

Flavour anomalies, leptoquarks, renormalisation group fixed-points, and collider physics

Ulrich Nierste, Karlsruhe Institute of Technology

KIT Center Elementary Particle and Astroparticle Physics (KCETA)

Institute for Theoretical Particle Physics (TTP)



Leptoquarks and semileptonic decays

Scalar leptoquarks are a popular explanation of flavour anomalies.

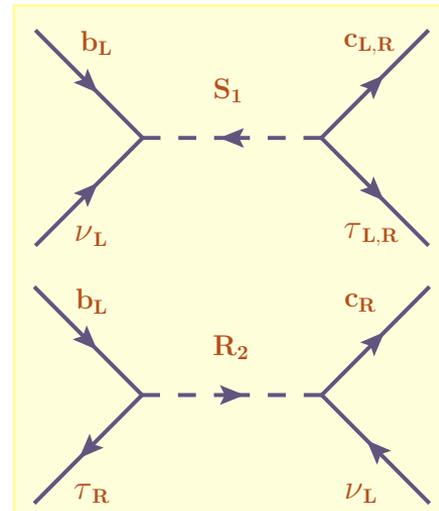
S_1 or R_2 for

$$R(D^{(*)}) = \frac{B(B \rightarrow D^{(*)}\tau\nu)}{B(B \rightarrow D^{(*)}\ell\nu)}, \quad \ell = e, \mu,$$

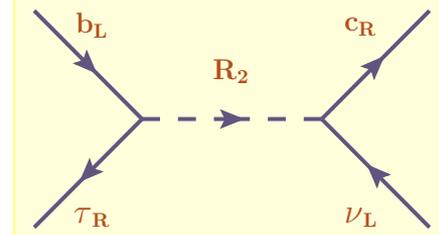
S_3 for $\text{low-}q^2$ deficit in several

$b \rightarrow s\ell^+\ell^-$, $\ell = e, \mu$,
decay distributions.

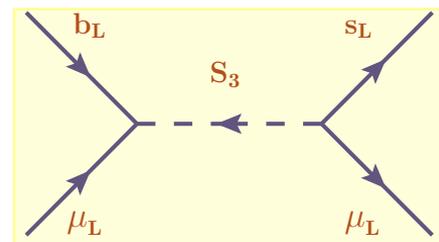
Spin 0,
SU(2) singlet



Spin 0,
SU(2) doublet



Spin 0,
SU(2) triplet



BSM mass reach

Flavour physics probes virtual effects of new heavy particles coupling to quarks, with a mass reach of

a **few TeV** in the case of S_1 or R_2 for $b \rightarrow c\tau\bar{\nu}$ and
 a **few tens of TeV** in the case of S_3 for $b \rightarrow s\ell^+\ell^-$.

⇒ The firm establishment of a flavour anomaly helps for the design of a future hadron collider and could establish a “**no-lose**” situation for **FCC-hh**.

FCC-hh fans  flavour physics

flavour physicists  **FCC-ee: 10^{13} Z bosons** are a perfect b factory!

Outline

- Status of new physics in $b \rightarrow c\tau\nu$
- Status of new physics in $b \rightarrow s\ell^+\ell^-$
- Renormalisation group analysis of leptoquark solutions
- Leptoquarks at colliders
- Summary and outlook

Status of new physics in $b \rightarrow c\tau\nu$

$$b \rightarrow c\tau\nu$$

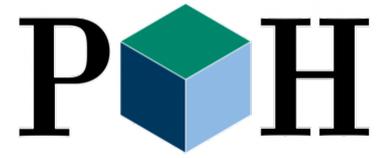
b-flavoured hadron $H_b = B_d, B^+, \Lambda_b$:

$$R(H_c) \equiv \frac{B(H_b \rightarrow H_c\tau\nu)}{B(H_b \rightarrow H_c\ell\nu)} \text{ with } \ell = e, \mu$$

Predictions involve form factors like $\langle D(\vec{p}_D) | \gamma^\mu | B(\vec{p}_B) \rangle$ or $\langle D^*(\vec{p}_D, \epsilon) | \gamma^\mu \gamma_5 | B(\vec{p}_B) \rangle$.

Lattice gauge theory calculates form factors for $\vec{p}_D = \vec{p}_B = \mathbf{0}$ and a few points with small $D^{(*)}$ velocity.

$b \rightarrow c\tau\nu$: Developments since Quirks 2022



$$R(H_c) \equiv \frac{B(H_b \rightarrow H_c\tau\nu)}{B(H_b \rightarrow H_c\ell\nu)}$$

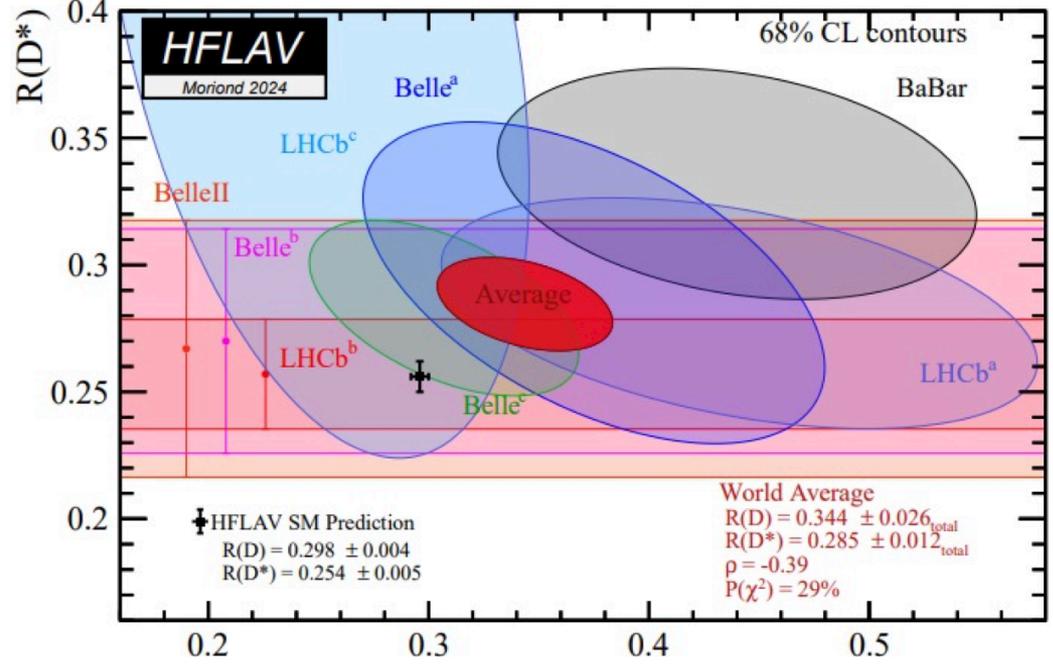
New LHCb $R(D^+)$ measurement:
Significance of deviation from SM
down:

$$3.3\sigma \rightarrow 3.1\sigma,$$

for the form factors used by HFLAV.

Different measurements (from four experiments) agree within normal statistical fluctuations.

After $R(D^+)$



$B \rightarrow D^*$ form factors

Compare

BGL (Boyd, Grinstein, Lebed 1995):

global fit by Gambino, Jung, Schacht in 2019 to all available calculations and data in $B \rightarrow D^* \ell \nu$ with light leptons $\ell = e, \mu$. Phys. Lett. B 795 (2019) 386

HQET (using expansions in $\Lambda_{\text{QCD}}/m_{c,b}$):

global fit by Iguro, Kitahara and Watanabe in 2022 to all available calculations and data (including q^2 shapes) in $B \rightarrow D^* \ell \nu$ with light leptons $\ell = e, \mu$. arXiv:2210.10751

Fermilab/MILC (2021):

first lattice calculation employing $q^2 \neq q_{\text{max}}^2$.

Eur. Phys. J. C 82 (2022) 1141, Eur.Phys.J.C 83, 21 (2023).

$B \rightarrow D^*$ form factors

DM (Dispersive Matrix approach, Rome lattice group):

uses Fermilab/MILC data and Rome calculation of susceptibility χ ,

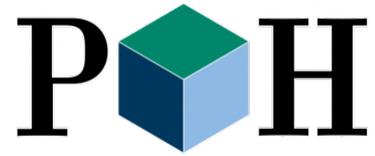
employs analyticity and unitarity constraints to derive two-sided bounds on form factors.

G. Martinelli, S. Simula, and L. Vittorio, Phys. Rev. D 104 (2021) 094512,
Eur. Phys. J. C 82 (2022) 1083, JHEP 08 (2022) 022.

G. Martinelli, M. Naviglio, S. Simula, and L. Vittorio, Phys. Rev. D 106 (2022) 093002.

With DM method find $R(D^*)$ compatible with Standard Model prediction and furthermore $|V_{cb}|$ from $B \rightarrow D^* \ell \nu$ consistent with $|V_{cb}|$ from inclusive $B \rightarrow X_c \ell \nu$ decays.

$B \rightarrow D^*$ form factors vs new physics



Next slides: confront all four form factor predictions with new data on

the fraction $F_L^{D^*,\text{light}}$ of longitudinally polarized D^* in $B \rightarrow D^* \ell \nu$
and

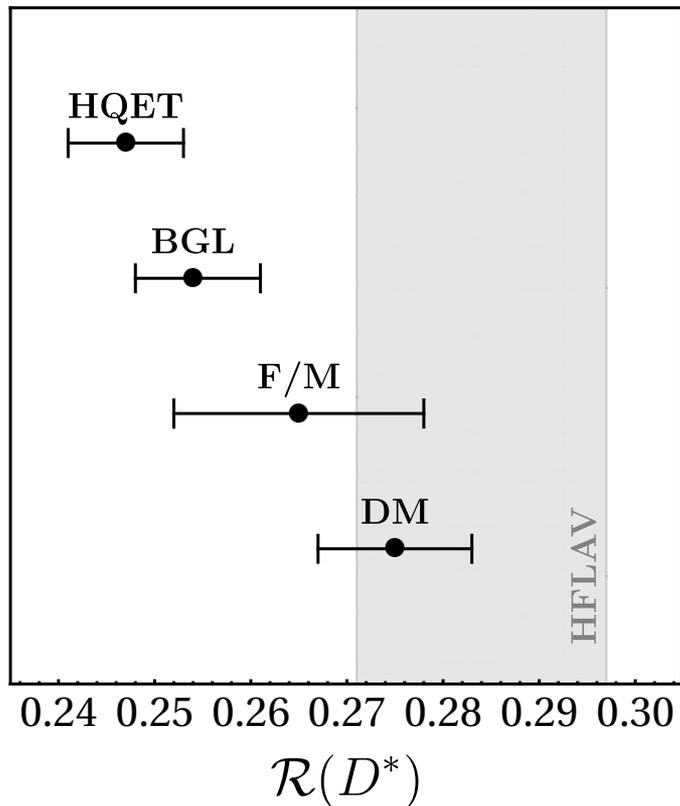
the forward-backward asymmetries A_{FB}^e and A_{FB}^μ

[Belle, 2301.07529](#); Belle II, talk by Chaoyi Lyu at ALPS, March 2023

Discriminating $B \rightarrow D^* \ell \nu$ form factors via polarization observables and asymmetries

[Fedele,Blanke,Crivellin,Iguro,UN,Simula,Vittorio, arXiv:2305.15457.](#)

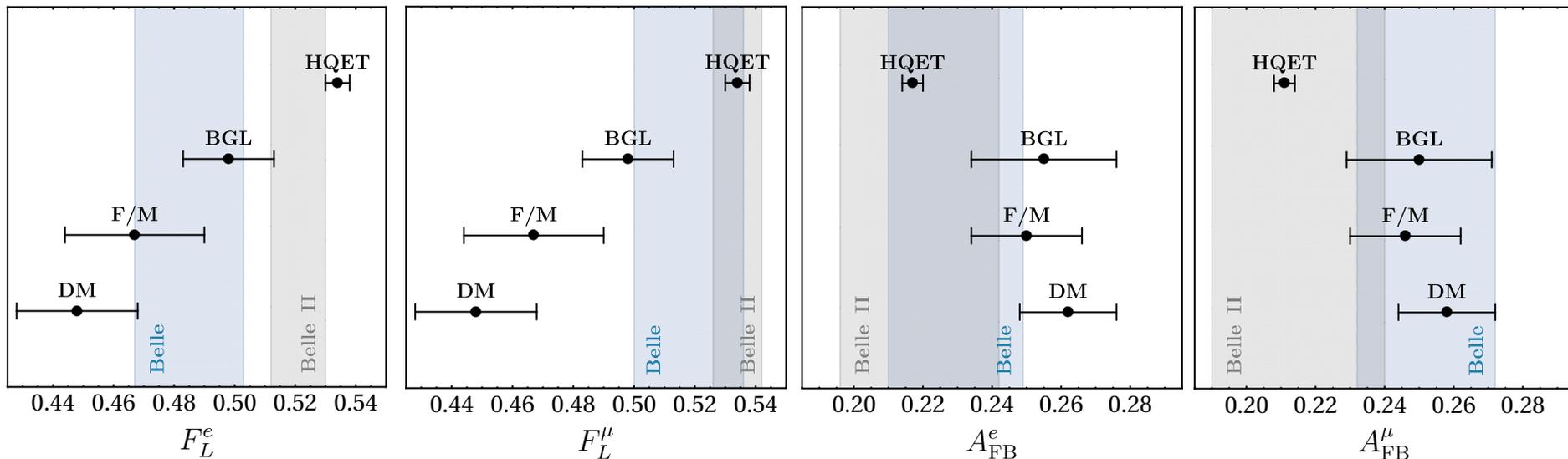
$B \rightarrow D^*$ form factors vs new physics



compatible with Standard Model

with DM method one finds the same $R(D)$ as with other methods, [arXiv:2205.13952](https://arxiv.org/abs/2205.13952)

Predictions for $F_L^{D^*,\text{light}}$ and $A_{\text{FB}}^{e,\mu}$



SM predictions with $\left\{ \begin{array}{l} \text{HQET or BGL} \\ \text{F/M or DM} \end{array} \right\}$ describe $\left\{ \begin{array}{l} B \rightarrow D^* \ell \nu \\ R(D^*) \end{array} \right\}$ data.

Effective BSM operators

Nice: We can describe **all types** of new physics in terms of effective four-quark operators:

$$O_V^L = \bar{c}_L \gamma^\mu b_L \bar{\tau}_L \gamma_\mu \nu_{\tau L},$$

$$O_S^R = \bar{c}_L b_R \bar{\tau}_R \nu_{\tau L},$$

$$O_S^L = \bar{c}_R b_L \bar{\tau}_R \nu_{\tau L},$$

$$O_T = \bar{c}_R \sigma^{\mu\nu} b_L \bar{\tau}_R \sigma_{\mu\nu} \nu_{\tau L}.$$

Fit the corresponding coefficients $C_V^L, C_S^{R,L}, C_T$ to data.

Blanke, Crivellin, de Boer, UN, Nisandzic, Kitahara, *Phys.Rev.D* 100(2019) 3, 035035

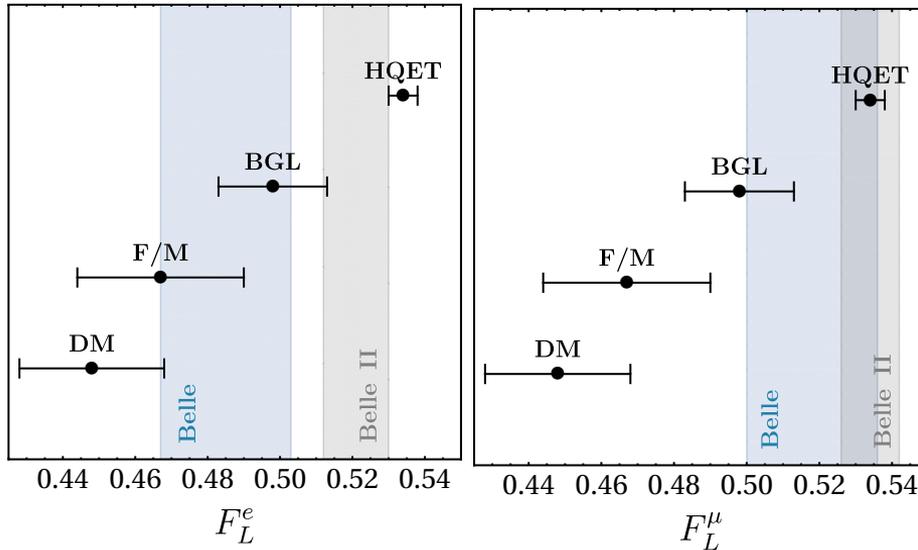
Iguro, Kitahara, Watanabe, arXiv:2210:10751, arXiv:2405:06062

$F_L^{D^*,\text{light}}$ as a form factor filter



No BSM scenario has a measurable impact on $F_L^{D^*,\text{light}}$!

Fedele, Blanke, Crivellin, UN, Iguro, Simula, Vittorio, *Phys.Rev.D* 108 (2023) 5, 5

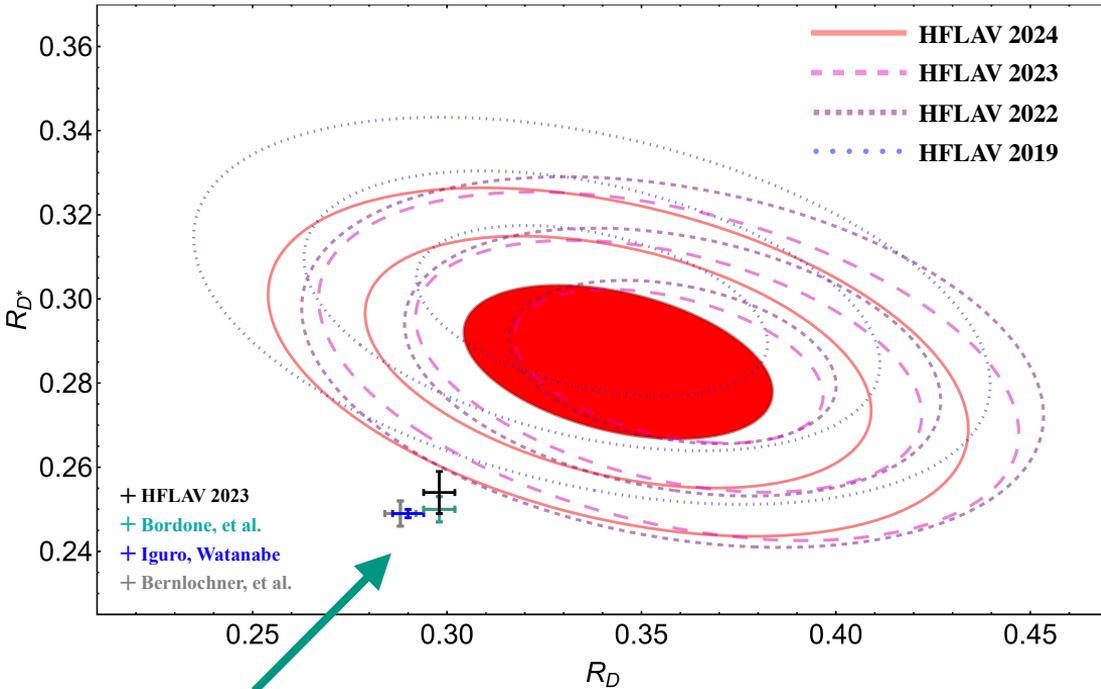


} good form factors

} too steep form factors

“HQET” form factors of Watanabe et al. use Belle(-II) data

$R(D^{(*)})$ with best form factors



difference in HFLAV and HQET form factors matters!

Deviation from SM prediction:

4.3σ

using also new Belle/LHCb average

$$F_L^{D^{*},\tau} = 0.49 \pm 0.05$$

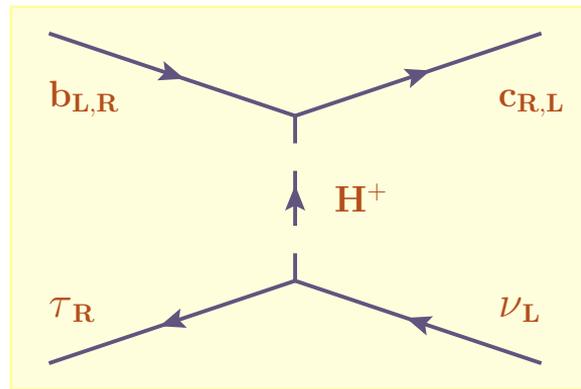
Good fits (pulls $\geq 4.0\sigma$) for all tree-level BSM scenarios, including charged-Higgs exchange.

Iguro, Kitahara, Watanabe, arXiv:2405.06062

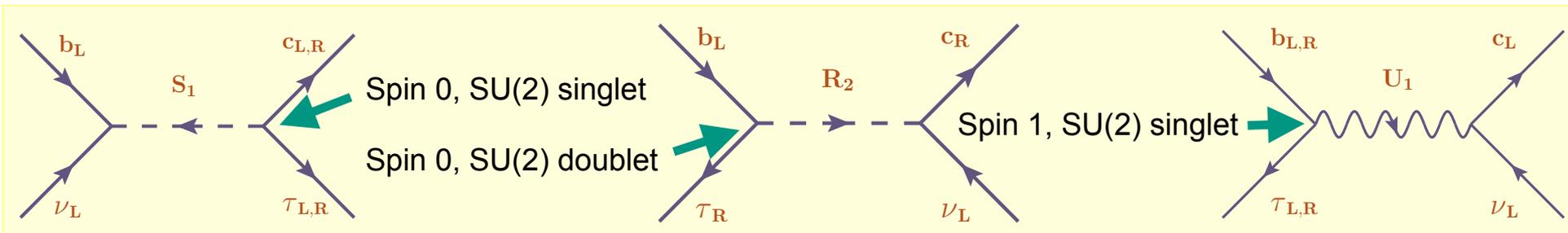
BSM explanations of $b \rightarrow c\tau\bar{\nu}$ data

- Charged Higgs boson:
 - was known to be sensitive to effects of a hypothetical **charged Higgs boson** since 1992.

Grzadkowski, Hou, Phys. Lett. B **283** (1992) 427

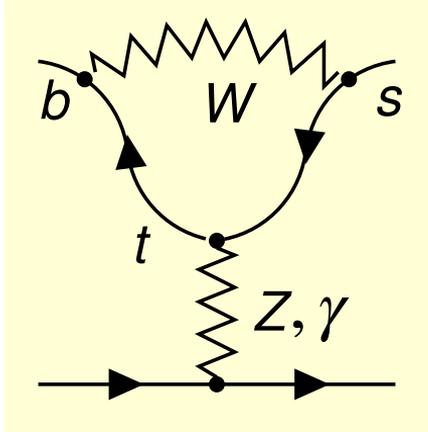


- Leptoquarks:
 - bosons with quark-lepton coupling
 - appear in **SU(4)** gauge theories, where lepton number is the fourth colour



Status of new physics

in $b \rightarrow s \ell^+ \ell^-$



Belle II has measured $B(B \rightarrow K\nu\bar{\nu})$ 2.7σ above the SM prediction.

[arXiv:2311.14647](https://arxiv.org/abs/2311.14647)

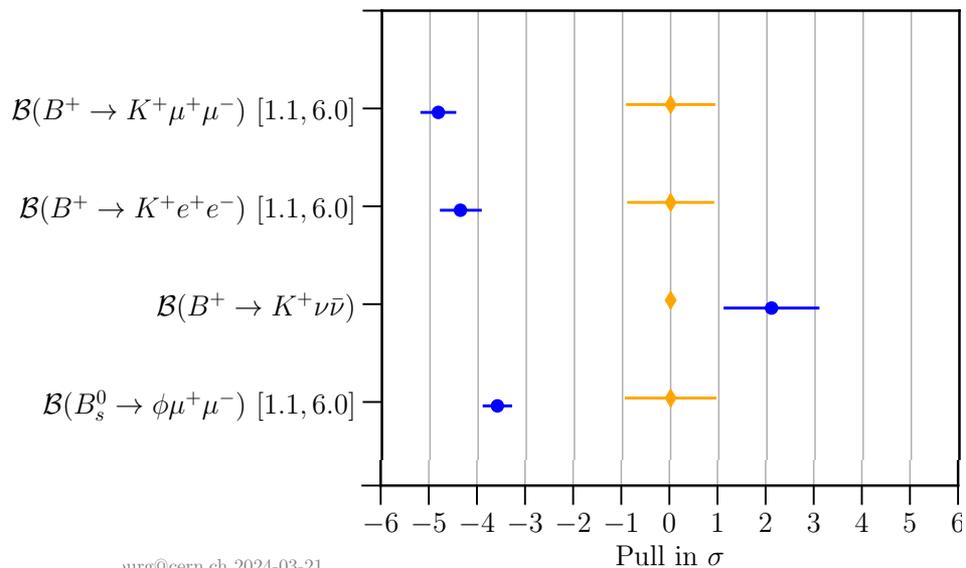
persists since 2013

$B(B \rightarrow K^{(*)}\ell^+\ell^-)$,
 $B(B_s \rightarrow \phi\mu^+\mu^-)$ lower than SM predictions for $1.1 \text{ GeV}^2 \leq q^2 \leq 8 \text{ GeV}^2$.

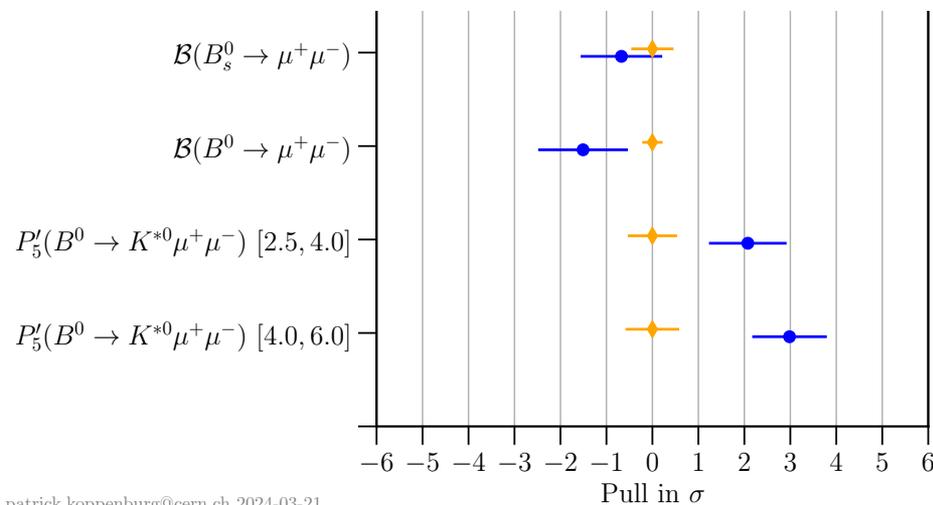
ν_ℓ and ℓ form an SU(2) doublet $L = \begin{pmatrix} \nu_\ell \\ \ell \end{pmatrix}$.

\Rightarrow potential connection between the two anomalies.

$b \rightarrow s$ flavour anomalies overview



nurg@cern.ch 2024-03-21



patrick.koppenburg@cern.ch 2024-03-21

from Patrick Koppenburg's web page <https://www.nikhef.nl/~pkoppenb/anomalies.html>

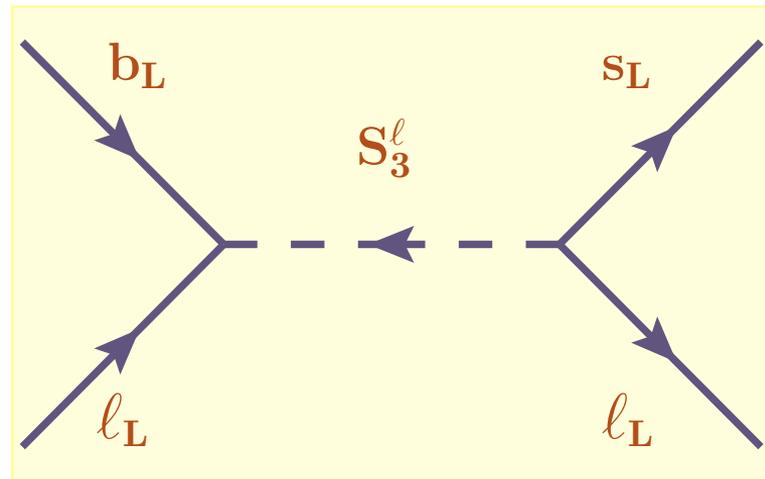
$b \rightarrow s\ell^+\ell^-$: Developments since Quirks 2022

Hints of $B(B \rightarrow K^{(*)}e^+e^-) \neq B(B \rightarrow K^{(*)}\mu^+\mu^-)$ were not confirmed after 2022 reanalysis of LHCb data.

⇒ New-physics contributions must affect **both** $b \rightarrow s\mu^+\mu^-$ and $b \rightarrow se^+e^-$.

Leptoquarks: To avoid excessive contributions to $\mu \rightarrow e$ conversion, need different copies of S_3^ℓ , with S_3^e coupling to electrons and S_3^μ coupling to muons.

LHCb data are compatible with lepton flavour universality (LFU)

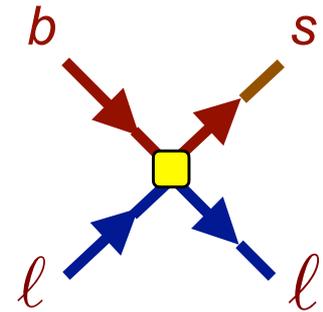
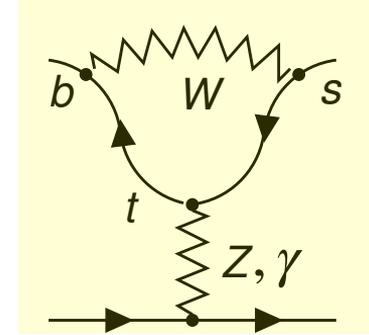


Effective hamiltonian

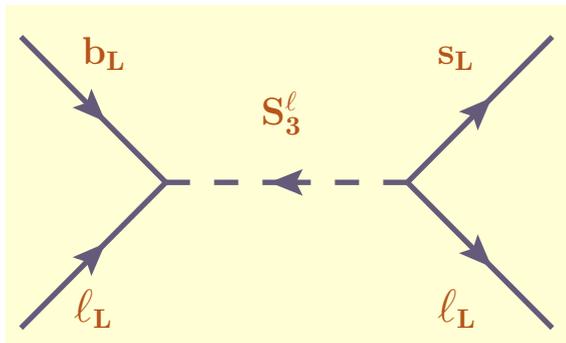
$$H \propto \sum_{\ell=e,\mu,\tau} C_9^\ell Q_9^\ell + C_{10}^\ell Q_{10}^\ell$$

with

$$Q_9^\ell = \frac{\alpha}{4\pi} \bar{s}_L \gamma_\mu b_L \ell \gamma^\mu \ell \quad \text{and} \quad Q_{10}^\ell = \frac{\alpha}{4\pi} \bar{s}_L \gamma_\mu b_L \ell \gamma^\mu \gamma_5 \ell$$



Leptoquark explanation



SU(3) triplet leptoquark.

Mass < 35 TeV for couplings $< \mathcal{O}(1)$.

Contributes to both $C_9^{\ell\ell}$ and $C_{10}^{\ell\ell}$. Effects in $C_{10}^{\mu\mu}$ will affect $B(B_s \rightarrow \mu^+ \mu^-)$ as well. O.k. with **LHCb** data, less so with **CMS** data.

To avoid unacceptably large $\mu \rightarrow e$ conversion postulate one leptoquark S_3^ℓ per flavour $\ell = e, \mu, \tau$.

But observed approximate lepton flavour universality requires $M_{S_3^e} \sim M_{S_3^\mu}$ and also similar couplings of S_3^e and S_3^μ .

Renormalisation group analysis of leptoquark solutions

Mass gap

Flavour anomalies are usually explained by postulating a new particle with mass in the TeV range *ad-hoc*. The other particles of a reasonable UV completion are heavier.

Leptoquarks: Motivation in models with quark-lepton unification, such as $SU(4)_c$ models à la Pati-Salam. Heavy gluons (which are vector-like leptoquarks) must have masses above 1000 TeV to comply with bounds on $B(K_L \rightarrow \mu e)$.

Mass gap between the LQ masses as and the scale of the UV completion:
 ⇒ study low-energy properties of LQ couplings without knowing details of the UV model with **renormalisation group (RG)** equations.

Prototype example: Probing SM **gauge unification** at GUT scale only involves SM RG equations. GUT masses only enter next-to-leading order corrections.

Leptoquark-quark-lepton couplings

Couplings of several $SU(2)$ triplet leptoquarks S_3^a :

$$\mathcal{L}_{S_3} = y_{3ij}^a \bar{Q}_{L,i}^{C,l} \epsilon^{lm} (\tau^k S_3^{a,k})^{mn} L_{L,j}^n + \text{h.c.}$$

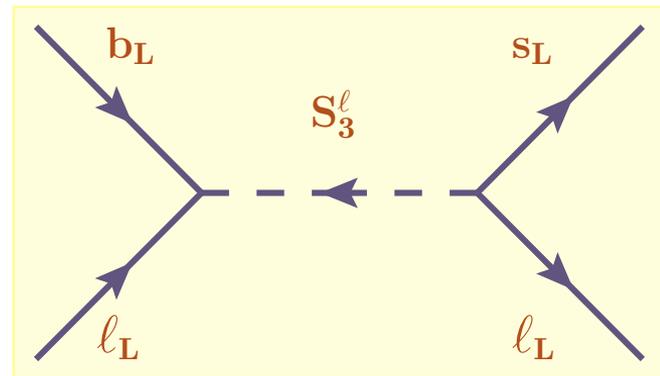
a : labels the LQ

i : quark generation index

j : lepton generation index

$$\epsilon = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$$

Pauli matrices



Consider lepton number conservation $y_{3ij}^a \propto \delta_{aj}$ to suppress LFV processes like $\mu \rightarrow e$ conversion.

Infrared fixed-point

RG beta functions are known for generic BSM theories.
 Machacek, Vaughn, 1983, 1984

At fixed points of the RG equations the beta functions are zero.

Quasi-fixed point: The beta functions of the LQ couplings y_{3ij}^a are zero, while the beta function of the SM couplings are not.

Infrared fixed point: y_{3ij}^a at the low scale as probed in flavour or collider experiments is predicted.

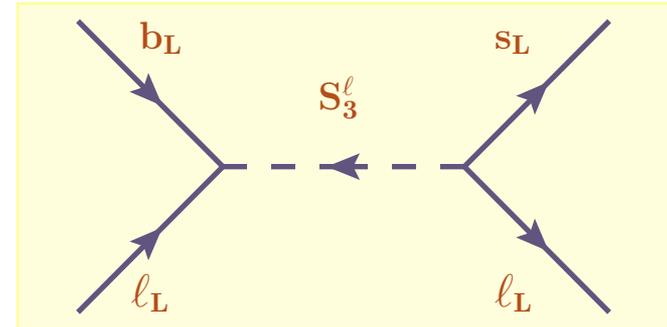
Infrared fixed-point for S_3^ℓ scenario

Result for S_3^ℓ leptoquarks:

Fedele, UN, Wüst, JHEP 11 (2023) 131, Bachelor thesis F.Wüst

Infrared fixed-point solutions:

$y_{3\ 21}^e$	$y_{3\ 31}^e$	$y_{3\ 22}^\mu$	$y_{3\ 32}^\mu$	$y_{3\ 23}^\tau$	$y_{3\ 33}^\tau$
0.760	0.189	0.191	0.759	0.639	-0.452
0.189	0.760	0.759	0.191	0.639	-0.452

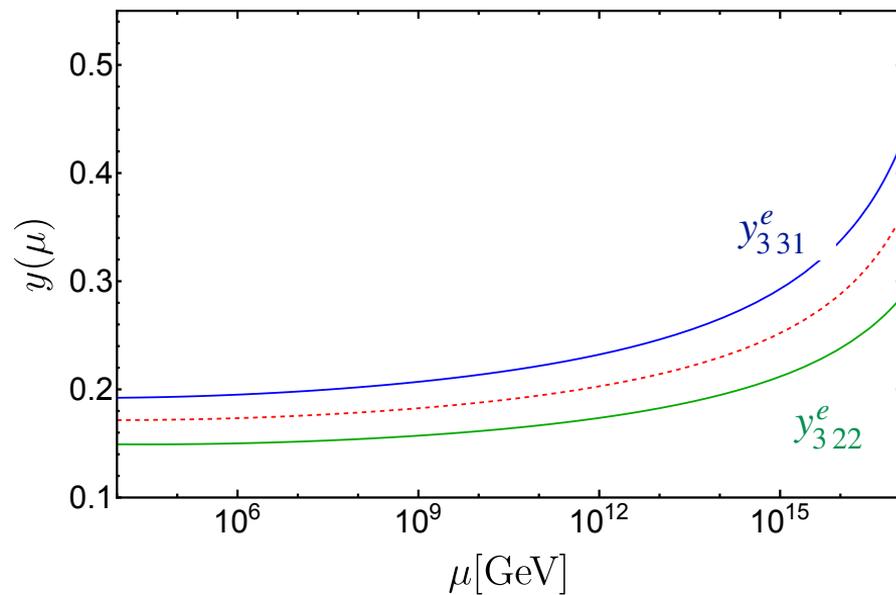
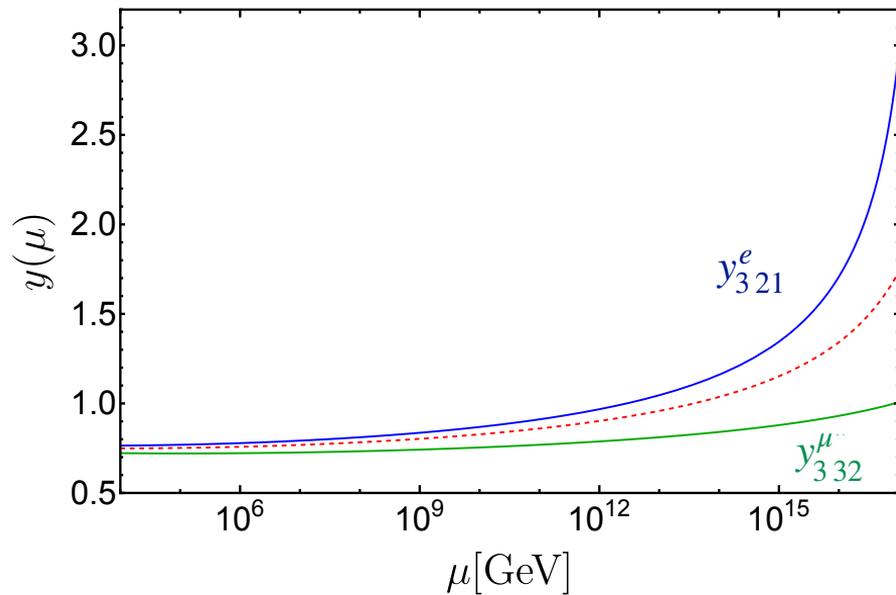


and two more pairs found from permutations of (e, μ, τ) .

Partial lepton-flavour universality (LFU) as an emerging feature! The third generation comes with opposite sign for $C_{9,10}^{\ell\ell}$. Prediction for $b \rightarrow s\tau^+\tau^-$!

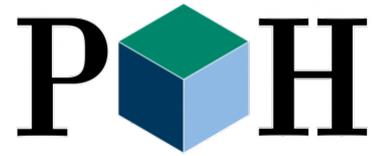
LFU needs three copies of S_3^ℓ , with just two S_3^ℓ find opposite signs.

Infrared fixed-point for (S_1^ℓ, S_3^ℓ) scenario



Bizarre: s - e coupling converges to b - μ coupling and b - e coupling converges to s - μ coupling!

Infrared fixed-point (S_1^ℓ, S_3^ℓ) scenario

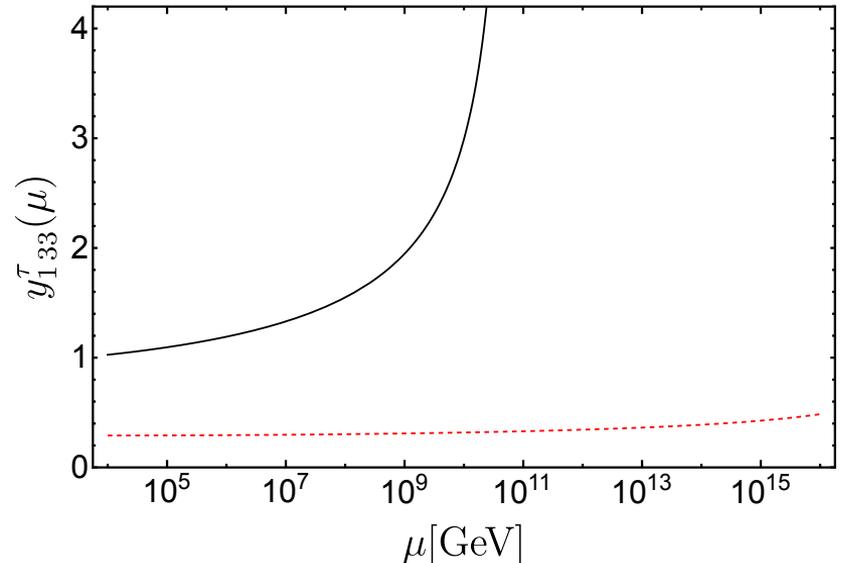


The infrared fixed point for the S_1^τ coupling is smaller than the coupling inferred from $b \rightarrow c\tau\bar{\nu}$ data (for S_1^τ masses allowed by collider searches).

Landau pole:

⇒ upper bound on scale of
quark-lepton unification:

$$M_{\text{QLU}} \lesssim 10^{11} \text{ GeV}$$



Prediction for $B \rightarrow K^{(*)}\nu\bar{\nu}$

For the fixed-point solution for the S_3^ℓ couplings and the S_1^ℓ coupling fixed from the $b \rightarrow c\tau\nu$ anomaly we find a 10% enhancement of $B(B \rightarrow K\nu\bar{\nu})$ and $B(B \rightarrow K^*\nu\bar{\nu})$ from the S_1^ℓ contribution, detectable by Belle II.

Leptoquarks at colliders

Radiative corrections...

...to collider processes with leptoquarks (LQ):

- QCD corrections to pair production at Tevatron and LHC:
M. Krämer, T. Plehn, M. Spira, P.M. Zerwas, *Phys. Rev. Lett.* 79, 341 (1997), *Phys.Rev.D* 71 (2005) 057503;
- QCD and QED corrections to resonant production:
A. Greljo, N. Selimovic, *JHEP* 03 (2021) 279.
- NNLO resummation of soft gluon radiation in pair production
C. Borschensky, B. Fuks, A. Kulesza, D. Schwartländer, *JHEP* 02 (2022) 157.

But if we invoke $\mathcal{O}(1)$ quark-lepton-LQ couplings to explain B anomalies, radiative corrections with these might be sizeable as well.

Radiative corrections...

...linking low-energy to collider observables.

Innes Bigaran, Rodolfo Capdevilla, UN

Focus: **universal** radiative corrections linking couplings

$$y_{njk}^{XY} \text{ with } X, Y = L, R,$$

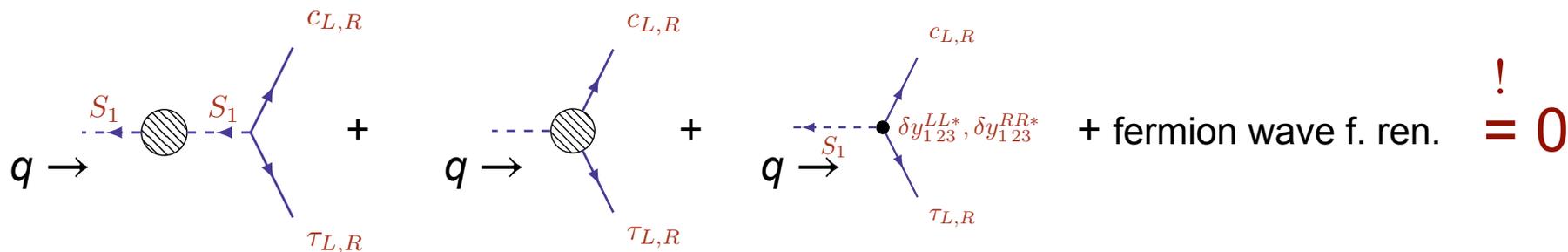
probed at low and high energy to each other.

Define two renormalisation schemes with couplings $y_{njk}^{XY,low}$ and $y_{njk}^{XY,high}$,

defined such that radiative corrections vanish for zero LQ momentum q or for on-shell LQ, $q^2 = M_{LQ}^2$.

Coupling renormalisation

Example: coupling of LQ S_1 to charm and tau, $y_{123}^{LL,RR}$.



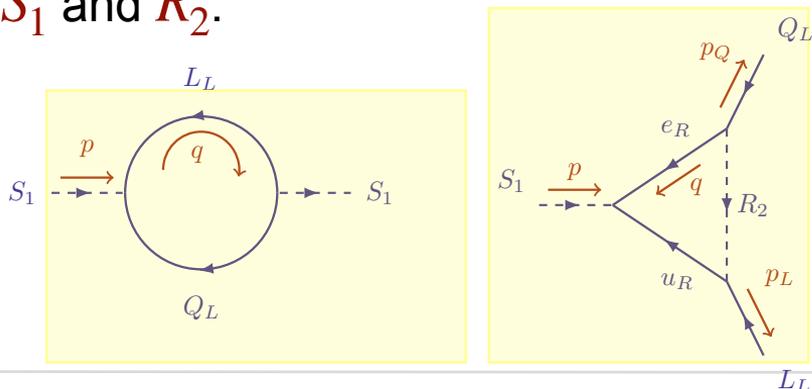
For $y_{123}^{LL,RR,low}$ this condition on the counterterm is imposed for $q = 0$. $b \rightarrow c\tau\bar{\nu}$ data constrain $y_{123}^{LL,RR,low} \times y_{133*}^{LL,RR,low}$ as a function of M_{S_1} .
Likewise $y_{123}^{LL,RR,high}$ is defined by imposing this for $q^2 = M_{S_1}^2$.

Couplings at low and high energy

$\kappa_{1jk}^{LL} \equiv \frac{y_{1jk}^{LL,high}}{y_{1jk}^{LL,low}}$ captures the process-independent part of the radiative corrections

entering collider-physics observables of S_1 , if $y_{1jk}^{LL,low}$ is taken from flavour data.

If only one LQ species is present, there are no vertex corrections. For these need both S_1 and R_2 :



If only one LQ species is present, only the LQ self-energy contributes to κ_{1jk}^{LL} .

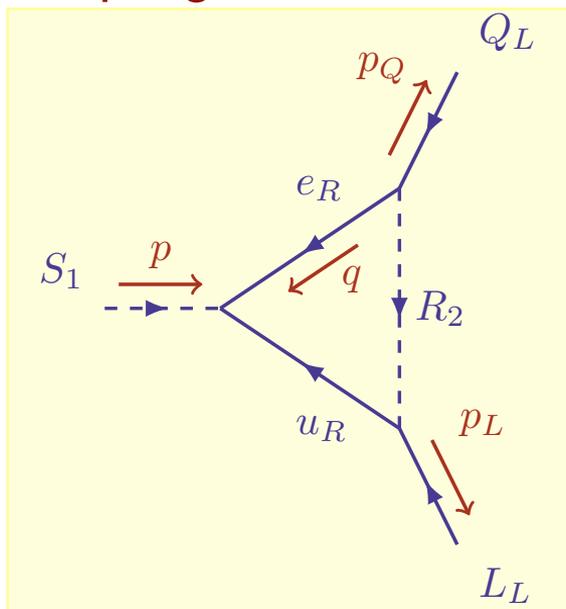
Couplings at low and high energy

- The κ_{njk}^{XY} factors are close to one, if all y_{njk}^{XY} are $\leq \mathcal{O}(1)$. In these cases one can use the y_{njk}^{XY} inferred from the flavour anomalies for collider searches.
- Perturbation theory seems to work for $y_{njk}^{XY} = \mathcal{O}(5)$. Collider searches first exclude the parameter region with small LQ mass and large couplings, thus for this the κ_{njk}^{XY} factors matter. If such a scenario shall explain flavour anomalies (with not-too-heavy LQ), the couplings must be hierarchical, e.g.

$$|y_{123}^{LL,RR}| \gg |y_{133}^{LL,RR}| \text{ or } |y_{123}^{LL,RR}| \ll |y_{133}^{LL,RR}|.$$
- $\kappa_{njk}^{XY} < 1 \Rightarrow$ couplings in collider processes **weaker** than in flavour physics

Vertex corrections

- The vertex correction in scenarios with both S_1 and R_2 involves **different couplings** than the tree-level coupling, e.g.



$$S_1 - Q_L - L_L \text{ coupling} \propto y_{1jk}^{RR} \times y_{2jl}^{RL} \times y_{2mk}^{LR*}$$

can be important if y_{1ml}^{LL} is small.

The vertex loop function is smaller than expected.

Summary

Summary

- Current flavour anomalies probe BSM physics with particle masses in the multi-TeV range.
 - ⇒ instrumental to justify and design future hadron colliders
- $b \rightarrow c\tau\bar{\nu}$:
 - Form factors better known thanks to new polarisation measurements in $b \rightarrow c\ell\bar{\nu}$ polarisation data.
 - **Charged-Higgs** and various **leptoquark** scenarios have pulls of 4.0σ compared to SM.
 - Future: D^* and τ polarisation data

Summary

- $b \rightarrow s\ell^+\ell^-$:
 - Data show approximate LFU between e and μ . Popular S_3 leptoquark needs several copies with lepton number conservation
- Leptoquark models:
 - embedding into theory of quark-lepton unification requires a mass gap, opportunity to use RG methods
 - $S_3^{\ell\ell}$ couplings have IR fixed point with equal contributions to two of the three $C_{9,10}^{\ell\ell}$ coefficients, while the third one has opposite sign.
 - ⇒ Two-generation LFU emerges dynamically.

Summary

- Radiative corrections with virtual leptoquarks involve small loop functions.
 - Does perturbation theory permit largish quark-lepton-LQ couplings? Will this permit us to explain $b \rightarrow c\tau\bar{\nu}$ anomalies with large LQ masses evading collider search bounds?
 - For $\mathcal{O}(1)$ couplings our radiative corrections are very small.
 - Since collider exclusion bounds probe the large-coupling region most efficiently, the κ_{njk}^{XY} factors should be included when deriving bounds on the couplings y_{njk}^{XY} .

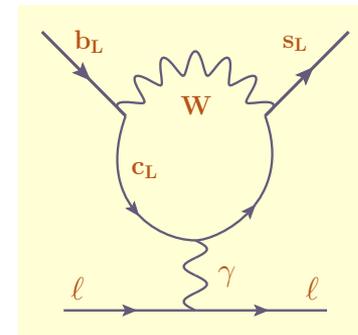
Backup slides

$$b \rightarrow s \ell^+ \ell^-$$

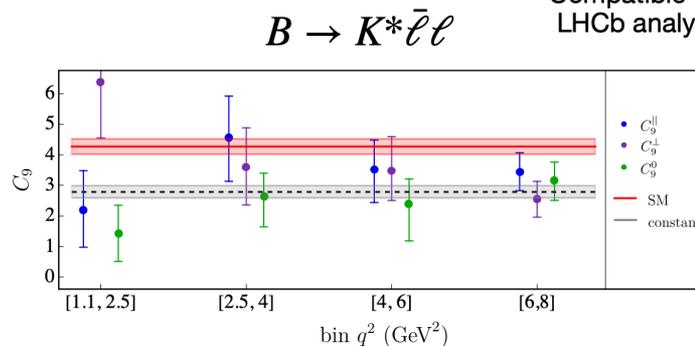
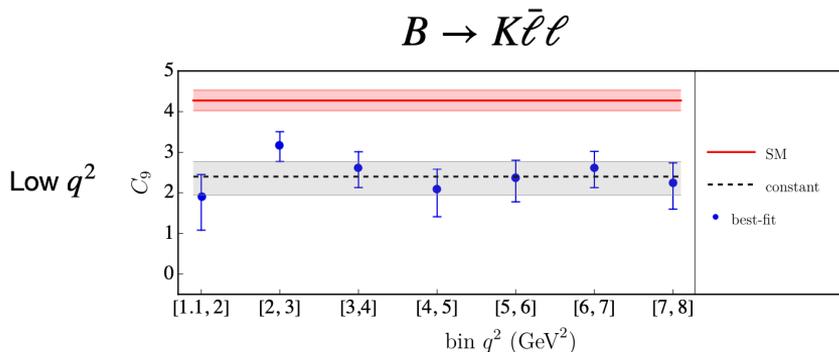
A BSM explanation of $b \rightarrow s \ell^+ \ell^-$ data require contribution to $C_9^{\mu\mu} \sim C_9^{ee}$ of order $-0.25 \cdot C_9^{\text{SM}}$.

Claim: enhancement of charm loop could fake BSM signal.

Test this by fitting for q^2 -dependence of C_9^{BSM} :



Compatible with LHCb analysis!



[Bordone, Isidori, Mächler, Tinari, arXiv:2401.18007](https://arxiv.org/abs/2401.18007)