

Quirks
2024



CP-ODD OBSERVABLES IN $B \rightarrow P\ell^-\ell^+$

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INTRODUCTION

Flavor in the SM

$$\mathcal{L}_{\text{SM}} = \underbrace{|D_\mu H|^2 + \mu^2 |H|^2 - \lambda |H|^4 + \sum_f \bar{f} i \not{D} f - \frac{1}{4} \sum_X \text{tr}(X_{\mu\nu} X^{\mu\nu})}_{\text{flavor blind/symmetric}} + \underbrace{\mathcal{L}_{\text{Yuk}}}_{\text{flavor}}$$

global

$$U(3)_q \times U(3)_u \times U(3)_d \times U(3)_l \times U(3)_e$$

Higgs Yukawa couplings distinguish generations.

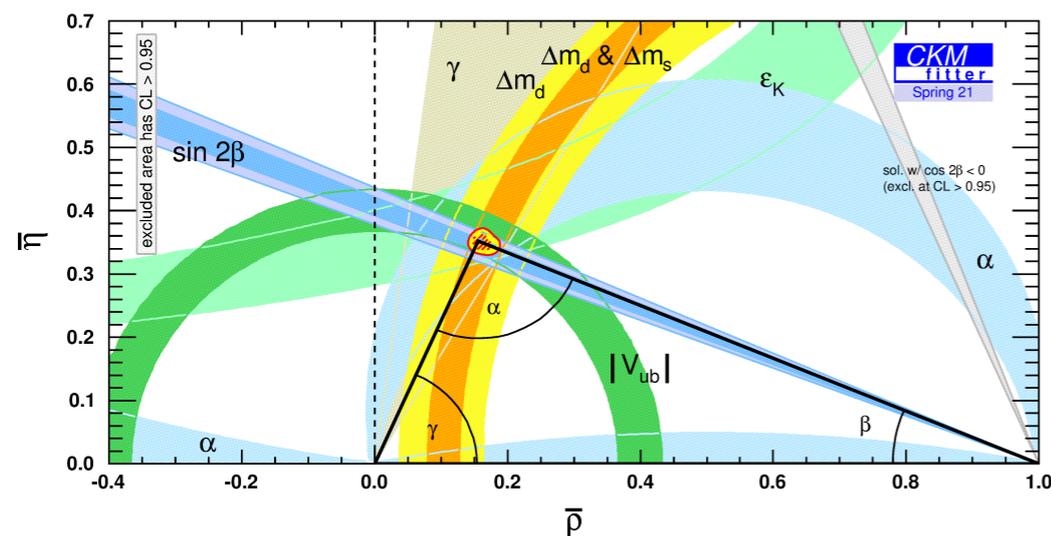


$$U(1)_B \times U(1)_{L_e} \times U(1)_{L_\mu} \times U(1)_{L_\tau}$$

- ▶ 13 parameters of the SM Yukawa sector: 9 masses, 3 mixing angles, 1 CP phase
- ▶ SM effective theory predicts $\sim 10^3$ additional flavour breaking parameters

SM(EFT) FLAVOUR

$$\mathcal{L}_{\text{SM}} + \frac{1}{\Lambda^2} \sum_i C_i Q_i$$



| CPV + 18 CP even parameters

$$\det(i[M_d, M_u]) = J(m_t - m_c)(m_t - m_u) \dots$$

$$J \approx 3 \times 10^{-5} \quad \text{Jarlskog '85}$$

	$(\bar{L}L)(\bar{L}L)$
Q_{ll}	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$ \dots
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$

At dim-6:

- 1149 CPV + 1350 CP even flavor couplings

Grzadkowski et al '10
Alonso et al '13

- 699 Jarlskog-like invariants

Bonnefoy et al. '21

RARE SEMILEPTONIC B-DECAYS

► Rare semileptonic B -meson decays are excellent probes of (B)SM flavour structure

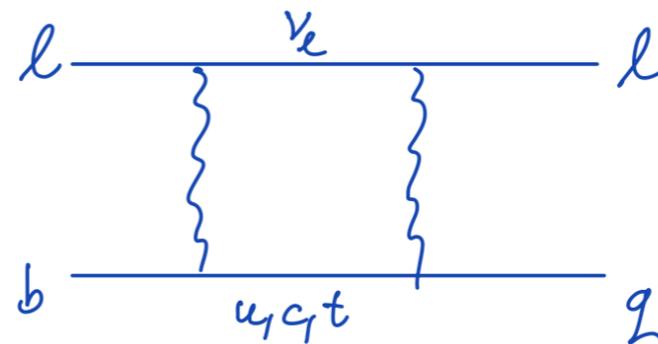
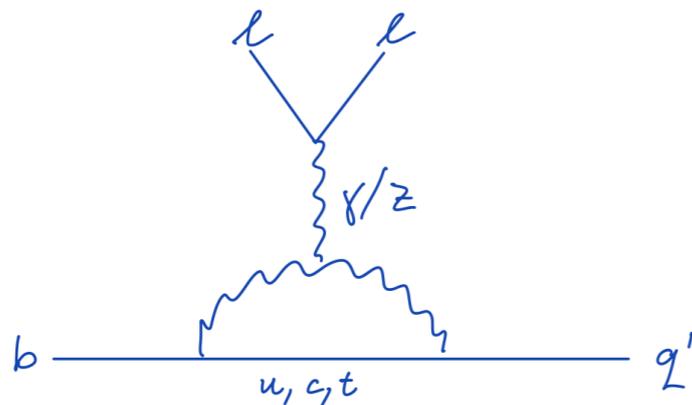
$$B \rightarrow K l^+ l^-$$

$$B \rightarrow \pi l^+ l^-$$

► At short distances SM amplitudes are severely suppressed

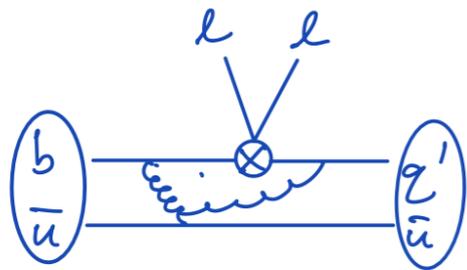
$$\mathcal{A}_{\text{SM}} \sim \frac{g^4 V_{tb} V_{ts}^*}{(4\pi)^2} \frac{m_t^2}{v^2}$$

► CKM suppression (GIM suppression broken by m_t)
 ► Loop suppression

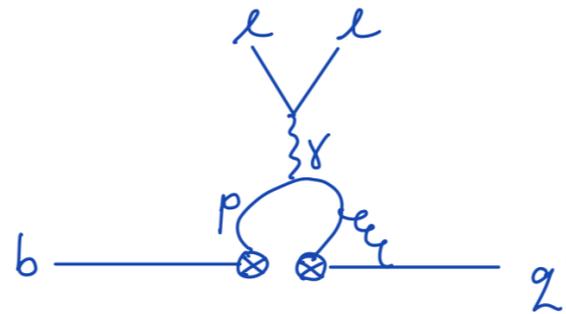


RARE SEMILEPTONIC B -DECAYS

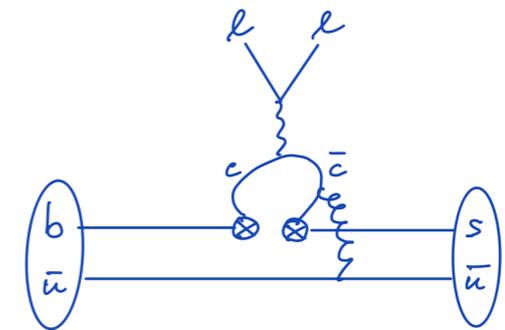
► Effects of QCD obstruct the view at scale m_B



local form factors -
single current insertion



non-local (non)-factorisable QCD effects



- Can we disentangle the effects of long-distance QCD from short distance SM and potential NP contributions ?
- Notoriously difficult to calculate nonlocal effects of light quark propagation ($c\bar{c}$, $u\bar{u}$)
 - Light-cone sum rules
 - Experimental fits to a series of known intermediate resonances (à la Breit-Wigner) or via dispersive approach

OUTLINE

- ▶ CP-even and CP-odd parts of $B \rightarrow P\ell^+\ell^-$ spectra
- ▶ Use experimental data to:
 - * extract non-local amplitudes from data (assuming SM)
 - * relation between CP-odd $B^- \rightarrow \pi^-\ell^+\ell^-$ and $B^- \rightarrow K^-\ell^+\ell^-$

- ▶ Direct CPV in $B \rightarrow K\ell^+\ell^-$, enhanced by narrow charmonium resonance (J/ψ)

CP-EVEN/ODD RATES

► $b \rightarrow q'\ell\ell$ with $q' = d, s$

$$\mathcal{L}_{\text{eff}}^{(q')} = \frac{4G_F\lambda_t^{(q')}}{\sqrt{2}} \sum_{i=3}^{10} c_i \mathcal{O}_i^{(q')} + \frac{4G_F}{\sqrt{2}} \sum_{p=u,c} \lambda_p^{(q')} \sum_{i=1,2} c_i \mathcal{O}_{i,p}^{(q')}$$

$$\lambda_p^{(q')} = V_{pb}V_{pq'}^*$$

semileptonic operators

hadronic operators

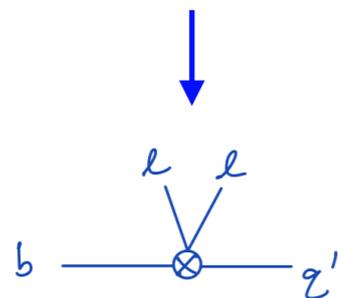
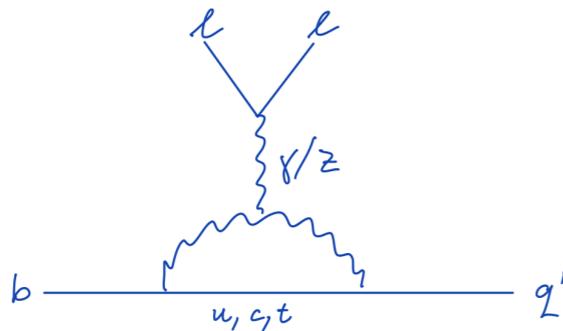
$$\mathcal{O}_7^{(q')} = \frac{em_b}{(4\pi)^2} \bar{q}'_L \sigma_{\mu\nu} b_R F^{\mu\nu}$$

$$\mathcal{O}_9^{(q')} = \frac{\alpha}{4\pi} (\bar{q}'_L \gamma_\mu b_L) (\bar{\ell} \gamma^\mu \ell)$$

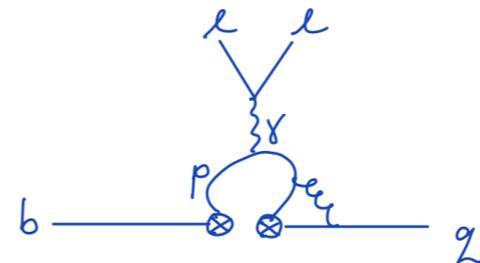
$$\mathcal{O}_{10}^{(q')} = \frac{\alpha}{4\pi} (\bar{q}'_L \gamma_\mu b_L) (\bar{\ell} \gamma^\mu \gamma^5 \ell)$$

$$\mathcal{O}_{1,p}^{(q')} = (\bar{q}'_L \alpha \gamma^\mu p_{L\beta}) (\bar{p}_{L\beta} \gamma_\mu b_{L\alpha})$$

$$\mathcal{O}_{2,p}^{(q')} = (\bar{q}'_L \gamma^\mu p_L) (\bar{p}_L \gamma_\mu b_L)$$



local, short distance



non-local

(NON)LOCAL AMPLITUDE

► Differential rate for $B^- \rightarrow P^- \ell \ell$

$$\frac{d\Gamma_P}{dq^2} = \mathcal{N}_P \left(f_+^{(P)} \right)^2 \left(|C_{10}|^2 + \left| C_9^{\text{eff}} + \tilde{f}_T^{(P)} C_7 \right|^2 \right)$$

► All long-distance effects can be absorbed in $C_9^{\text{eff}}(q^2)$

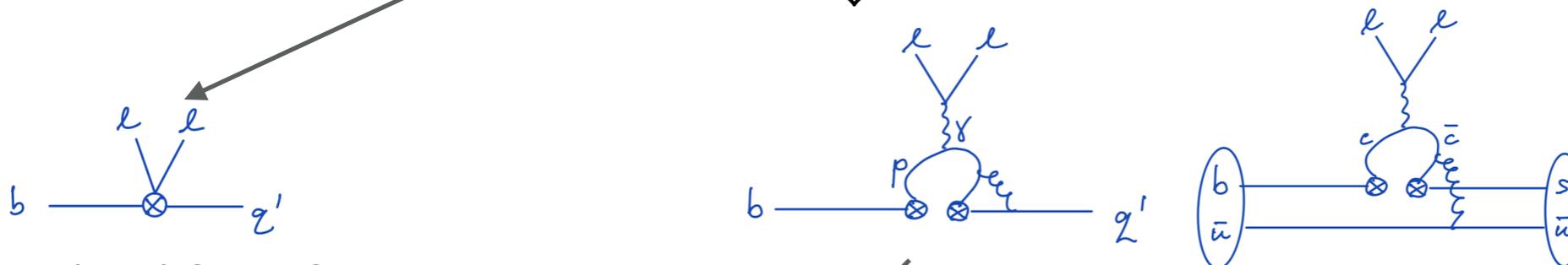
$f_+^{(P)}(q^2)$ = vector form factor

$$\mathcal{N}_P = \frac{G_F^2 \alpha^2 |\lambda_t^{(q')}|^2}{3 \cdot 512 \pi^5 m_B^3} \lambda_P^{3/2}(q^2)$$

$$\tilde{f}_T^{(P)} \equiv \frac{2f_T^{(P)}(q^2)(m_b + m_{q'})}{f_+^{(P)}(q^2)(m_B + m_P)}$$

$$C_9^{\text{eff}}(q^2) = C_9 - \underbrace{\tilde{\lambda}_c^{(q')} Y_{c\bar{c}}(q^2) + \tilde{\lambda}_u^{(q')} Y_{u\bar{u}}(q^2)}$$

$$\tilde{\lambda}_p^{(q')} = \lambda_p^{(q')} / \lambda_t^{(q')}$$



► local form factors

Gubernari et al., 2305.06301

$$f_+^{(P)} Y_{p\bar{p}}(q^2) \equiv \frac{(8\pi)^2 Q_p}{\lambda_P(q^2)} \int d^4x e^{iq \cdot x} \langle P(k) | \mathcal{T} \left\{ \bar{p} \not{k} p(x), \sum_{i=1,2} C_i \mathcal{O}_{i,p}^{(q')}(0) \right\} | \bar{B}(q+k) \rangle$$

Khodjamirian, Mannel, Wang, 1211.0234

- $m_\ell = 0$
- real local coefficients C_7, C_9, C_{10}
- with SM values $C_7^{\text{SM}} = -0.292$, $C_9^{\text{SM}} = 4.07$, $C_{10}^{\text{SM}} = -4.31$
- complex valued $Y_{q\bar{q}}$, independent in each bin

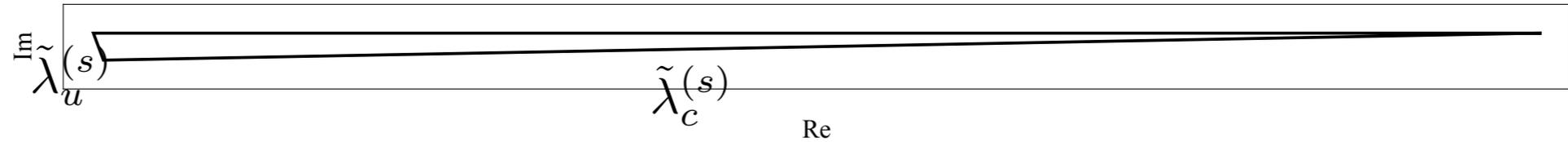
Assumptions

$B^- \rightarrow K^- \ell \ell$

► In CP-even rate quirky CKM hierarchy selects the charm quark non-local contribution

$$\tilde{\lambda}_c^{(s)} = -1 + \lambda^2(\rho - i\eta)$$

$$\tilde{\lambda}_u^{(s)} = -\lambda^2(\rho - i\eta)$$



$$\frac{(d\Gamma_K + d\bar{\Gamma}_K)/2}{dq^2} = \mathcal{N}_K \left(f_+^{(K)}\right)^2 \left[c_{10}^2 + \left(c_9 + \tilde{f}_T^{(K)} c_7\right)^2 + 2\left(c_9 + \tilde{f}_T^{(K)} c_7\right) \text{Re} Y_{c\bar{c}} + |Y_{c\bar{c}}|^2 \right]$$

< 2 % effect

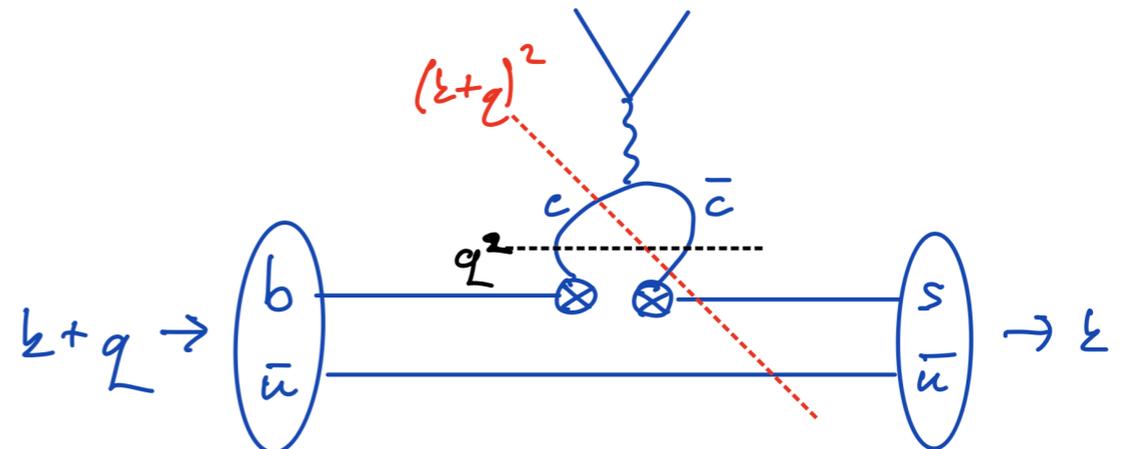
Kamenik, NK, Novoa-Brunet, 2403.13056

► CP-odd rate proportional to $\text{Im}\tilde{\lambda}_c^{(s)} = -\text{Im}\tilde{\lambda}_u^{(s)}$, both $u\bar{u}$ and $c\bar{c}$ contribute

$$\frac{d\Gamma_K - d\bar{\Gamma}_K}{dq^2} = 4\mathcal{N}_K \left(f_+^{(K)}\right)^2 \eta \lambda^2 \left[\left(c_9 + \tilde{f}_T^{(K)} c_7\right) \text{Im}(Y_{u\bar{u}} - Y_{c\bar{c}}) - \text{Im}(Y_{c\bar{c}} Y_{u\bar{u}}^*) \right]$$

< 30 % effect

► Analytic structure implies complex $Y_{q\bar{q}}$
- due to cuts in q^2 and $(k+q)^2$

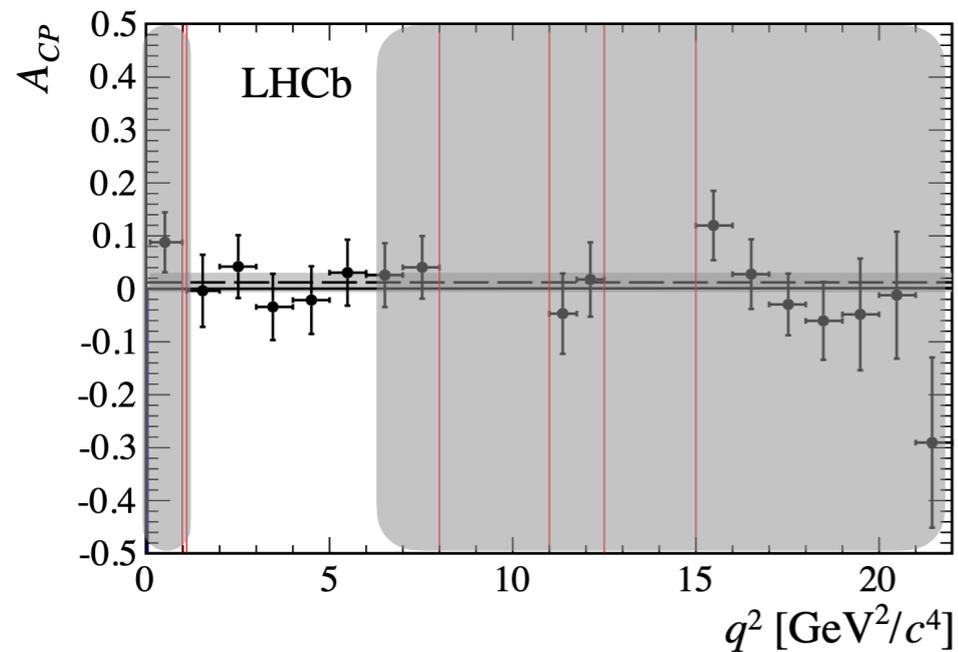


Khodjamirian, Mannel, Wang, 1211.0234

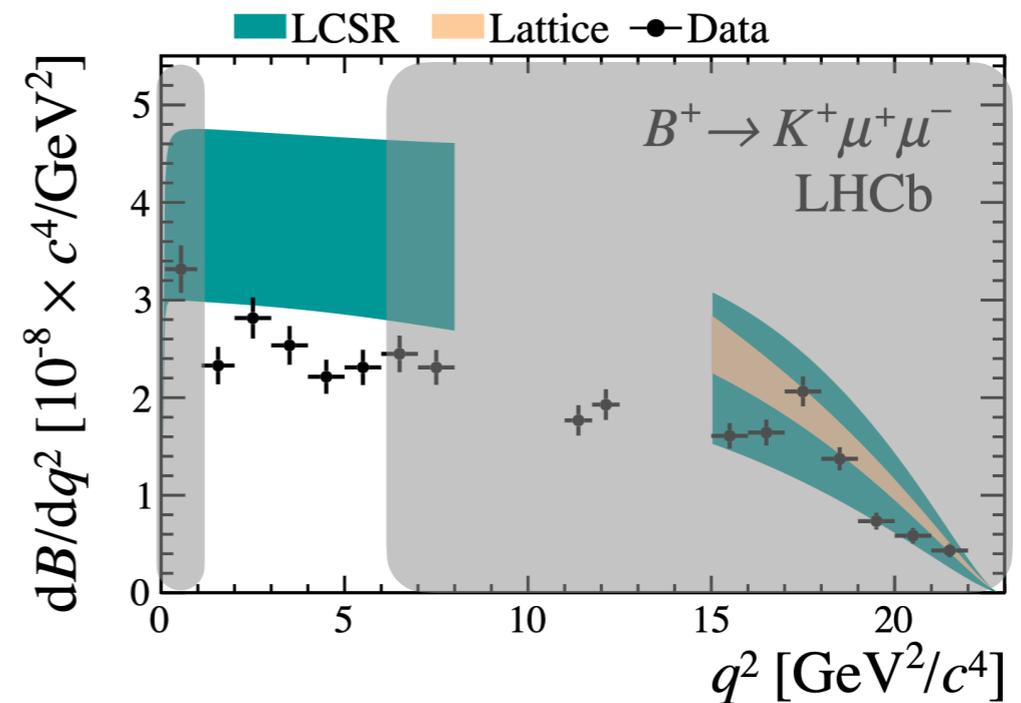
Asatrian, Greub, Virto, 1912.09099

DATA DRIVEN APPROACH

- ▶ Consider binned CP-averaged rates and CP-asymmetries



LHCb, 1408.0978



LHCb, 1403.8044

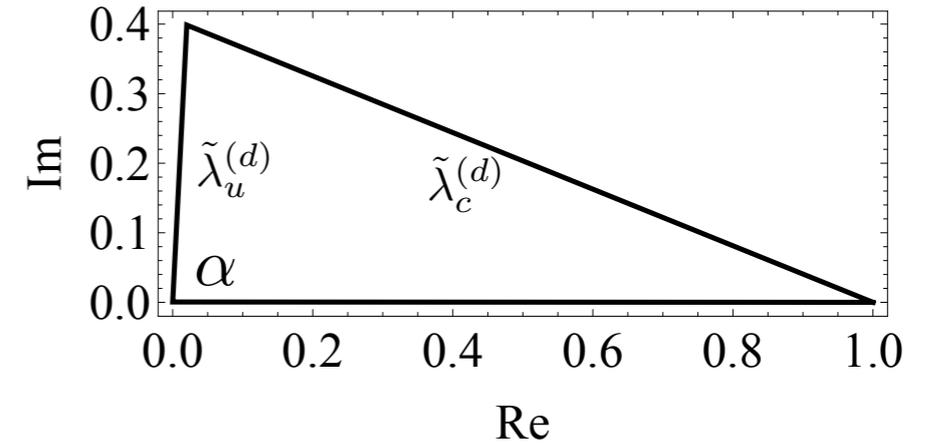
- ▶ bins $[1.1, 2] - [5, 6] \text{ GeV}^2$, between ρ/ω and $c\bar{c}$ peaks
- ▶ compare the rates and A_{CP} in each bin
- ▶ set $C_i = C_i^{\text{SM}}$
- ▶ extract nonlocal functions $\text{Re}Y_{c\bar{c}}$ and $\text{Im}(Y_{c\bar{c}} - Y_{u\bar{u}})$ in each bin

$B^- \rightarrow \pi^- \ell \ell$

- ▶ Similar sizes of $\tilde{\lambda}_c^{(d)}$ and $\tilde{\lambda}_u^{(d)}$, large CPV phase
- ▶ $\tilde{\lambda}_u^{(d)}$ almost imaginary
- ▶ small expansion parameter $\rho(1 - \rho) - \eta^2 = -0.022$

$$\tilde{\lambda}_c^{(d)} = \frac{\rho - 1 + i\eta}{(1 - \rho)^2 + \eta^2} \approx 0.4i - 1$$

$$\tilde{\lambda}_u^{(d)} = \frac{\rho(1 - \rho) - \eta^2 - i\eta}{(1 - \rho)^2 + \eta^2} \approx -0.4i$$



< 2 % effect

$$\frac{(d\Gamma_\pi + d\bar{\Gamma}_\pi)/2}{dq^2} = \mathcal{N}_\pi \left(f_+^{(\pi)} \right)^2 \left[\mathcal{C}_{10}^2 + (\mathcal{C}_9 + \tilde{f}_T^{(\pi)} \mathcal{C}_7)^2 + 2(\mathcal{C}_9 + \tilde{f}_T^{(\pi)} \mathcal{C}_7) \text{Re} Y_{c\bar{c}} + |Y_{c\bar{c}}|^2 + (\text{Im} \tilde{\lambda}_u^{(d)})^2 |Y_{u\bar{u}} - Y_{c\bar{c}}|^2 \right]$$

Hambrock, Khodjamirian, Rusov, 1506.07760

- ▶ CP-odd rate is large

$$\frac{d\Gamma_\pi - d\bar{\Gamma}_\pi}{dq^2} = 4\mathcal{N}_\pi \left(f_+^{(\pi)} \right)^2 \frac{(-\eta)}{(1 - \rho)^2 + \eta^2} \left[(\mathcal{C}_9 + \tilde{f}_T^{(\pi)} \mathcal{C}_7) \text{Im}(Y_{u\bar{u}} - Y_{c\bar{c}}) - \text{Im}(Y_{c\bar{c}} Y_{u\bar{u}}^*) \right] < 30 \% \text{ effect}$$

- ▶ Note: $Y_{q\bar{q}} = Y_{q\bar{q}}^{(P)}$ and $Y_{q\bar{q}}^{(K)} \neq Y_{q\bar{q}}^{(\pi)}$

No binned data for $B^- \rightarrow \pi^- \ell \ell$ at this time.

$B^- \rightarrow K^- \ell \ell$ AND $B^- \rightarrow \pi^- \ell \ell$ CPV RATES

► Consider the ratio of CP-odd rates

$$R_{K/\pi}^{\text{CP}} \equiv - \frac{(d\Gamma_K - d\bar{\Gamma}_K)/dq^2}{(d\Gamma_\pi - d\bar{\Gamma}_\pi)/dq^2}$$

Kamenik, NK, Novoa-Brunet, 2403.13056

Sensitive to U -spin breaking:

$$R_{K/\pi}^{\text{CP}}|_{\text{SM}} = \underbrace{\left(\frac{\lambda_K}{\lambda_\pi}\right)^{3/2} \left(\frac{f_+^{(K)}}{f_+^{(\pi)}}\right)^2}_{\text{known } U\text{-spin breaking}} \left[1 - \underbrace{\frac{c_7^{\text{SM}}(\tilde{f}_T^{(\pi)} - \tilde{f}_T^{(K)})}{c_9^{\text{SM}} + c_7^{\text{SM}} \tilde{f}_T^{(K)}}}_{\text{unknown } U\text{-spin breaking}} - \epsilon_{uc} + \mathcal{O}(\Delta_U^2) \right]$$

↑
↑
↑
 subleading

► Unknown U -spin breaking parameter: $\epsilon_{uc} < 0.3$

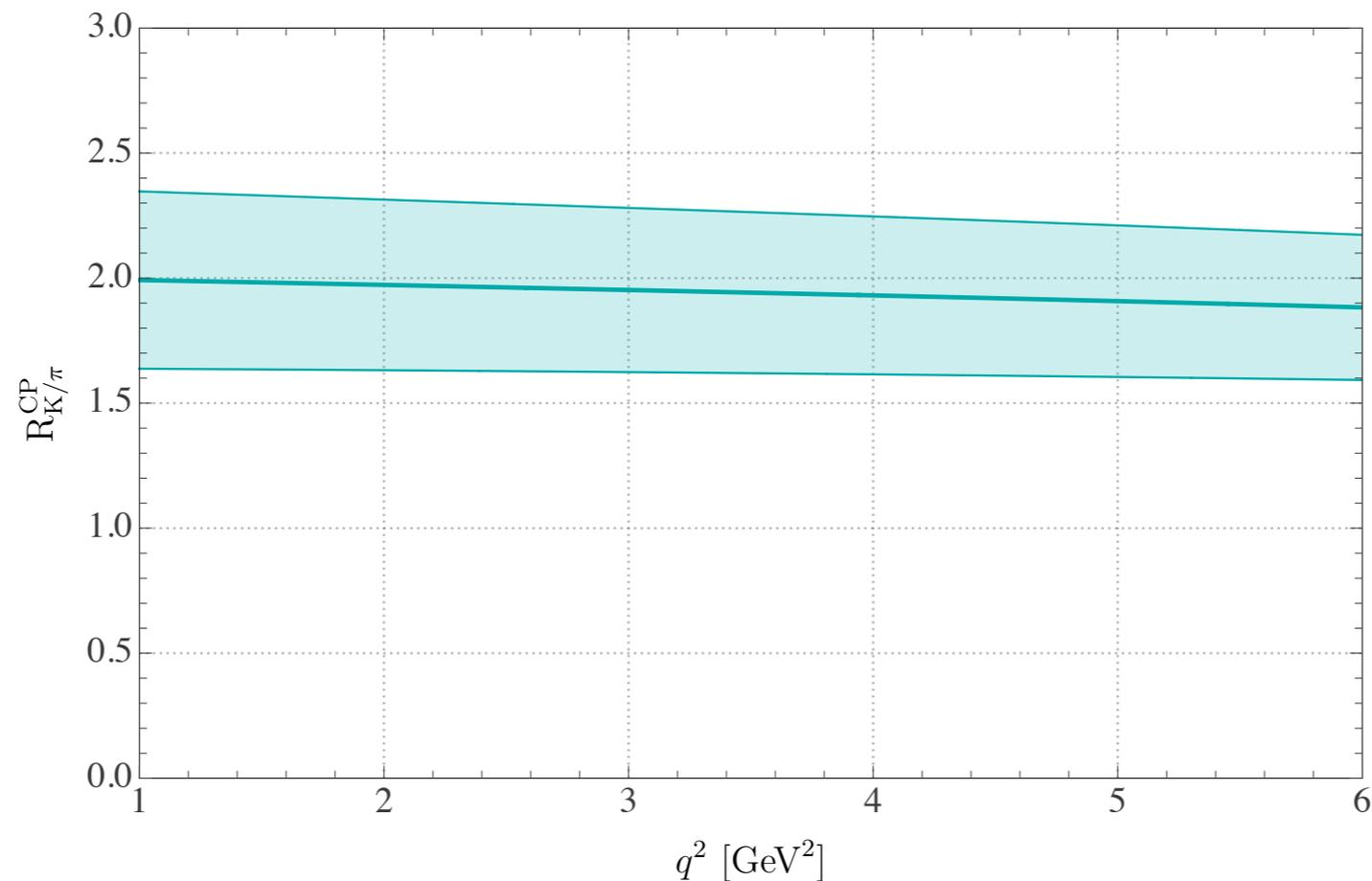
$$\text{Im} \left(Y_{u\bar{u}}^{(\pi)} - Y_{c\bar{c}}^{(\pi)} \right) = (1 + \epsilon_{uc}) \text{Im} \left(Y_{u\bar{u}}^{(K)} - Y_{c\bar{c}}^{(K)} \right)$$

► Experimental check of U -spin:

$$\left| \frac{Y_{c\bar{c}}^{(K)}}{Y_{c\bar{c}}^{(\pi)}} \right|_{q^2=m_{J/\psi}^2} = \left| \frac{\lambda_c^{(d)}}{\lambda_c^{(s)}} \right| \sqrt{\frac{|\mathbf{k}_\pi| \Gamma(B^+ \rightarrow J/\psi K^+)}{|\mathbf{k}_K| \Gamma(B^+ \rightarrow J/\psi \pi^+)}} = 1.2$$

U-SPIN RATIO

$$R_{K/\pi}^{\text{CP}}|_{\text{SM}} = \left(\frac{\lambda_K}{\lambda_\pi}\right)^{3/2} \left(\frac{f_+^{(K)}}{f_+^{(\pi)}}\right)^2 \left[1 - \frac{\mathcal{C}_7^{\text{SM}}(\tilde{f}_T^{(\pi)} - \tilde{f}_T^{(K)})}{\mathcal{C}_9^{\text{SM}} + \mathcal{C}_7^{\text{SM}}\tilde{f}_T^{(K)}} - \cancel{\epsilon_{uc}}\right]$$

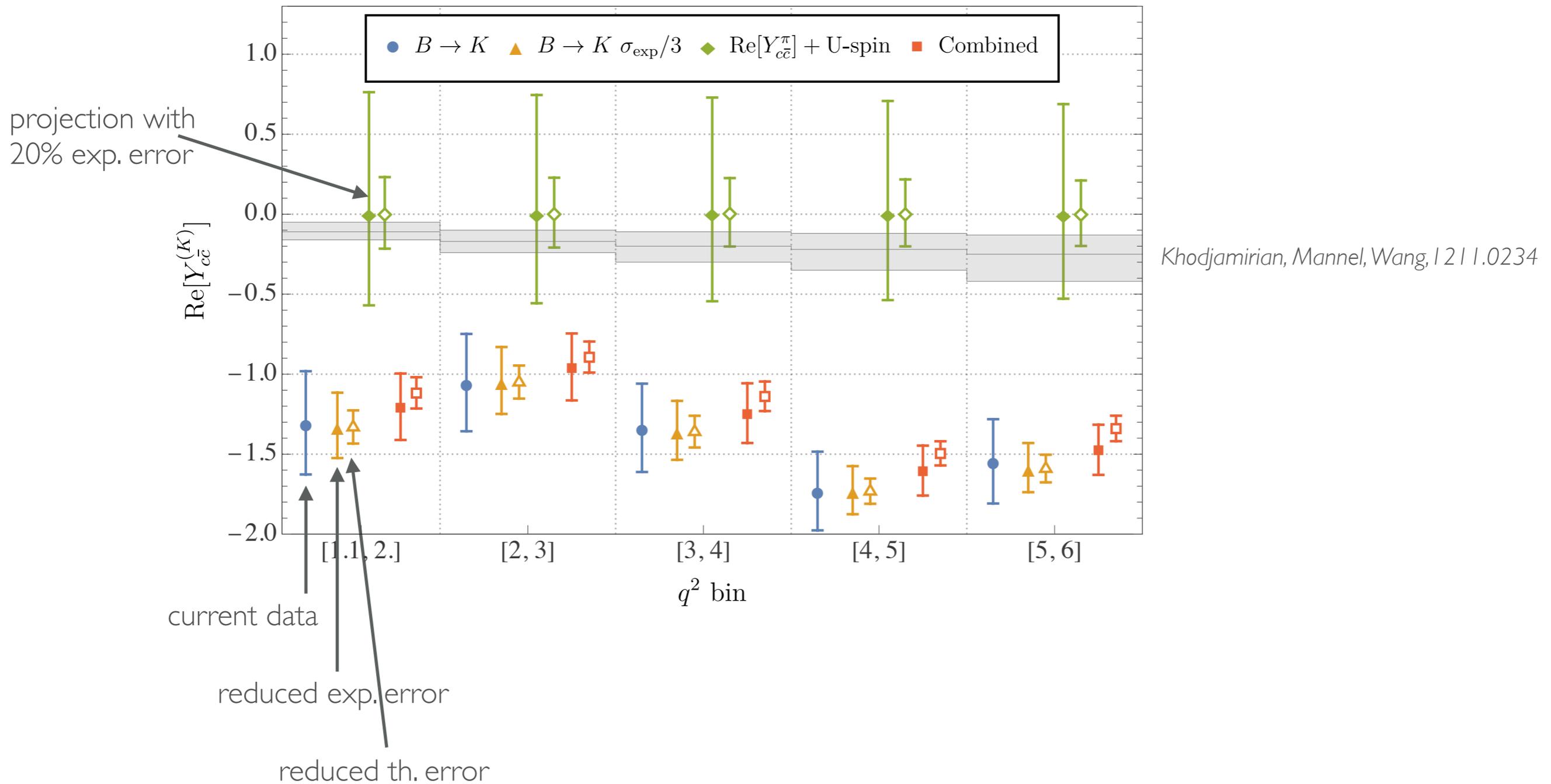


Independent of $Y_{q\bar{q}}$ values!

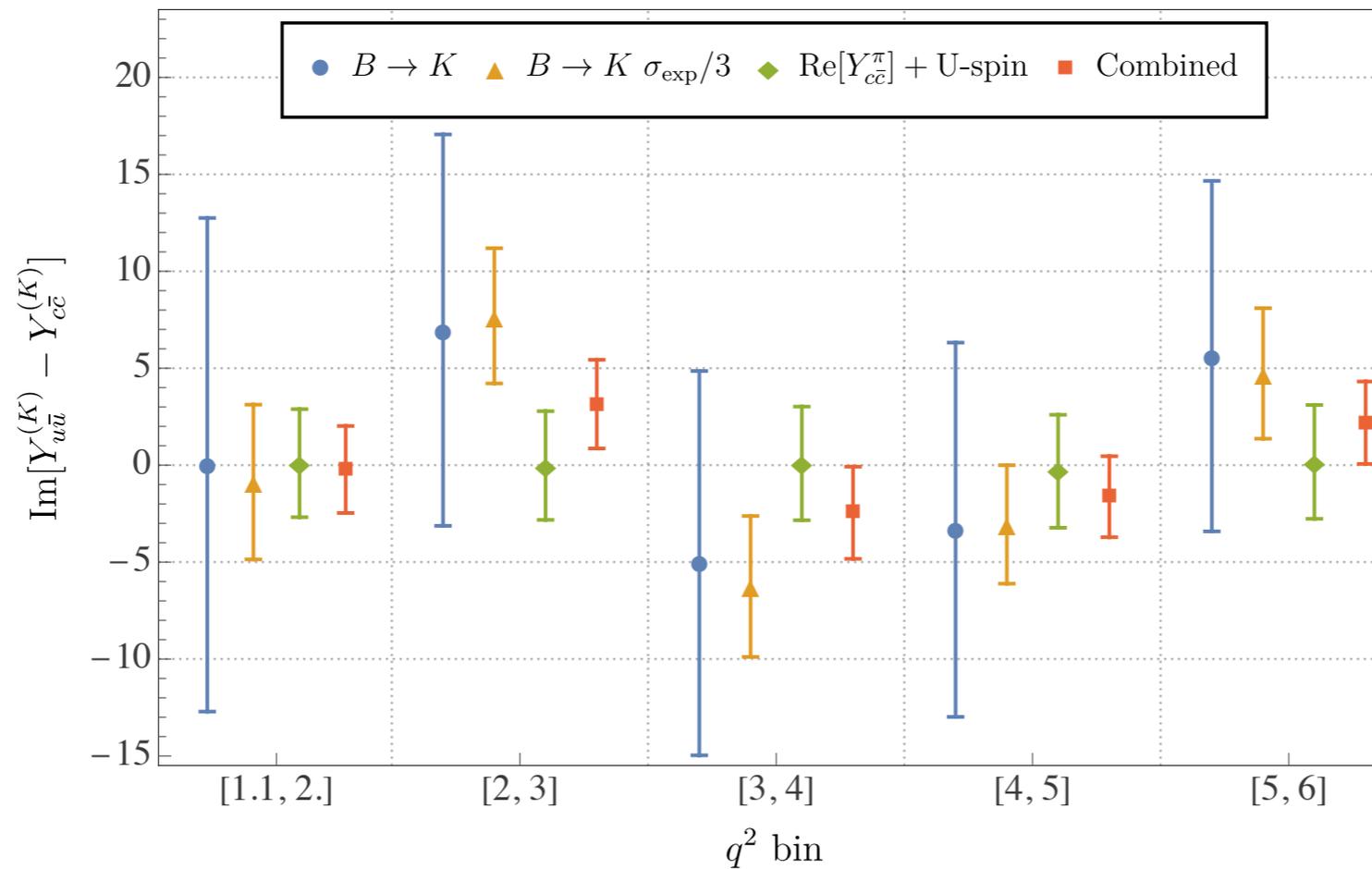
Accounts for known U -spin breaking

Remains valid in the CP-conserving U -spin symmetric New Physics case ($\delta\mathcal{C}_i^{(s)} = \delta\mathcal{C}_i^{(d)}$)

REAL PARTS OF NONLOCAL AMPS



IM. PARTS OF NONLOCAL AMPS



Caveat: omitted quadratic terms in $Y_{q\bar{q}}$

U-SPIN RATIO AND NEW PHYSICS

- ▶ CP-conserving NP in $B \rightarrow K\ell\ell$: $C_{7,9}^{(s)} = C_{7,9}^{\text{SM}} + \delta C_{7,9}^{(s)}$

$$R_{K/\pi}^{\text{CP}}|_{\text{NP}} = \left(\frac{\lambda_K}{\lambda_\pi}\right)^{3/2} \left(\frac{f_+^{(K)}}{f_+^{(\pi)}}\right)^2 \left[1 - \frac{C_7^{\text{SM}}(\tilde{f}_T^{(\pi)} - \tilde{f}_T^{(K)})}{C_9^{\text{SM}} + C_7^{\text{SM}}\tilde{f}_T^{(K)}} - \epsilon_{uc} \right] \times \left(1 + \frac{\delta C_9^{(s)} + \delta C_7^{(s)}\tilde{f}_T^{(K)}}{C_9^{\text{SM}} + C_7^{\text{SM}}\tilde{f}_T^{(K)}} \right)$$

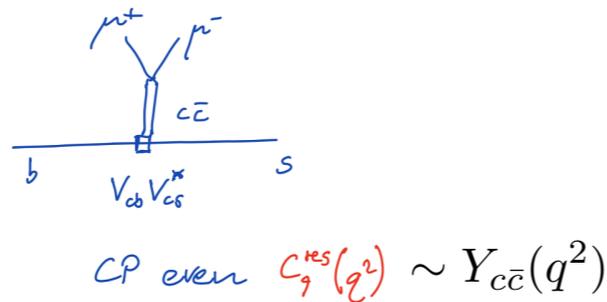
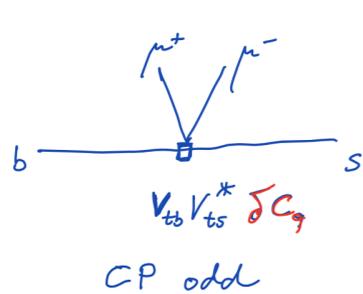
- ▶ Ratio probes CP-conserving contribution in orthogonal direction (relative to the CP-averaged rate)

- ▶ CP-violating NP in $B \rightarrow K\ell\ell$: $C_{7,9}^{(s)} = C_{7,9}^{\text{SM}} + i\delta C_{7,9}^{(s)}$

$$\frac{(d\Gamma_K - d\bar{\Gamma}_K)_{\text{ImNP}}}{(d\Gamma_K - d\bar{\Gamma}_K)_{\text{SM}}} = -\frac{\text{Im}\delta C_9^{(s)}}{\eta\lambda^2} \times \frac{\text{Im}Y_{c\bar{c}}^{(K)}}{(C_9^{\text{SM}} + \tilde{f}_T^{(K)}C_7^{\text{SM}})(\text{Im}Y_{c\bar{c}}^{(K)} - \text{Im}Y_{u\bar{u}}^{(K)}) + \text{Im}(Y_{c\bar{c}}^{(K)}Y_{u\bar{u}}^{(K)*})}$$

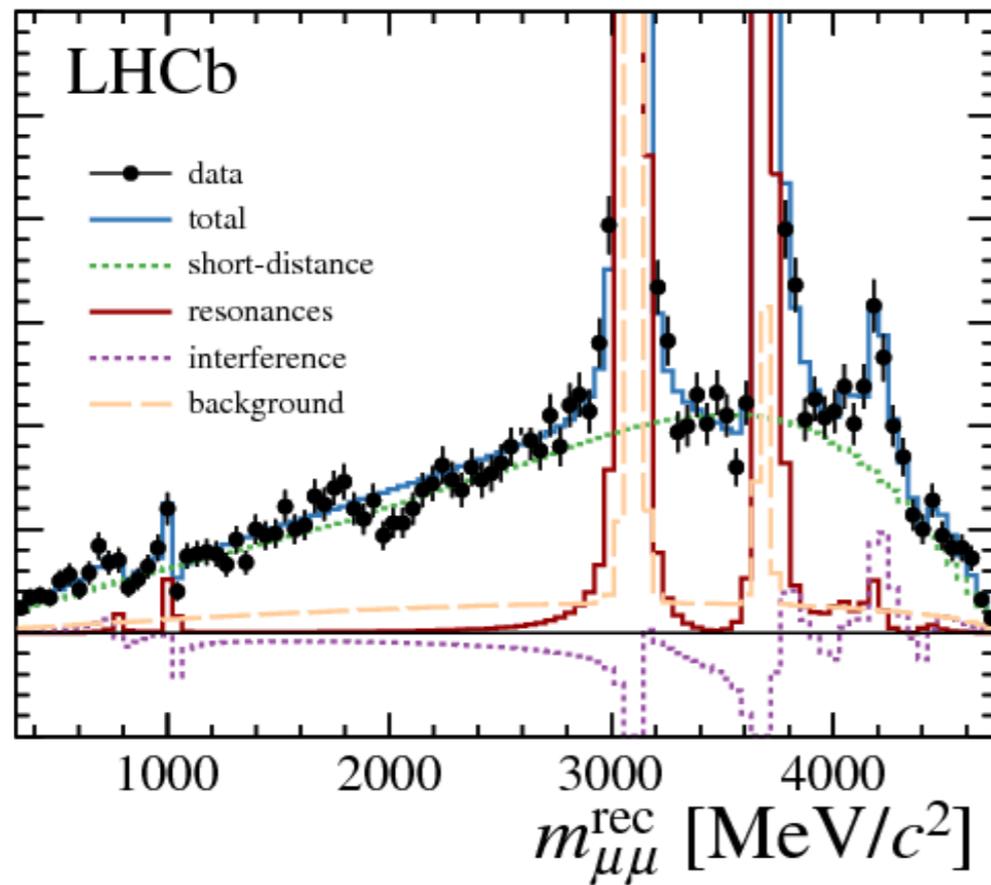
- ▶ CP-violating NP interferes with CP-even $c\bar{c}$ absorptive amplitude. Additional U -spin breaking parameter makes $R_{K/\pi}^{\text{CP}}$ less useful.

RESONANT STRONG PHASE



$$C_9^{\text{res}}(q^2) \approx \frac{m_j \Gamma_j \eta_j e^{i\delta_j}}{m_j^2 - q^2 - im_j \Gamma_j}$$

δ_j : extract from CP-averaged non-blinded spectrum



4-fold degeneracy of fit to the spectrum:

Branch 1: $\delta_{J/\psi} = -1.66$, $\delta_{\psi(2S)} = -1.93$,

Branch 2: $\delta_{J/\psi} = -1.50$, $\delta_{\psi(2S)} = 2.08$.

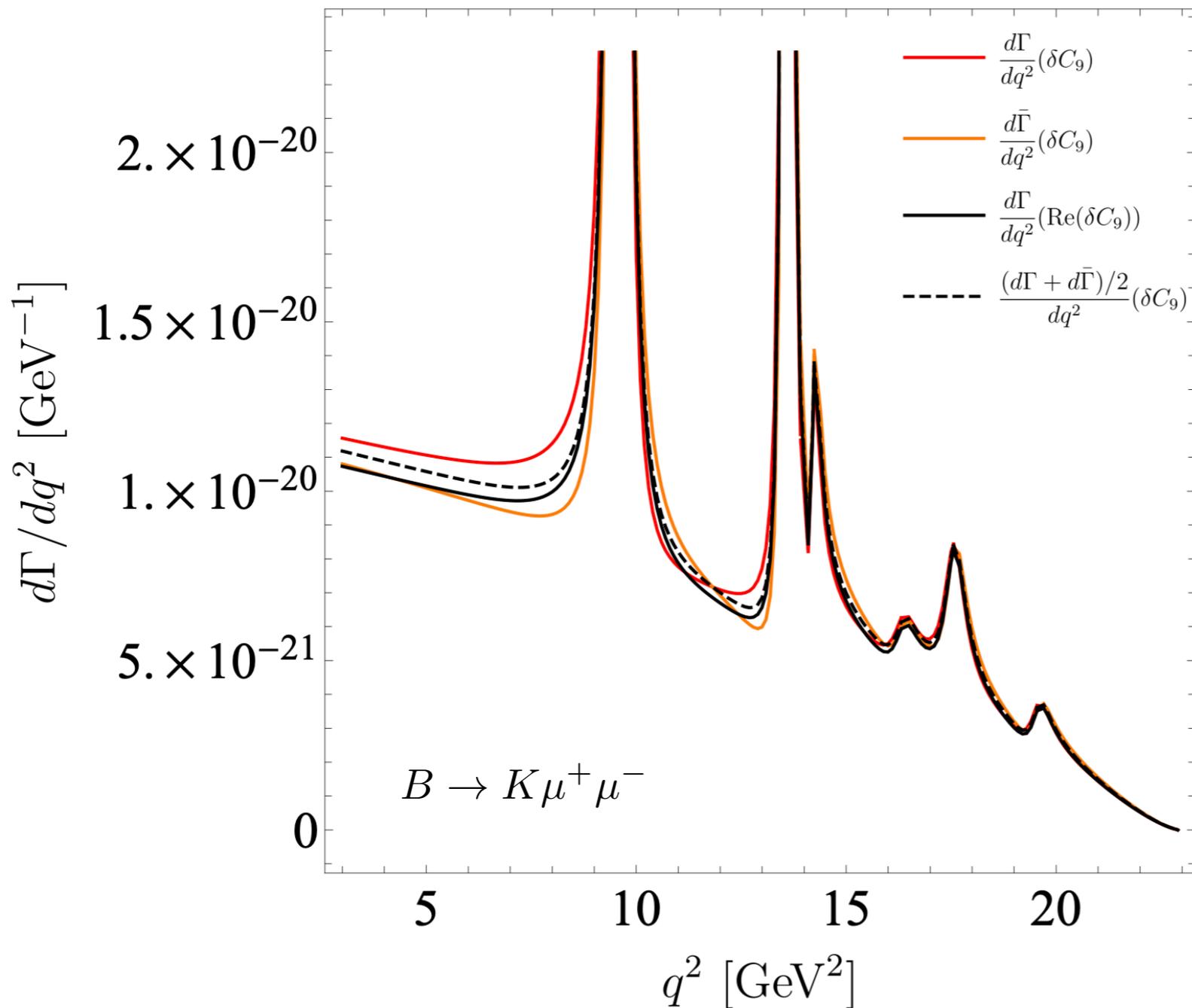
Branch 3,4 \sim Branch 1,2

LHCb '16

see also Blake, Egede, Owen, Petridis, Pomery '17

NO CP VS. CP-AVERAGE

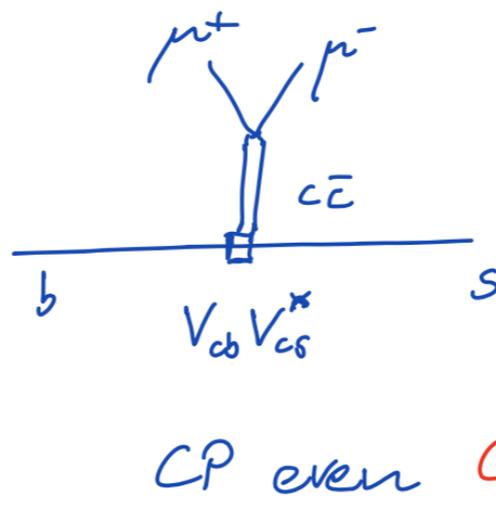
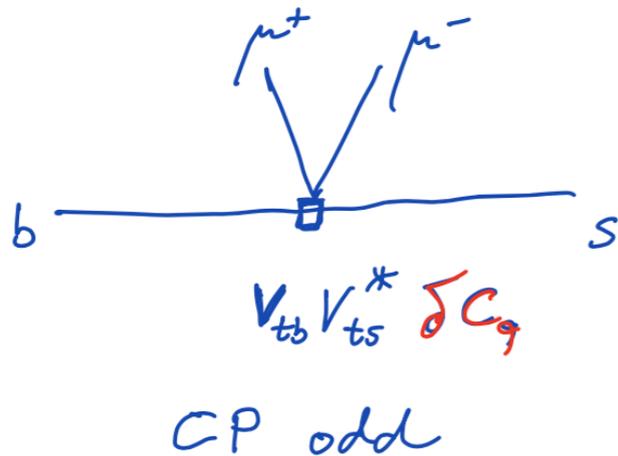
$$\delta C_9 = -\delta C_{10} = -0.48 - 0.7i$$



Resonant parameters taken from the LHCb fit to CP averaged rates.

CP-averaged fit is not sensitive to CPV phases

DIRECT ASYMMETRIES

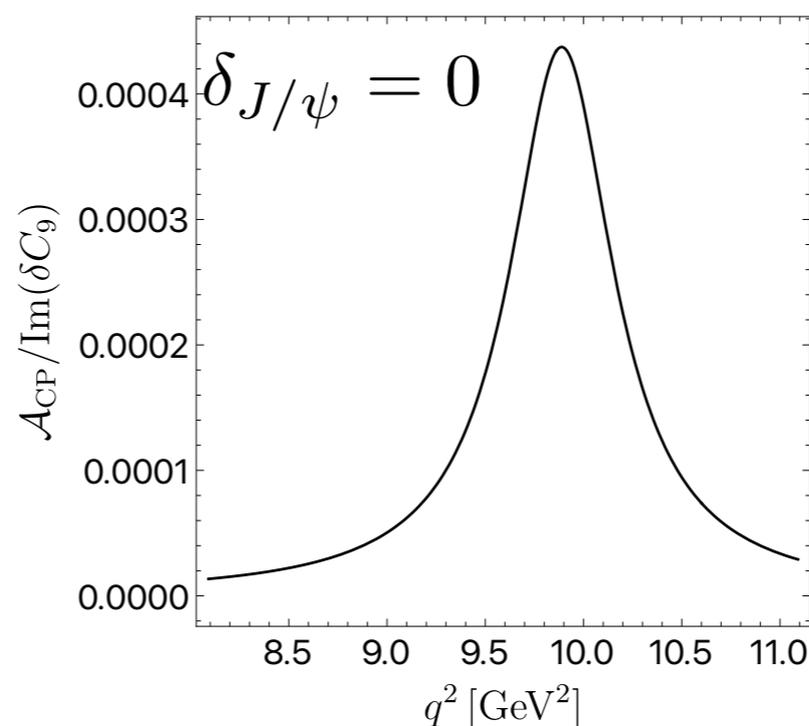
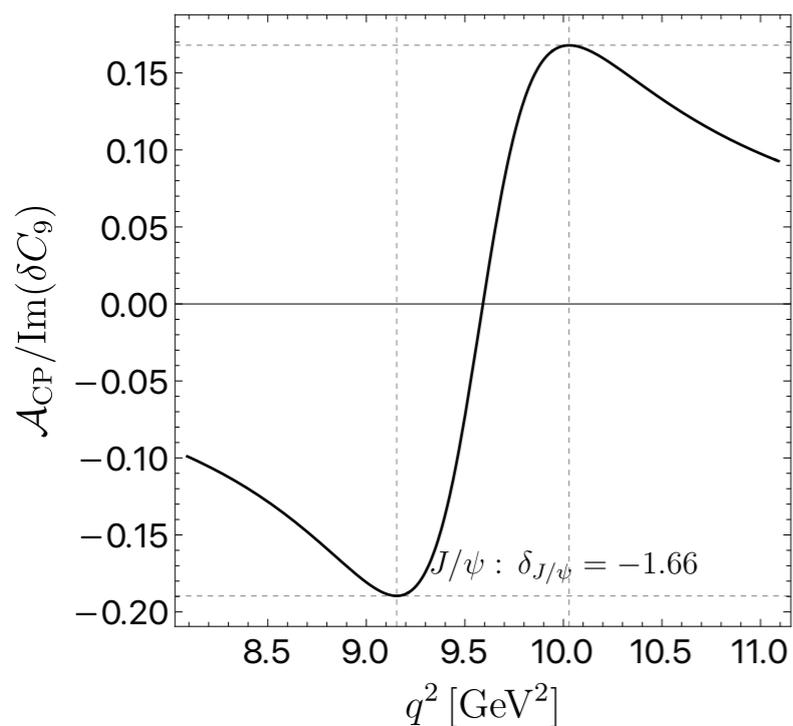


$$C_9^{\text{res}}(q^2) \approx \frac{m_j \Gamma_j \eta_j e^{i\delta_j}}{m_j^2 - q^2 - im_j \Gamma_j}$$

$$A_{\text{CP}} = \text{Im}(\delta C_9) \frac{2\eta_j (\cos \delta_j - x \sin \delta_j)}{\eta_j^2 - 2\eta_j B [\sin \delta_j + x \cos \delta_j] + A [1 + x^2]}$$

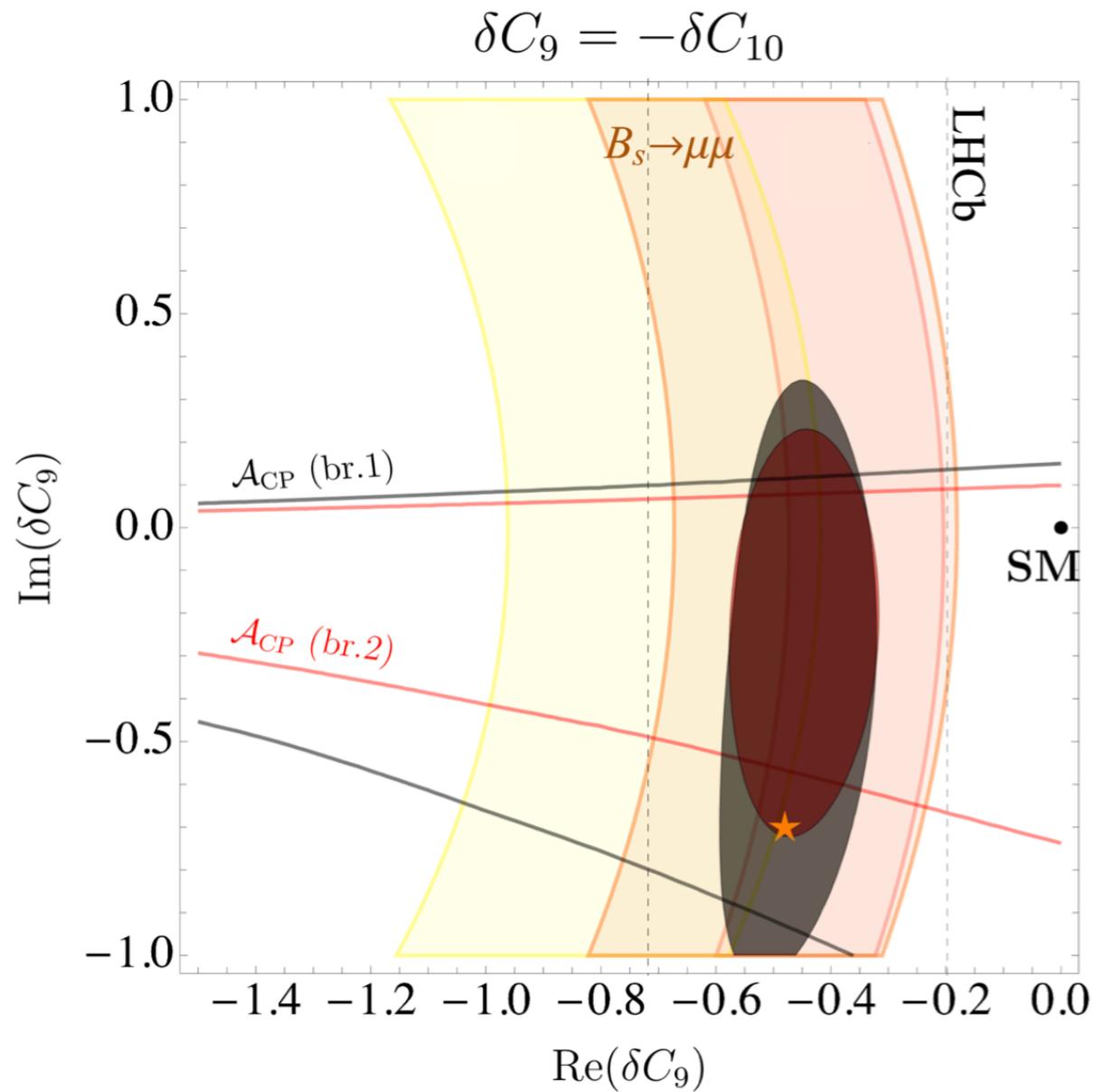
$$x \equiv (q^2 - m_j^2)/(m_j \Gamma_j)$$

Input: strong phase δ_j



Sensitive to CPV in δC_9

ALLOWED CPV IN NP



Orthogonality of constraints

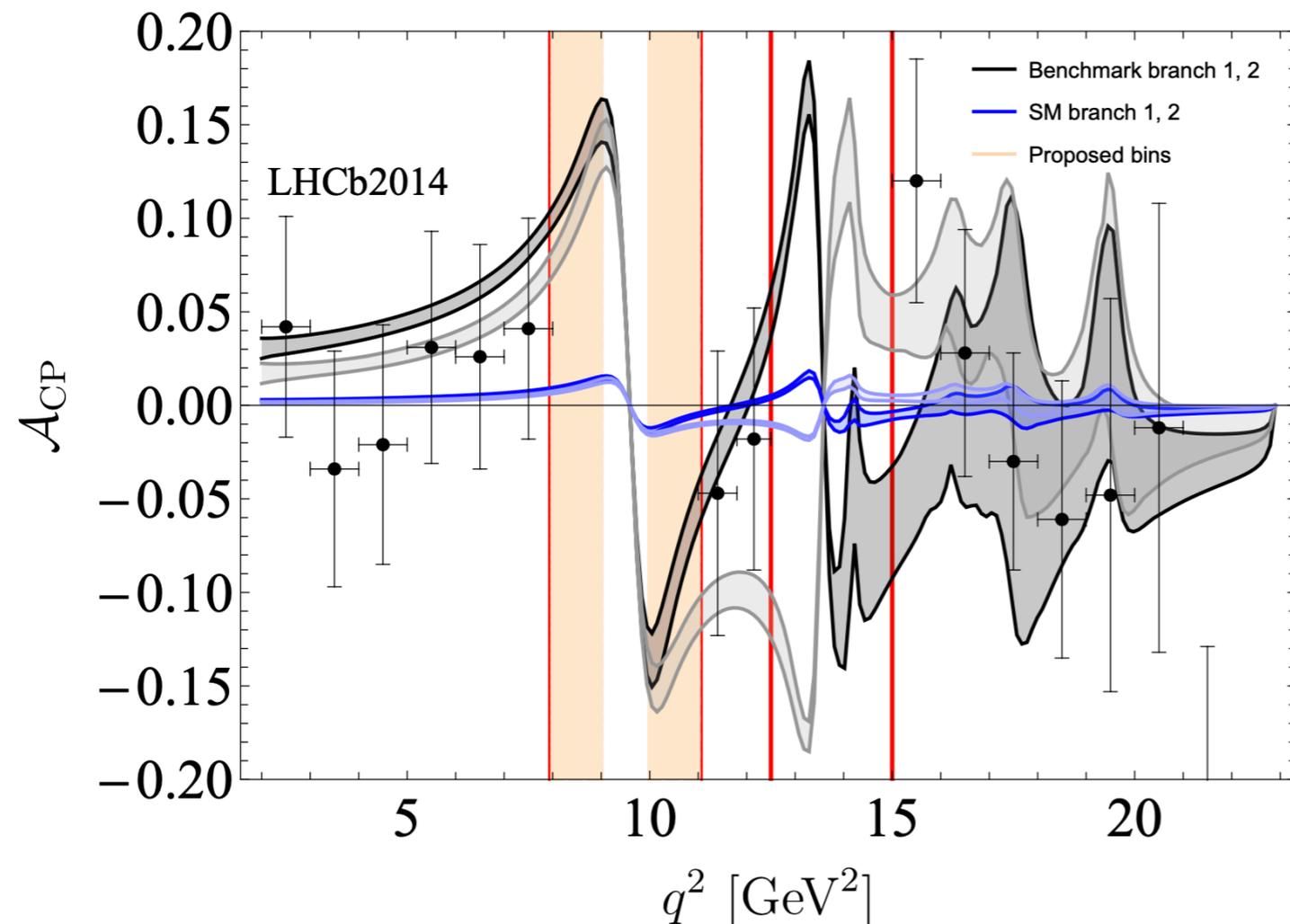
- Br($B_s \rightarrow \mu\mu$) and rates
- A_{CP} (2-8 GeV²)

★ $\delta C_9 = -\delta C_{10} = -0.46 - 0.71i$

benchmark scenario allows large imaginary part

RESONANT CPV

$$\delta C_9 = -\delta C_{10} = -0.46 - 0.71i$$



A. Smolkovic thesis '21
Becirevic et al, 2008.09064

Interesting region to look for direct CPV

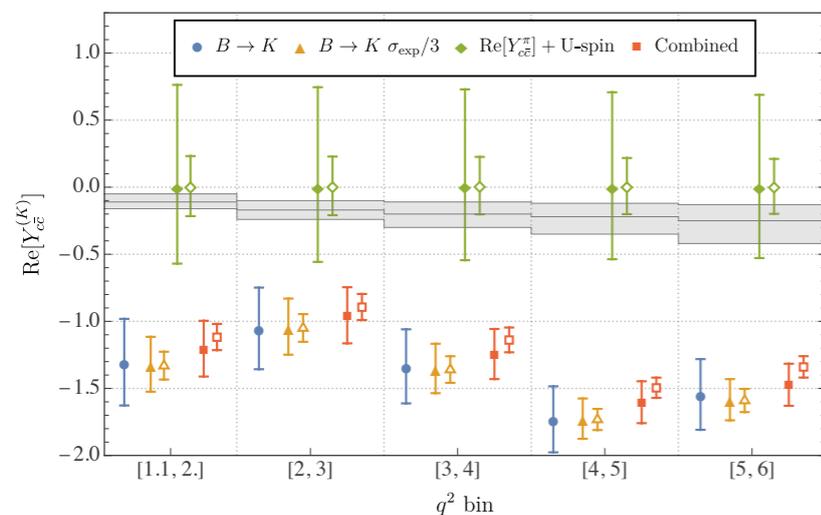
$$\Delta \mathcal{A}_{CP} \equiv \frac{\bar{\Gamma}_{[8,9]} - \Gamma_{[8,9]} - \bar{\Gamma}_{[10,11]} + \Gamma_{[10,11]}}{\bar{\Gamma}_{[8,9]} + \Gamma_{[8,9]} + \bar{\Gamma}_{[10,11]} + \Gamma_{[10,11]}}$$

$$\Delta \mathcal{A}_{CP} = \frac{0.0108(2) - 0.139(3) \text{Im}(\delta C_9)}{1 + 0.414(5) \text{Re}(\delta C_9) - 0.0082(1) \text{Im}(\delta C_9) + 0.054(1) |\delta C_9|^2}$$

NK, A. Smolkovic, 2108.11929
for other CPV constraints see also
Descotes-Genon, Novoa-Brunet, Vos, 2008.08000
Carvunis, Dettori, Gangal, Guadagnoli, Normand, 2102.13390

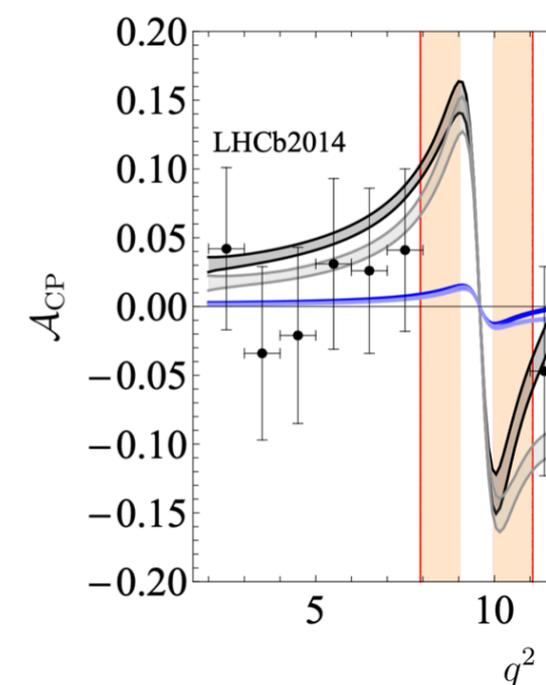
SUMMARY

- ▶ CKM structure enables extraction of non-local form factor $\text{Re}Y_{c\bar{c}}(q^2)$ for $B^- \rightarrow K^- \ell \ell$ and $B^- \rightarrow \pi^- \ell \ell$.
- ▶ U -spin ratio of CP-odd rates is an indicator of validity of CKM mechanism. Provides orthogonal handle on CP-even New Physics. Estimate of U -spin breaking needed!



$$R_{K/\pi}^{\text{CP}}|_{\text{NP}} = \left(\frac{\lambda_K}{\lambda_\pi}\right)^{3/2} \left(\frac{f_+^{(K)}}{f_+^{(\pi)}}\right)^2 \left[1 - \frac{\mathcal{C}_7^{\text{SM}}(\tilde{f}_T^{(\pi)} - \tilde{f}_T^{(K)})}{\mathcal{C}_9^{\text{SM}} + \mathcal{C}_7^{\text{SM}}\tilde{f}_T^{(K)}} - \epsilon_{uc}\right] \times \left(1 + \frac{\delta\mathcal{C}_9^{(s)} + \delta\mathcal{C}_7^{(s)}\tilde{f}_T^{(K)}}{\mathcal{C}_9^{\text{SM}} + \mathcal{C}_7^{\text{SM}}\tilde{f}_T^{(K)}}\right)$$

- ▶ New Physics with CPV in rare decays relies on absorptive $c\bar{c}$ amplitude, present close to the J/ψ resonance.



Thank you!