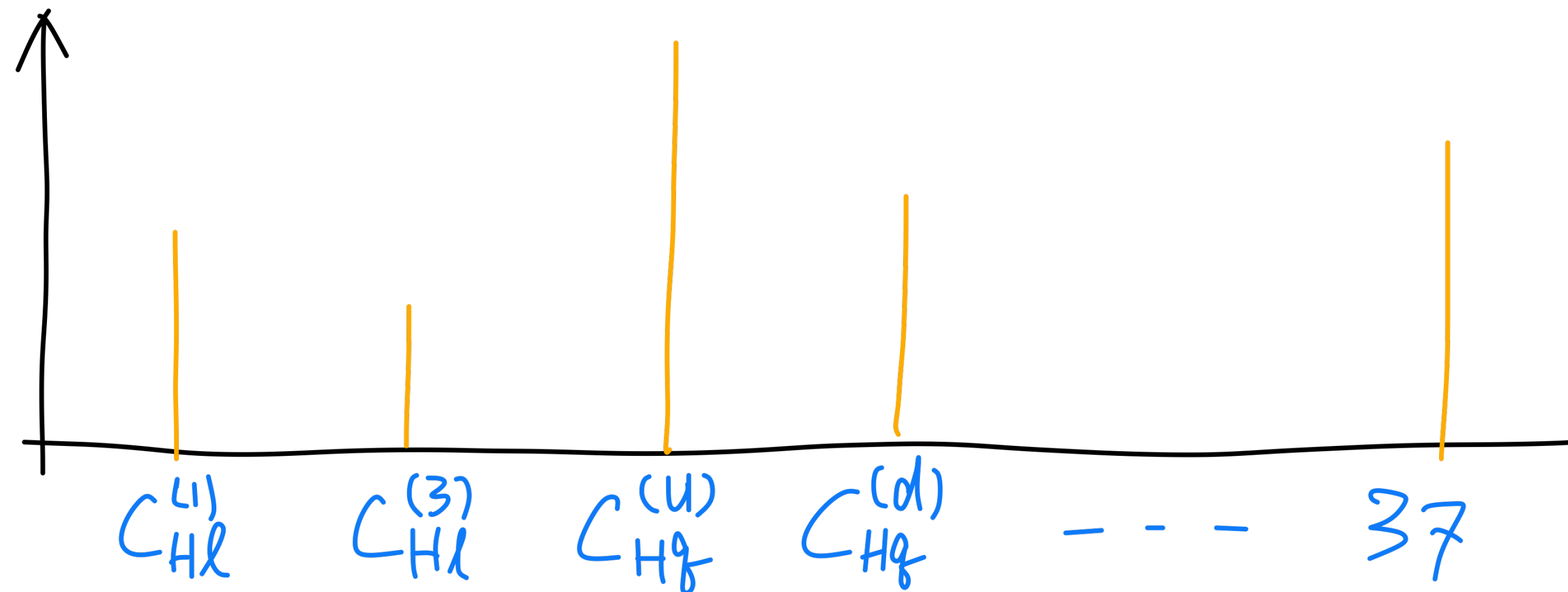
Global analysis	Indices
$C_{Hl}^{(1,3)}$ , $C_{He}^{pr}$	$pr \in \{ee, \mu\mu, \tau\tau\}$
$C_{Hq}^{(d)}$ , $C_{Hd}^{pr}$	$pr \in \{11, 22, 33\}$
$C_{Hq}^{(u)}$ , $C_{Hu}^{pr}$	$pr \in \{11, 22\}$
$C_{Hud}^{pr}$	$pr \in \{11, 12\}$
$C_{lq}^{(d)}$ , $C_{ledq}^{llpr}$	$l \in \{e, \mu\}$
$C_{lq}^{(u)}$ , $\bar{C}_{lequ}^{(1,3)}$	$l \in \{e, \mu\}$
$C_{HD}$ , $C_{HWB}$	
$C_{ll}^{2112}$	



What do we learn?



37 in total



# Still, some are more equal

Global analysis	Indices
$C_{Hl}^{(1,3)}$ , $C_{He}^{pr}$	$pr \in \{ee, \mu\mu, \tau\tau\}$
$C_{Hq}^{(d)}$ , $C_{Hd}^{pr}$	$pr \in \{11, 22, 33\}$
$C_{Hq}^{(u)}$ , $C_{Hu}^{pr}$	$pr \in \{11, 22\}$
$C_{Hud}^{pr}$	$pr \in \{11, 12\}$
$C_{lq}^{(d)}$ , $C_{ledq}^{llpr}$	$l \in \{e, \mu\}$ , $pr \in \{11, 22\}$
$C_{lq}^{(u)}$ , $C_{lequ}^{(1,3)}$ $ll11$ $ll11$	$l \in \{e, \mu\}$
$C_{HD}$ $C_{HWB}$	
$C_{ll}^{2112}$	



Let's do  $2^{37} \approx 10^{11}$  fits!



# Group them into 10 categories

Global analysis	Indices
$C_{Hl\ pr}^{(1,3)}$ , $C_{He\ pr}$	$pr \in \{ee, \mu\mu, \tau\tau\}$
$C_{Hq\ pr}^{(d)}$ , $C_{Hd\ pr}$	$pr \in \{11, 22, 33\}$
$C_{Hq\ pr}^{(u)}$ , $C_{Hu\ pr}$	$pr \in \{11, 22\}$
$C_{Hud\ pr}$	$pr \in \{11, 12\}$
$C_{lq\ llpr}^{(d)}$ , $C_{ledq\ llpr}$	$l \in \{e, \mu\}$ , $pr \in \{11, 22\}$
$C_{lq\ ll11}^{(u)}$ , $\bar{C}_{lequ\ ll11}^{(1,3)}$	$l \in \{e, \mu\}$
$C_{HD}$ , $C_{HWB}$	
$C_{2112\ ll}$	

Category	Operators	Description	# of Ops.
I.	$C_{ST}$	Oblique corrections	1
II.	$C_{Hud}$	RH charged currents	2
III.	$C_{Hl}^{(1)}$ , $C_{Hl}^{(3)}$	LH lepton vertices	6
IV.	$C_{He}$	RH lepton vertices	3
V.	$C_{Hq}^{(u)}$ , $C_{Hq}^{(d)}$	LH quark vertices	5
VI.	$C_{Hu}$ , $C_{Hd}$	RH quark vertices	5
VII.	$C_{ll}$	Lepton 4-fermion	1
VIII.	$C_{lq}^{(u)}$ , $C_{lq}^{(d)}$	Semilepton 4-fermion	6
IX.	$C_{ledq}$ , $C_{lequ}^{(1)}$	Scalar 4-fermion	6
X.	$C_{lequ}^{(3)}$	Tensor 4-fermion	2

~~Let's do  $2^{37} \approx 10^{11}$  fits!~~

Let's do  $2^{10} = 1024$  fits!

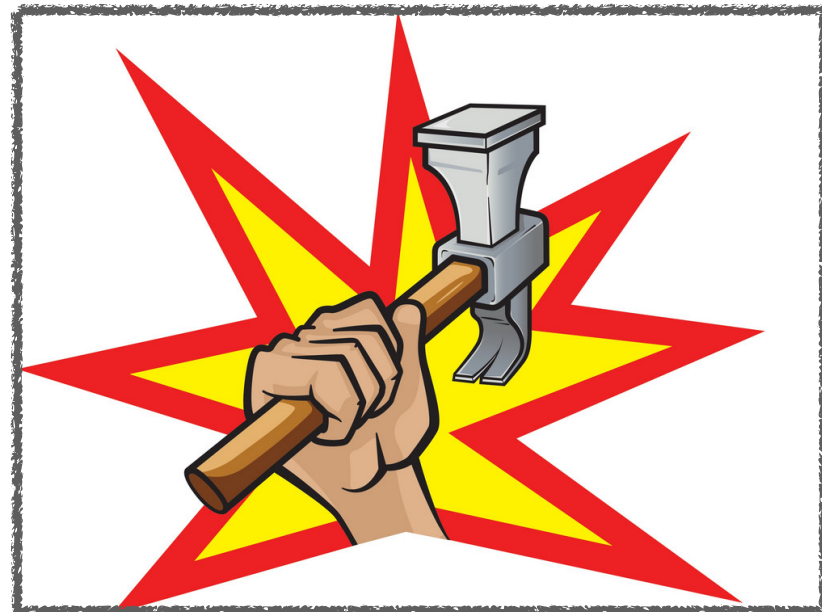


# AIC and one thousand fits



## Akaike Information Criterion

$$\text{AIC} = \chi^2 + 2 \times (\text{number of Ops.})$$



Category	Operators	Description	# of Ops.
I.	$C_{ST}$	Oblique corrections	1
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X.	$C_{lequ}^{(3)}$	Tensor 4-fermion	2

**Let's do  $2^{10} = 1024$  fits!**

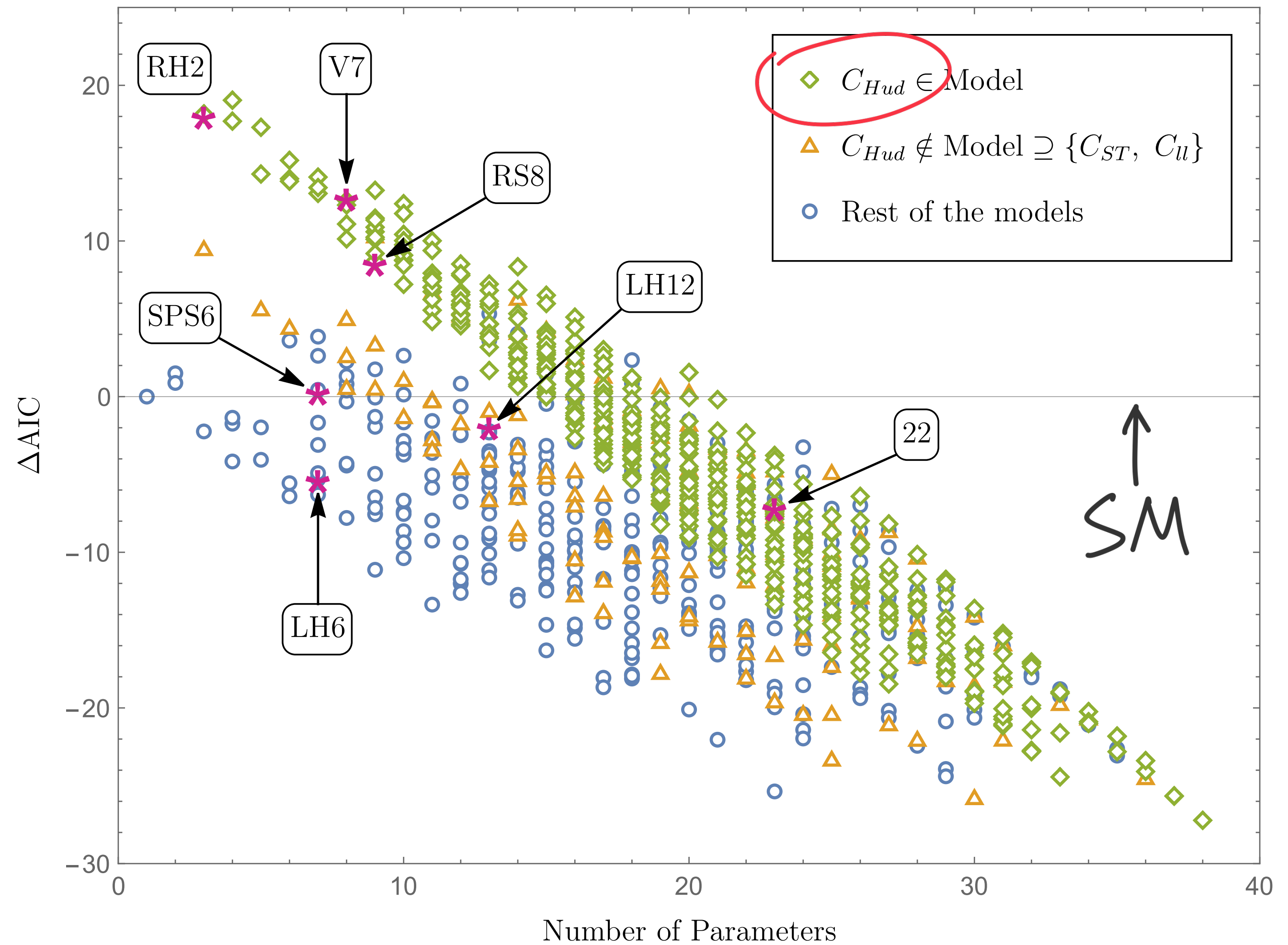
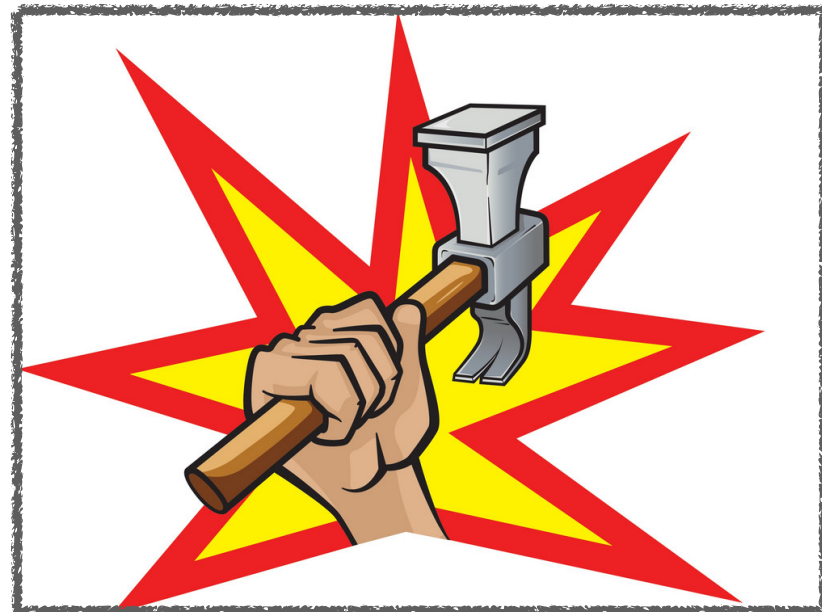


# AIC and one thousand fits



## Akaike Information Criterion

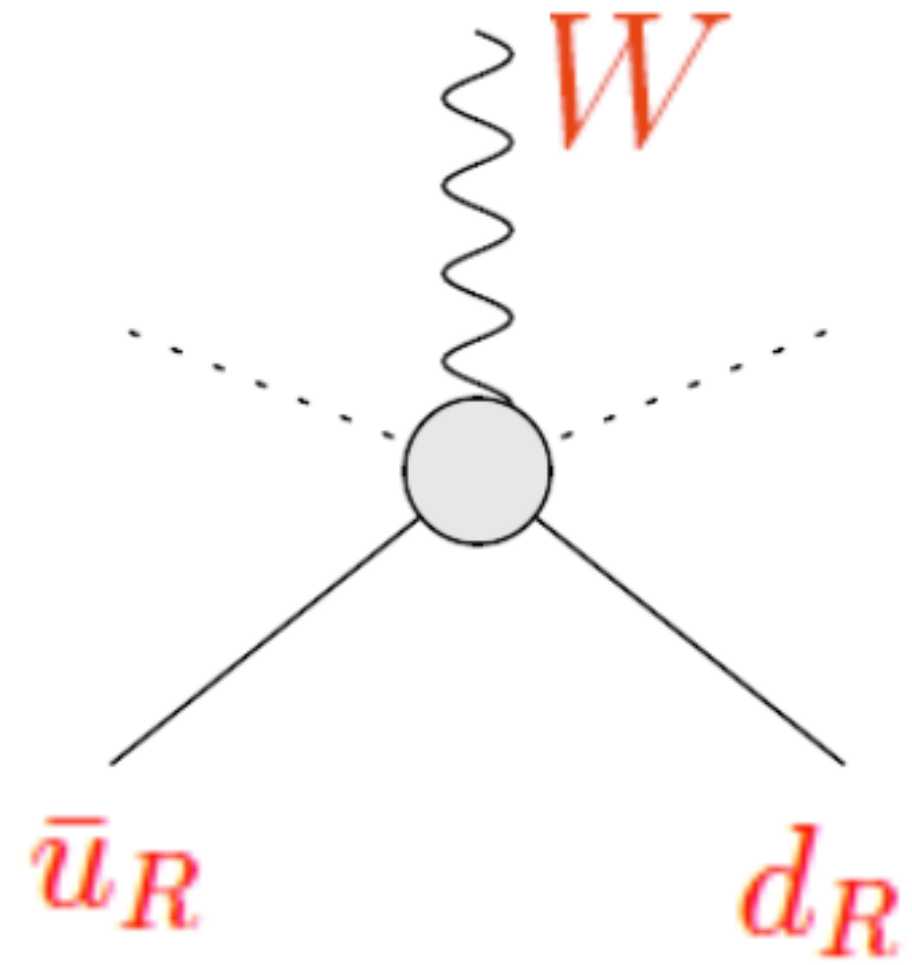
$$AIC = \chi^2 + 2 \times (\text{number of Ops.})$$



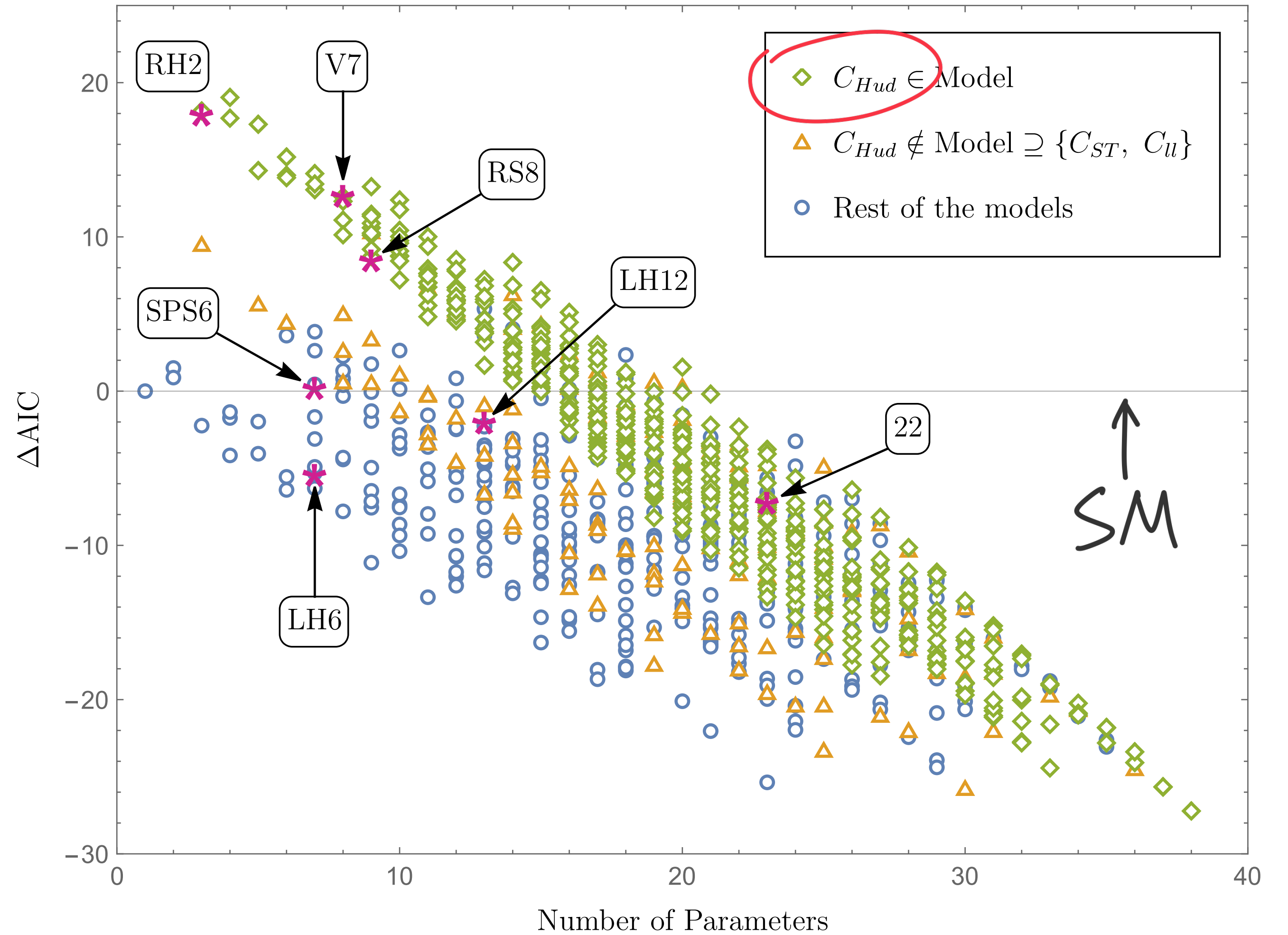
Higher the  $\Delta AIC$ , better the model



# Who is $C_{Hud}$ ?



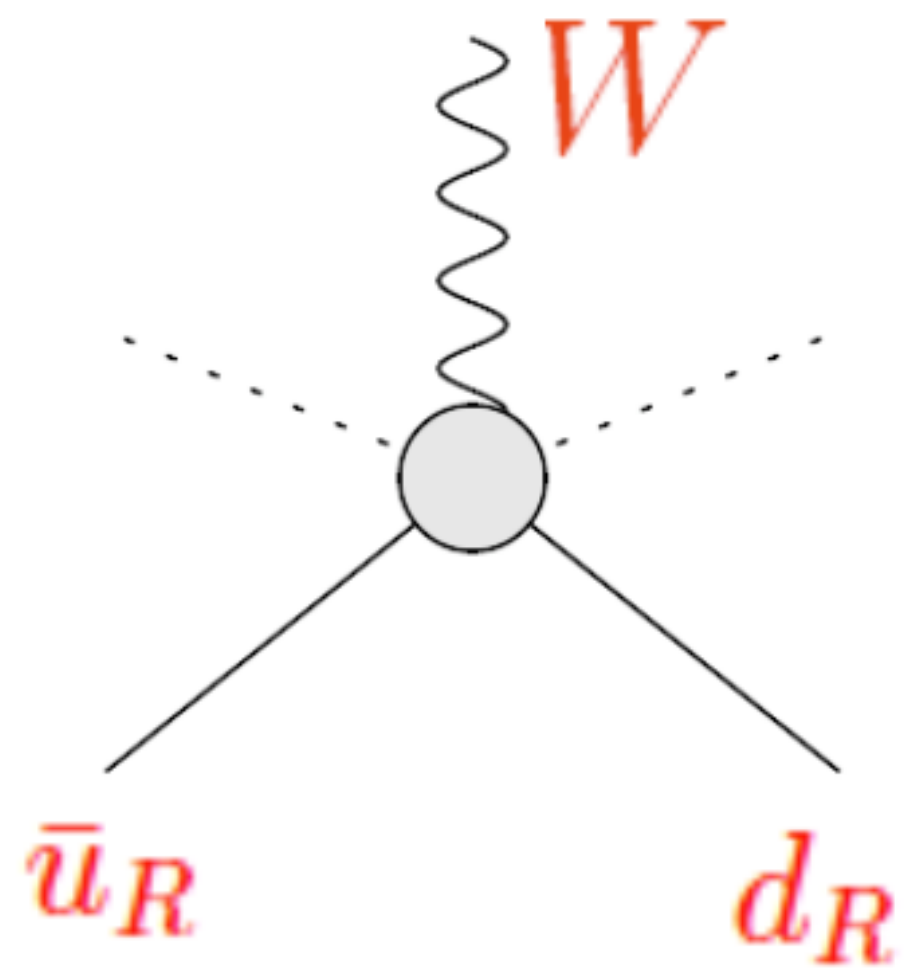
$$Q_{Hud} = i(\tilde{H}^\dagger D_\mu H)(\bar{u}_p \gamma^\mu d_r)$$



Higher the  $\Delta AIC$ , better the model



# Who is $C_{Hud}$ ?



$C_{Hud}$

$\sim Y_u Y_d^\dagger$  in MFV

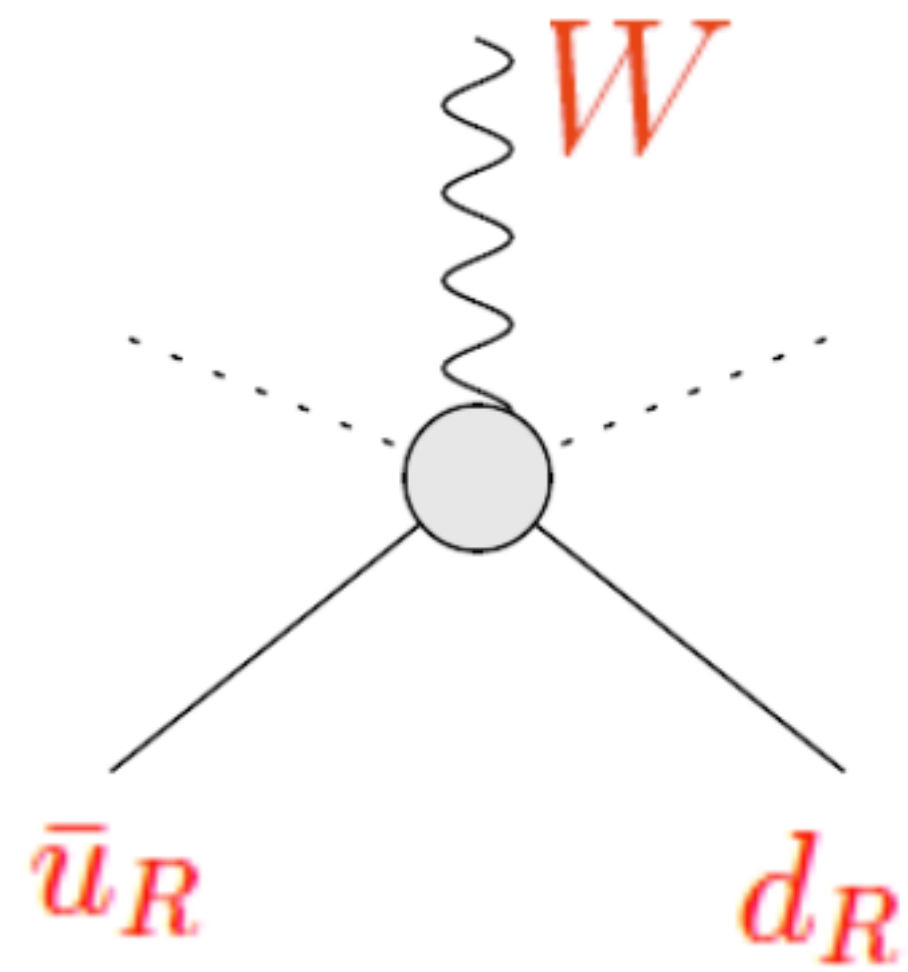
$$Q_{Hud} = i(\tilde{H}^\dagger D_\mu H)(\bar{u}_p \gamma^\mu d_r)$$

LEFT

$$\mathcal{L}_\beta = -\frac{G_F}{\sqrt{2}} V_{uD} \left[ \bar{\ell} \gamma_\mu (1 - \gamma_5) \nu_\ell \left( (1 + \epsilon_L^{\ell D} - \epsilon_L^\mu) \bar{u} \gamma^\mu (1 - \gamma_5) D + \epsilon_R^{\ell D} \bar{u} \gamma^\mu (1 + \gamma_5) D \right) \right. \\ \left. + \bar{\ell} (1 - \gamma_5) \nu_\ell \left( \epsilon_S^{\ell D} \bar{u} D + \epsilon_P^{\ell D} \bar{u} \gamma_5 D \right) + \epsilon_T^{\ell D} \bar{\ell} \sigma_{\mu\nu} (1 - \gamma_5) \nu_\ell \bar{u} \sigma^{\mu\nu} (1 - \gamma_5) D \right] + \text{h.c.},$$



# Who is $C_{Hud}$ ?



$C_{Hud}$

$\sim Y_u Y_d^\dagger$  in MFV

$$Q_{Hud} = i(\tilde{H}^\dagger D_\mu H)(\bar{u}_p \gamma^\mu d_r)$$

- Left-Right Symmetric Models

2107.10852

- Vector-Like Quarks  $\sim \mathcal{O}(\text{TeV})$

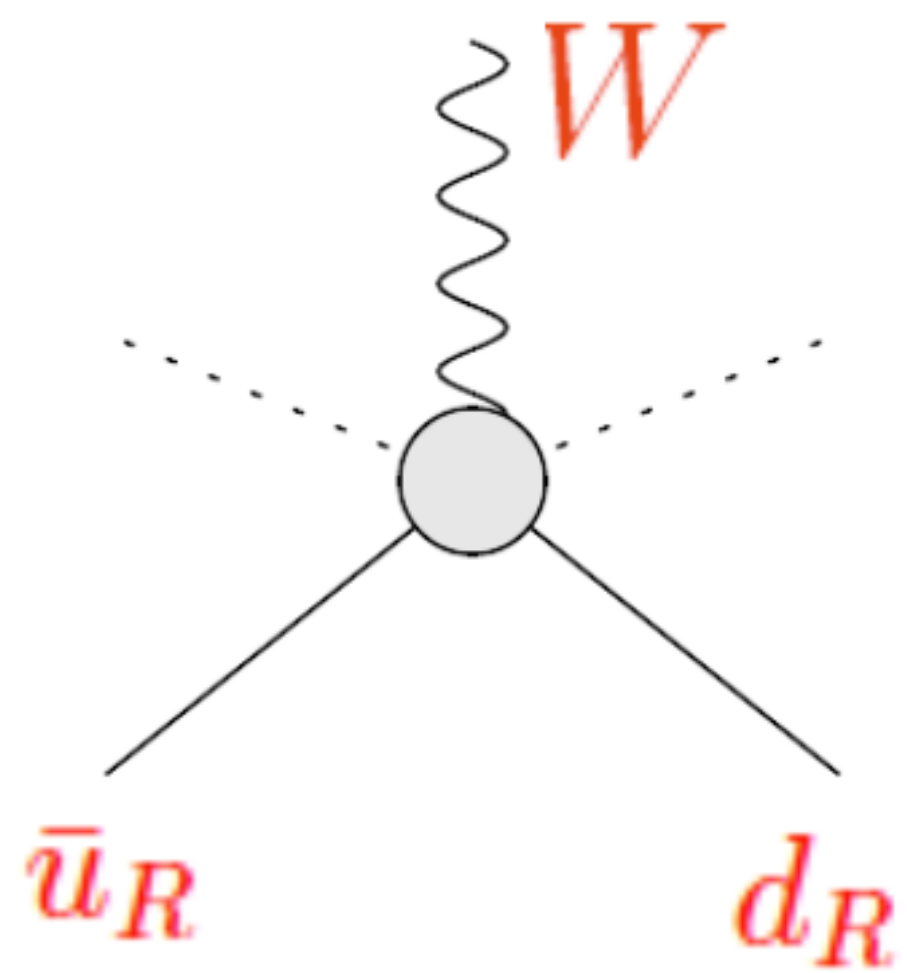
2212.06862, 2302.14097

LEFT

$$\left. \begin{aligned} &+ \epsilon_L^{\ell D} - \epsilon_L^\mu \bar{u} \gamma^\mu (1 - \gamma_5) D + \epsilon_R^{\ell D} \bar{u} \gamma^\mu (1 + \gamma_5) D \\ &+ \epsilon_T^{\ell D} \bar{\ell} \sigma_{\mu\nu} (1 - \gamma_5) \nu_\ell \bar{u} \sigma^{\mu\nu} (1 - \gamma_5) D \end{aligned} \right] + \text{h.c.},$$



# $C_{Hud}$ solves Cabibbo



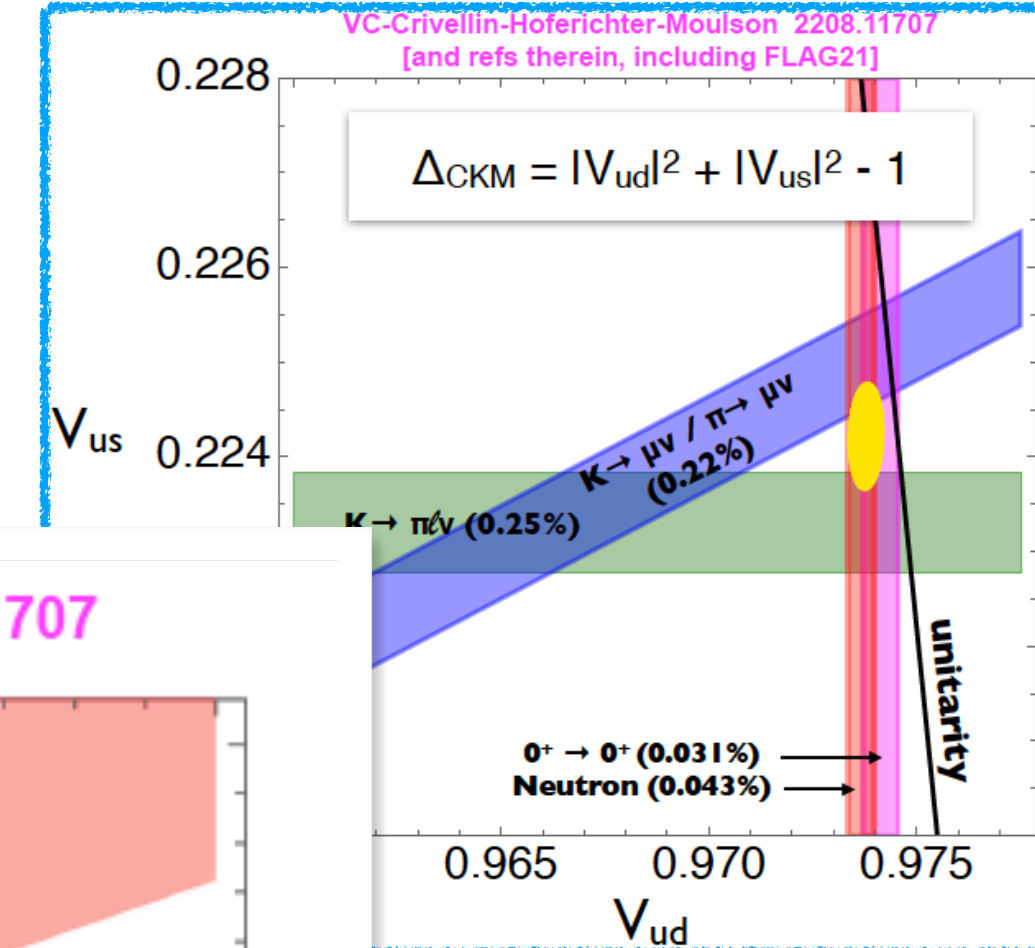
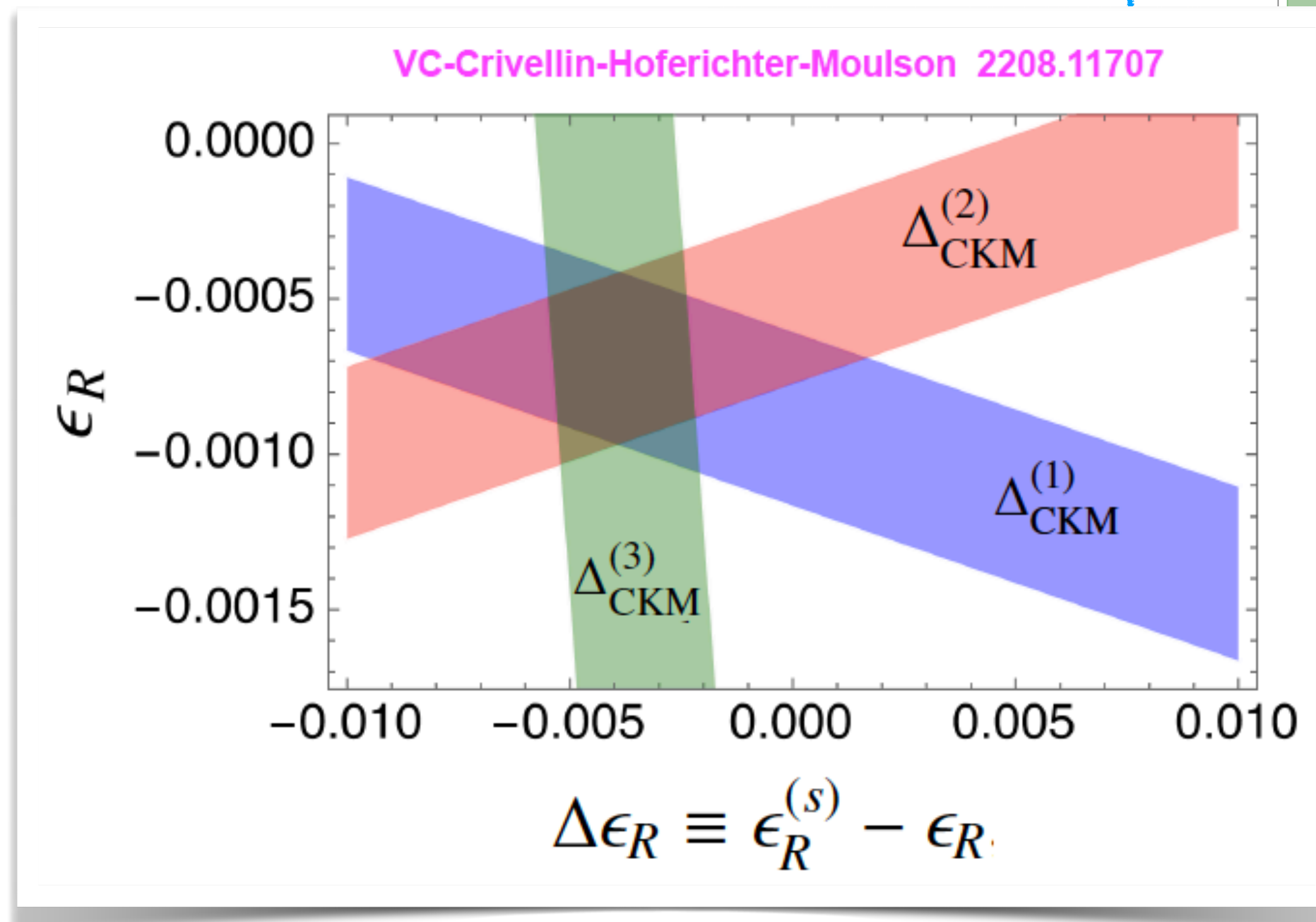
$$Q_{Hud} = i(\tilde{H}^\dagger D_\mu H)(\bar{u}_p \gamma^\mu d_r)$$

- Left-Right Symmetric Models

2107.10852

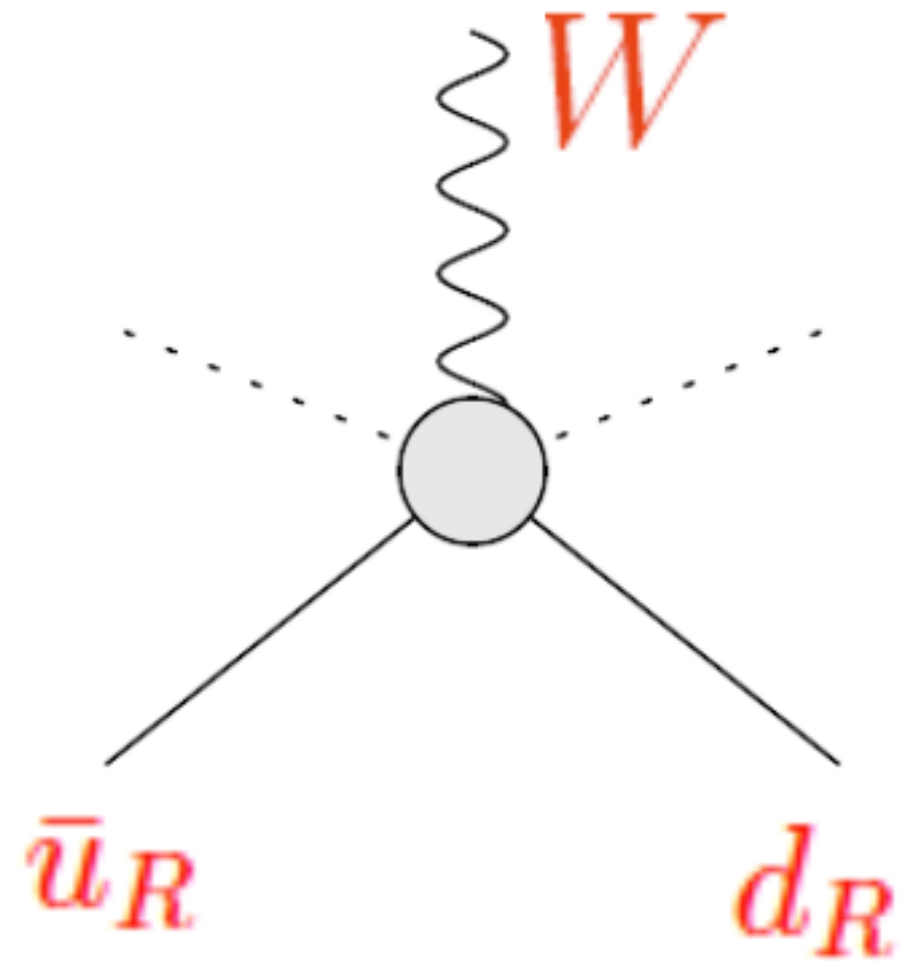
- Vector-Like Quarks  $\sim \mathcal{O}(\text{TeV})$

2212.06862, 2302.14097





# Falsifying $C_{Hud}$



$C_{Hud}$

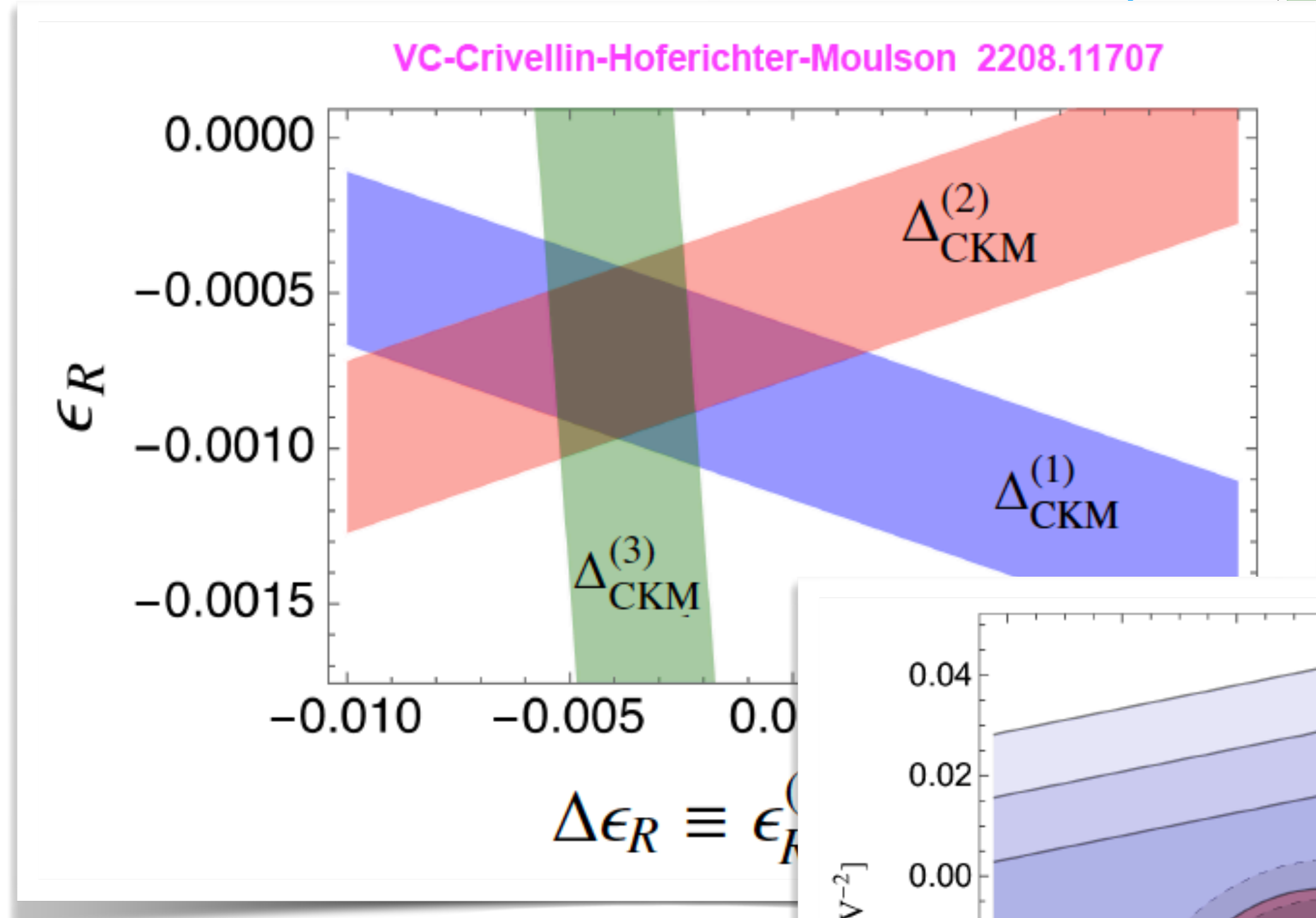
$$Q_{Hud} = i(\tilde{H}^\dagger D_\mu H)(\bar{u}_p \gamma^\mu d_r)$$

- Left-Right Symmetric Models

2107.10852

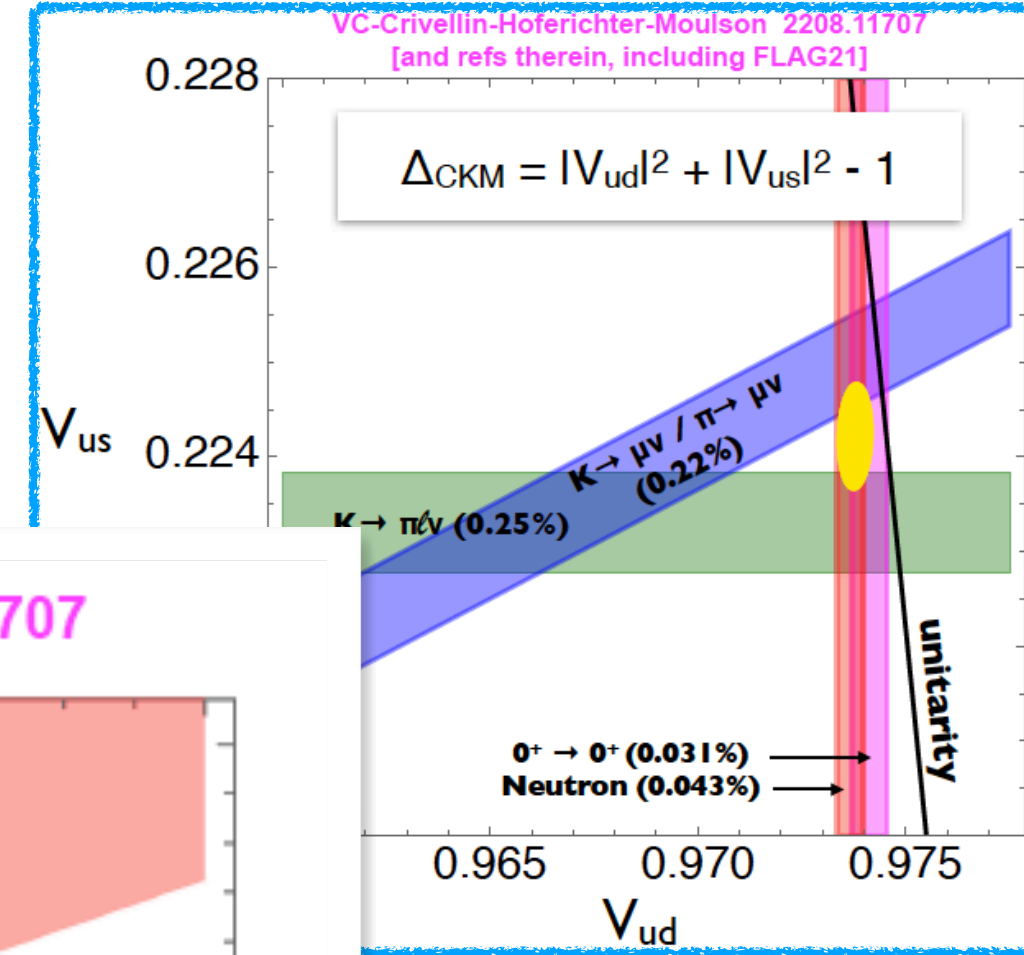
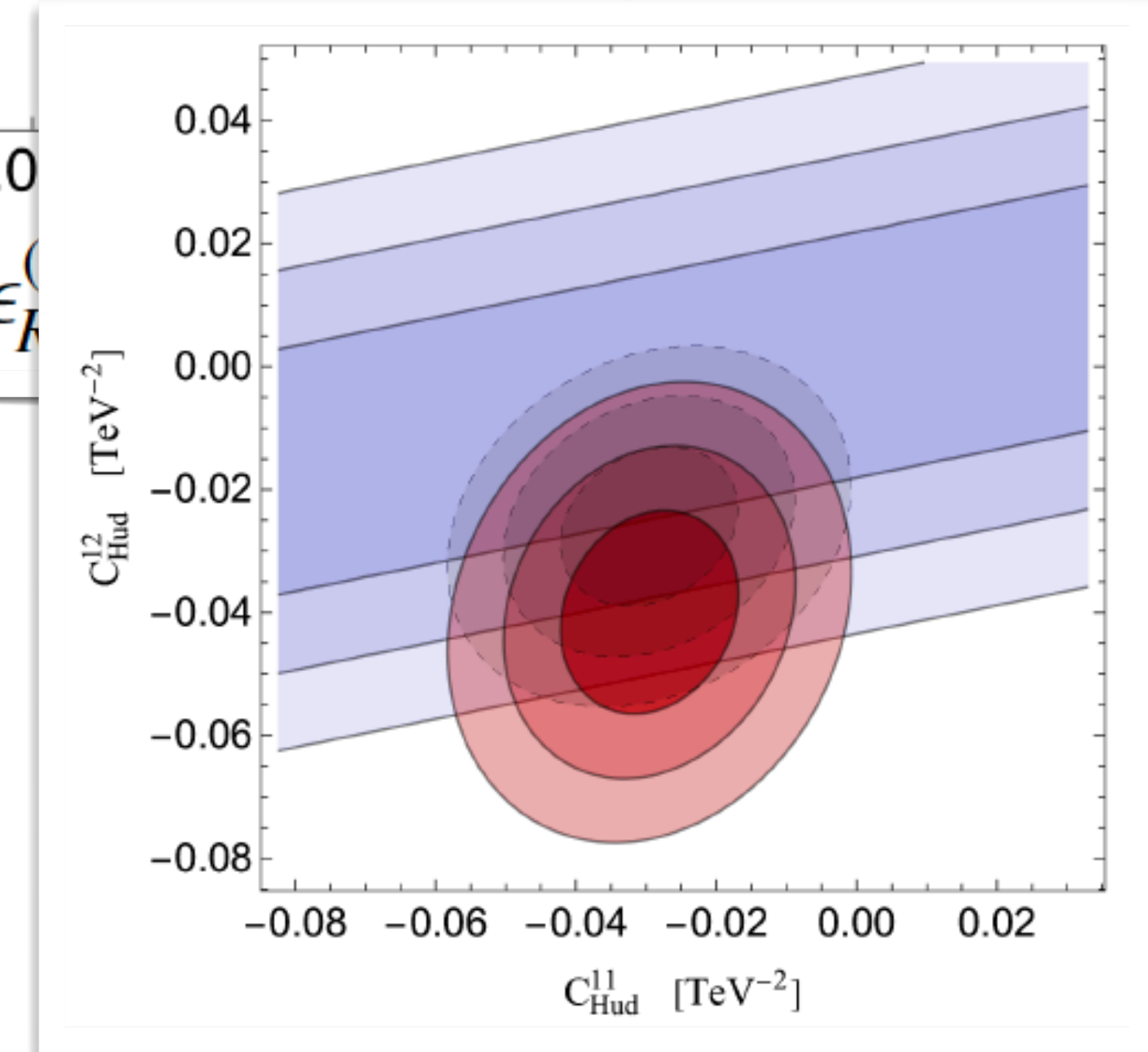
- Vector-Like Quarks  $\sim \mathcal{O}(\text{TeV})$

2212.06862, 2302.14097



$K \rightarrow \pi\pi$

$A_2$  from RBC/UKQCD

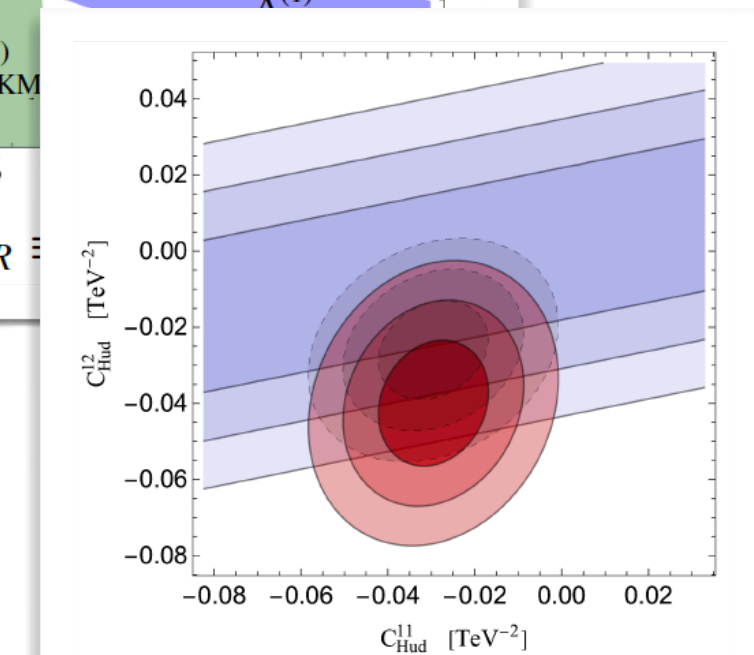
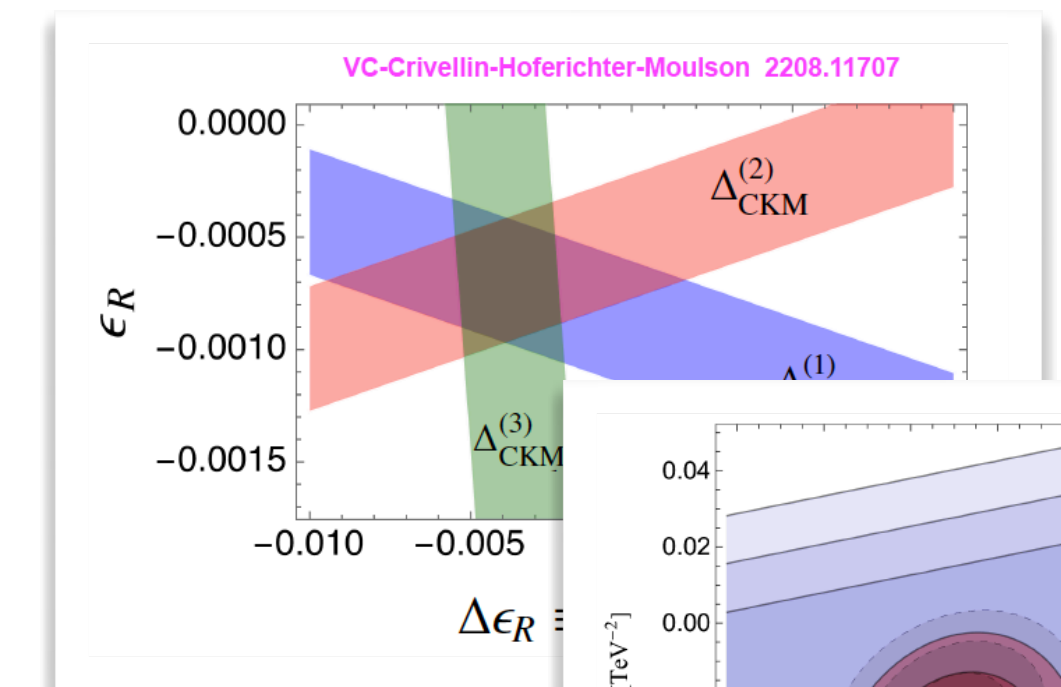
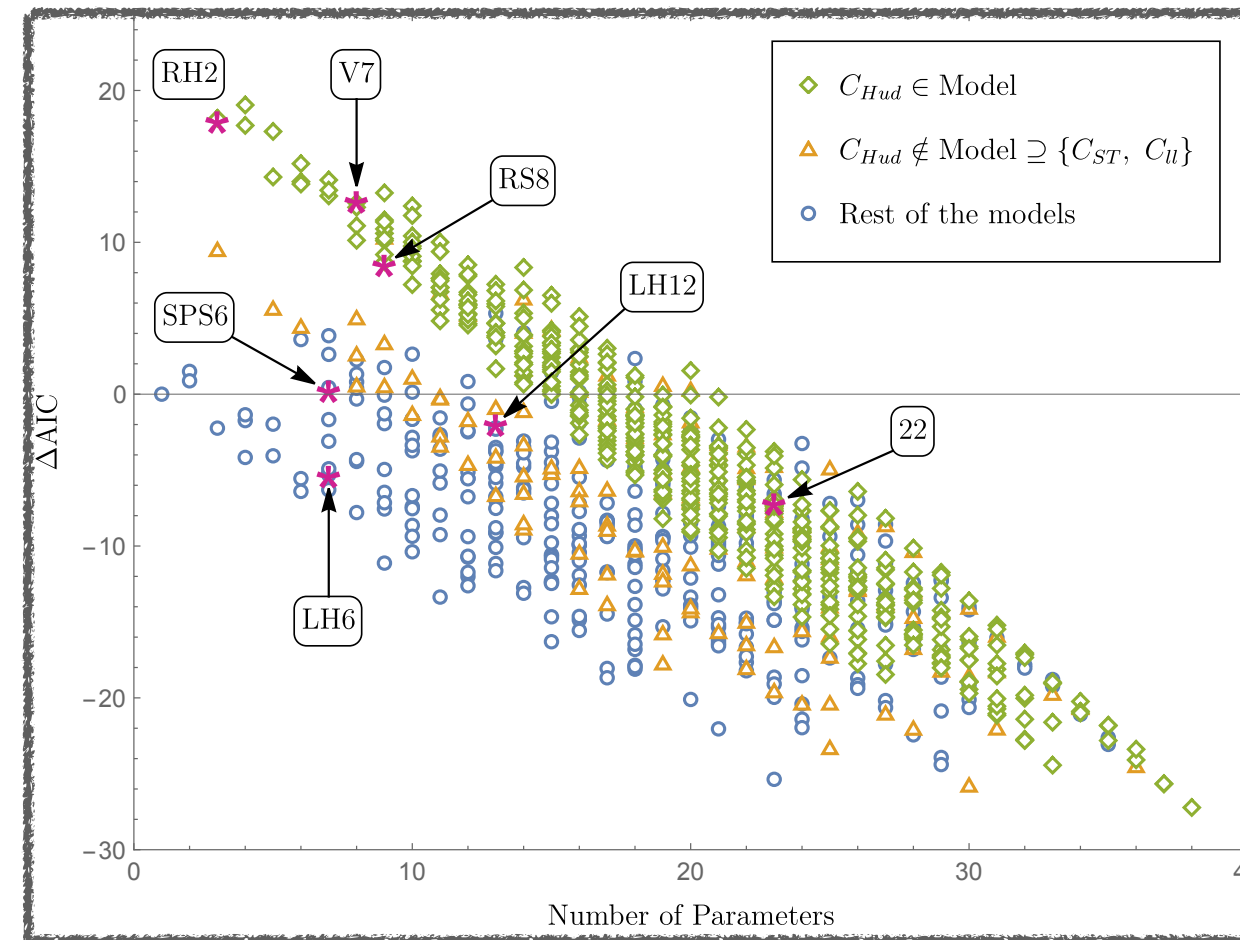
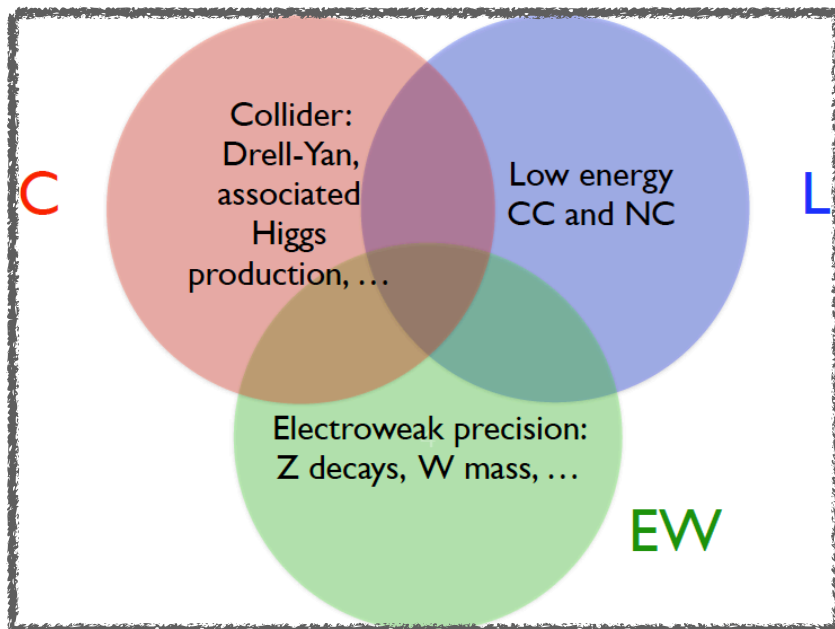




# Summary: the CLEW framework



Category	Operators	Description	# of Ops.
I.	$C_{ST}$	Oblique corrections	1
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X.	$C_{lequ}^{(3)}$	Tensor 4-fermion	2





# Finale

## 💡 Did you know?

The "ball of thread" meaning of *clew* (from Middle English *clewe* and ultimately from Old English *cliewen*) has been with us since before the 12th century. In Greek mythology, [Ariadne](#) gave a ball of thread to [Theseus](#) so that he could use it to find his way out of her father's labyrinth. This, and similar tales, gave rise to the use of *clew* for anything that could guide a person through a difficult place. This use led, in turn, to the meaning "a piece of evidence that leads one toward the solution of a problem." Today, the variant spelling *clue*, which appeared in the 17th century, is the more common spelling for the "evidence" sense, but you'll find *clew* in some famous works of literature.

Merriam-Webster Dictionary Thesaurus clew

## Dictionary

### Definition

**noun**

verb

**clew** 1 of 2 **noun**

'klü

1 : a ball of thread, yarn, or cord

