

Suppressed interference in the SMEFT  
and related topics  
Celine Degrande

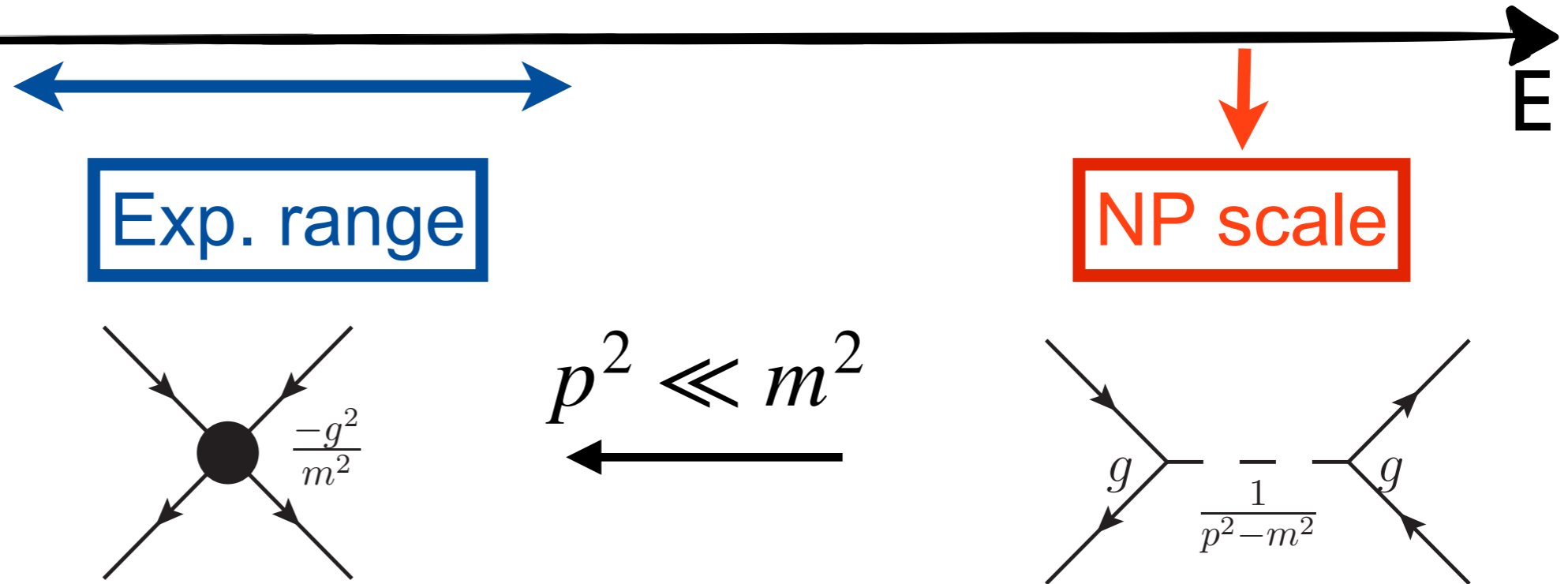
# Plan

- Introduction to SMEFT
- SMEFT and interference
- CPV in EW diboson
- NLO corrections
- Dim-8 in diboson
- Further comments

# Introduction to SMEFT

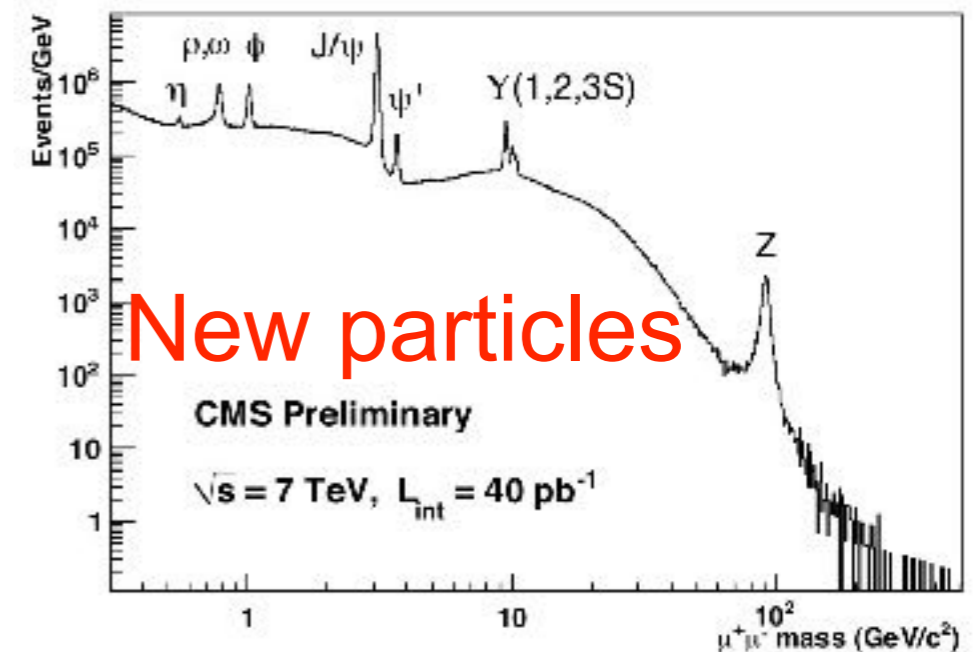
# Indirect detection of NP

- Assumption : NP scale  $\gg$  energies probed in experiments



One assumption :  $p^2 \ll m^2$

New/modified interactions between SM particles





# EFT

Parametrize any NP but an  $\infty$  number of coefficients

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_{d>4} \sum_i \frac{C_i}{\Lambda^{d-4}} \mathcal{O}_i^d \leftarrow \text{SM fields \& sym.}$$

- Assumption :  $E_{\text{exp}} \ll \Lambda$

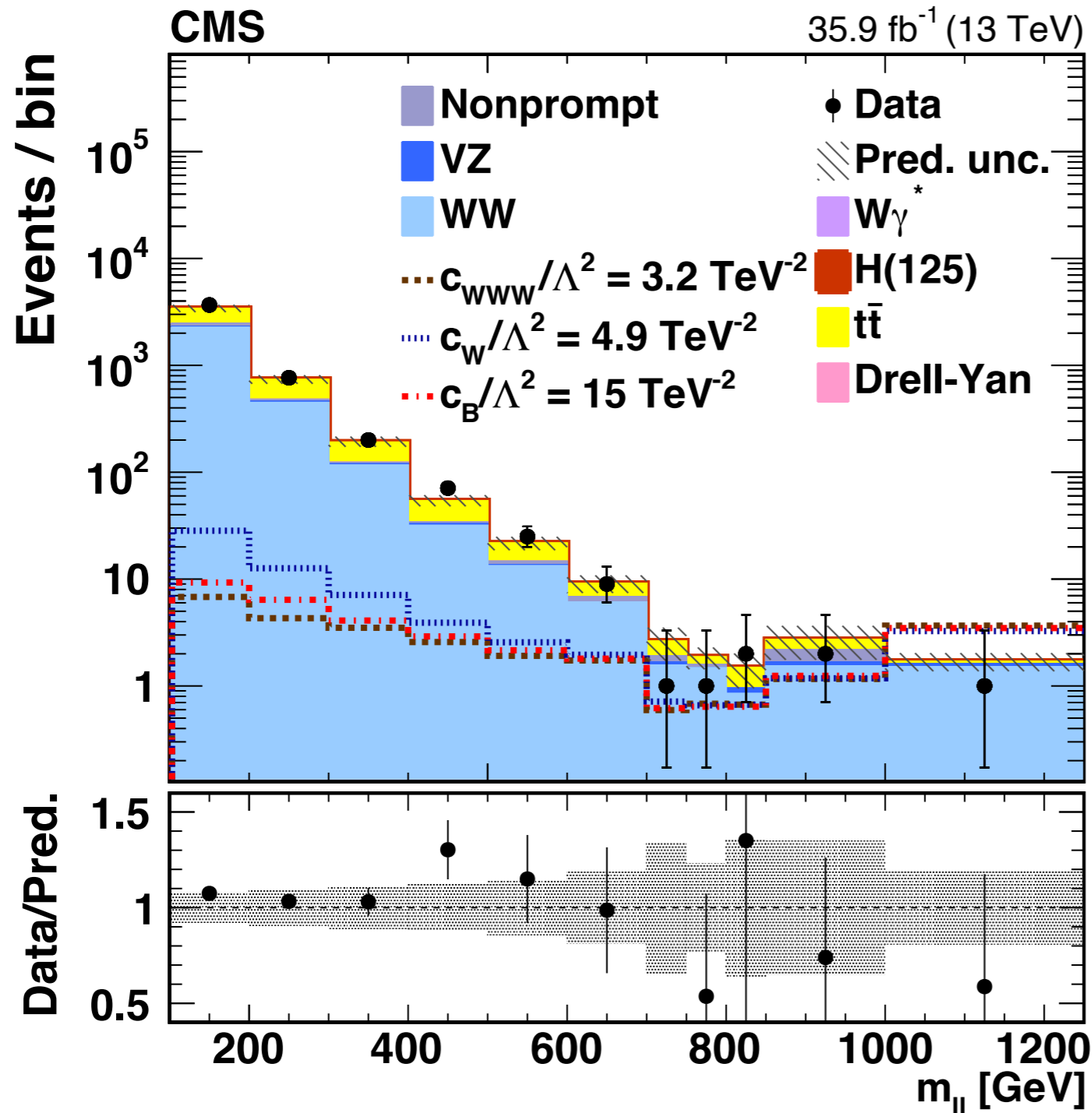
$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{C_i}{\Lambda^2} \mathcal{O}_i^6$$

measure only  $C_i/\Lambda^2$

a finite number of coefficients  
 $\Rightarrow$  Predictive!

- Model independent (i.e. parametrize a large class of models) : any **HEAVY** NP
- SM is the leading term : EFT for precision physics
- higher the exp. precision  $\Rightarrow$  smaller EFT error

# High energy tails



Cross-sections and precision plummet at high energy

EFT/SM is larger at H.E. but so are the EFT errors

2009.00119

# SMEFT and interference

# Errors : higher power of $1/\Lambda$

$$|M(x)|^2 = \underbrace{|M_{SM}(x)|^2}_{\Lambda^0} + \underbrace{2\Re(M_{SM}(x)M_{d6}^*(x))}_{\Lambda^{-2}} + \underbrace{|M_{d6}(x)|^2}_{\mathcal{O}(\Lambda^{-4})} + \dots$$

$\mathcal{O}(1)$                        $\mathcal{O}(0.1)$                        $\mathcal{O}(0.01)$   
 $\mathcal{O}(1)$                        $\mathcal{O}(0.5)$                        $\mathcal{O}(0.25)$

← 10%
→ 50%

- Contains :
  - 1 dim6 insertion squared
  - interference with 2 dim6 insertions
  - interference with 1 dim8 insertion
  - ... at  $1/\Lambda^{-6}$
- Error (estimate)

usually  
not  
included

Dimension 8 basis: Li et al., [2005.00008](#)

# interference suppression

Azatov et al., Helicity Selection Rules and Non-Interference for BSM Amplitudes, [1607.05236](#)

$A_4$	$ h(A_4^{\text{SM}}) $	$ h(A_4^{\text{BSM}}) $
$VVVV$	0	4,2
$VV\phi\phi$	0	2
$VV\psi\psi$	0	2
$V\psi\psi\phi$	0	2

$\psi\psi\psi\psi$	2,0	2,0
$\psi\psi\phi\phi$	0	0
$\phi\phi\phi\phi$	0	0

$$|M(x)|^2 = \underbrace{|M_{SM}(x)|^2}_{\Lambda^0} + \underbrace{2\Re(M_{SM}(x)M_{d6}^*(x))}_{\Lambda^{-2}} + \underbrace{|M_{d6}(x)|^2 + \dots}_{\Lambda^{-4}} + \mathcal{O}(\Lambda^{-6})$$

$\mathcal{O}(1)$                        $\sim 0$                        $\mathcal{O}(0.1)$                        $\mathcal{O}(0.03)$

Assuming  $\sim 0$

# Interference

$$|M(x)|^2 = \underbrace{|M_{SM}(x)|^2}_{\Lambda^0} + \underbrace{2\Re(M_{SM}(x)M_{d6}^*(x))}_{\Lambda^{-2}} + \underbrace{|M_{d6}(x)|^2}_{\mathcal{O}(\Lambda^{-4})} + \dots$$

$$\Re(M_{SM}(x)M_{d6}^*(x)) = \sqrt{|M_{SM}(x)|^2 |M_{d6}(x)|^2} \cos \alpha$$

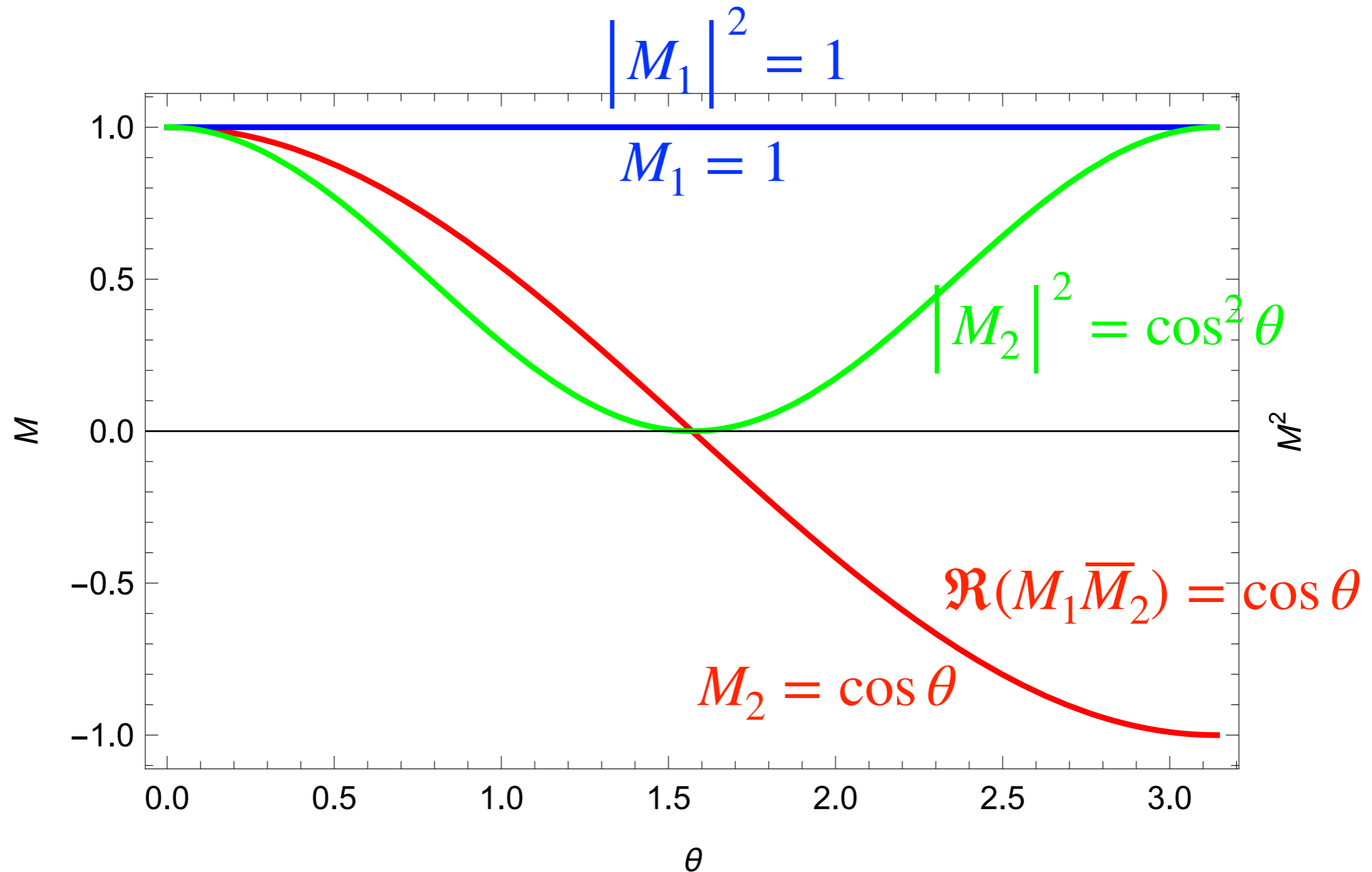
mom&spin Not always positive

Can be suppressed

$$\sigma \propto \sum_x |M(x)|^2 \quad \text{if} \quad \begin{array}{l} M_{SM}(x_1) = 1, M_{SM}(x_2) = \cancel{0} \\ M_{d6}(x_1) = \cancel{0}, M_{d6}(x_2) = 1 \end{array} \quad \sigma_{int} = 0$$

or  $\alpha \approx \pi/2$   $M^2 \rightarrow M^2 - i\Gamma M$   $\sigma_{int} \propto \Gamma$  Observable dependent

# Interference suppression from phase space



$$\sigma_{int} = \int_0^{\pi} 2\Re(M_1 \bar{M}_2) d\theta = \int_0^{\pi} 2 \cos \theta d\theta = 0$$

# Interference revival: Formalism

C.D., M. Maltoni [2012.06595](#)

$$\sigma^{|int|} \equiv \int d\Phi \left| \frac{d\sigma_{int}}{d\Phi} \right| \gg \sigma_{int} \quad = \text{Phase space Suppression}$$

$$\sigma^{|meas|} \equiv \int d\Phi_{meas} \left| \sum_{\{um\}} \frac{d\sigma}{d\Phi} \right| \quad \text{Experimentally accessible?}$$

$$= \lim_{N \rightarrow \infty} \sum_{i=1}^N w_i * \text{sign} \left( \sum_{um} ME(\vec{p}_i, um) \right)$$

Fully:  $\frac{d\sigma_{int}}{d\theta}(pp \rightarrow Z\gamma) \propto \cos \theta$

Not at all:  $\sigma_{int}(\mu_L) = -\sigma_{int}(\mu_R)$

neutrino momenta, helicities, jet flavours, initial parton direction, ...



# CPV in EWdiboson

# dominant CP operators

at the interference level

$m_t \neq 0 \neq m_b$

$(X^3)$		$(\psi^2 \phi^3)$		$(\psi^2 \phi^2 D)$	
$O_{\tilde{G}GG}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$O_{t\phi}$	$(\phi^\dagger \phi)(\bar{q}_3 t \tilde{\phi})$	$O_{\phi tb}$	$i(\tilde{\phi}^\dagger D_\mu \phi)(\bar{t} \gamma^\mu b)$
$O_{\tilde{W}WW}$	$\epsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$O_{b\phi}$	$(\phi^\dagger \phi)(\bar{q}_3 b \phi)$		
$(X^2 \phi^2)$		$(\psi^4)$		$(X \psi^2 \phi)$	
$O_{\phi \tilde{G}}$	$\phi^\dagger \phi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$O_{qtqb}^{(1)}$	$(\bar{q}_3^j t) \epsilon_{jk} (\bar{q}_3^k b)$	$O_{tG}$	$(\bar{q}_3 \sigma^{\mu\nu} T^A t) \tilde{\phi} G_{\mu\nu}^A$
$O_{\phi \tilde{W}}$	$\phi^\dagger \phi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$O_{qtqb}^{(8)}$	$(\bar{q}_3^j T_A t) \epsilon_{jk} (\bar{q}_3^k T_A b)$	$O_{tW}$	$(\bar{q}_3 \sigma^{\mu\nu} t) \tau^I \tilde{\phi} W_{\mu\nu}^I$
$O_{\phi \tilde{B}}$	$\phi^\dagger \phi \tilde{B}_{\mu\nu} B^{\mu\nu}$	<p>if imaginary coefficient</p>		$O_{tB}$	$(\bar{q}_3 \sigma^{\mu\nu} t) \tilde{\phi} B_{\mu\nu}$
$O_{\phi \tilde{W}B}$	$\phi^\dagger \tau^I \phi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$			$O_{bG}$	$(\bar{q}_3 \sigma^{\mu\nu} T^A b) \phi G_{\mu\nu}^A$
				$O_{bW}$	$(\bar{q}_3 \sigma^{\mu\nu} b) \tau^I \phi W_{\mu\nu}^I$
				$O_{bB}$	$(\bar{q}_3 \sigma^{\mu\nu} b) \phi B_{\mu\nu}$

Table 4: List of CP-odd dimension-6 operators in our reduced basis under the  $U(1)^{13}$  symmetry.

C.D., J. Touch  que, [2110.02993](#)  
Bonnefoy et al., [2112.03889](#)

# Basis reduction

If  $b$  is massless,

$$b_R \rightarrow e^{-i\varphi_{bG}} b'_R$$

leaves the SM Lagrangian invariant but

$$e^{i\varphi_{bG}} |C_{bG}| (\bar{Q} \sigma^{\mu\nu} T^A b) \tilde{\phi} G_{\mu\nu}^A \rightarrow |C_{bG}| (\bar{Q} \sigma^{\mu\nu} T^A b') \tilde{\phi} G_{\mu\nu}^A$$

No CP violation from  $C_{bG}$  in the massless  $b$  limit

The relative phase of operators only matter at  $\mathcal{O}(\Lambda^{-4})$

# CPV

neglecting CKM phase

$$\sigma_{int}(C - \text{even}) = 0$$

$$\text{Int } 0 \neq O^{CP\text{-odd}} = 0 \quad \text{SM/dim6}^2$$

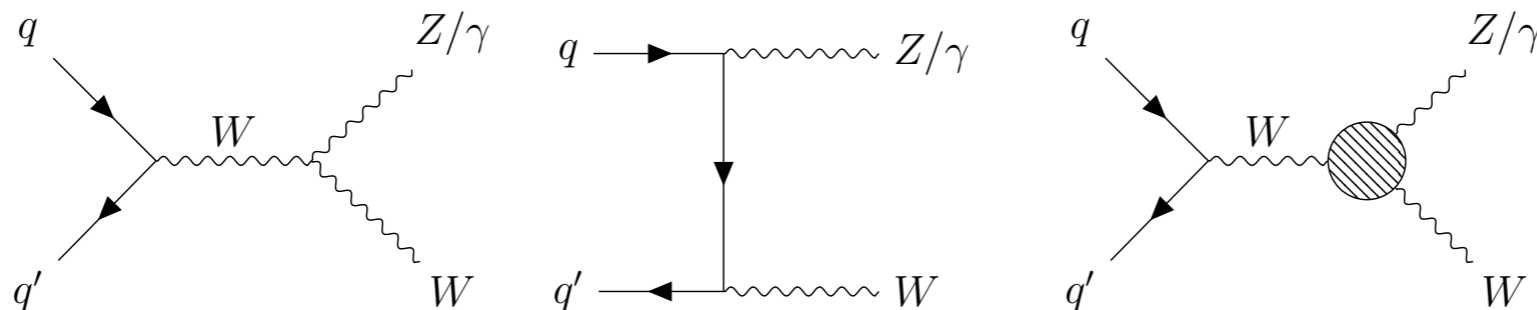
Only visible in distributions

$WZ/\gamma$  are not C-even processes but  $\sigma_{int} \approx 0$

$$O_{SM}^{CP\text{-odd}} \approx 0$$

Large enough cross-sections for accurate differential meas.

Leptonic and mostly visible decays



$$\mathcal{O}_{\widetilde{W}WW}, \mathcal{O}_{\phi\widetilde{W}B}$$

# Interference suppression

Process	$W^+Z \rightarrow \mu^- \mu^+ e^+ \nu_e$	$W^-Z \rightarrow \mu^- \mu^+ e^- \tilde{\nu}_e$
$\sigma(SM)$	15.74(2) fb	9.88(1) fb
$\delta_{PDF}$	3.45%	3.78%
$\sigma(\mathcal{O}_{\tilde{W}WW})$	0.047(4) fb	-0.033(3) fb
Schwartz Bound	16.13 fb	8.85 fb
$\sigma^{int}(\mathcal{O}_{\tilde{W}WW})$	3.302(4) fb	2.028(3) fb
$\sigma^{meas}(\mathcal{O}_{\tilde{W}WW})$	1.084(4) fb	0.634(3) fb
$\sigma_{\Lambda^{-4}}(\mathcal{O}_{\tilde{W}WW})$	4.133(5) fb	1.982(3) fb
$\sigma(\mathcal{O}_{\phi\tilde{W}B})$	0.0086(7) fb	-0.0066(4) fb
Schwartz Bound	1.21 fb	0.76 fb
$\sigma^{int}(\mathcal{O}_{\phi\tilde{W}B})$	0.5467(7) fb	0.3533(4) fb
$\sigma^{meas}(\mathcal{O}_{\phi\tilde{W}B})$	0.1807(7) fb	0.1100(4) fb
$\sigma_{\Lambda^{-4}}(\mathcal{O}_{\phi\tilde{W}B})$	0.0231(3) fb	0.0145(2) fb

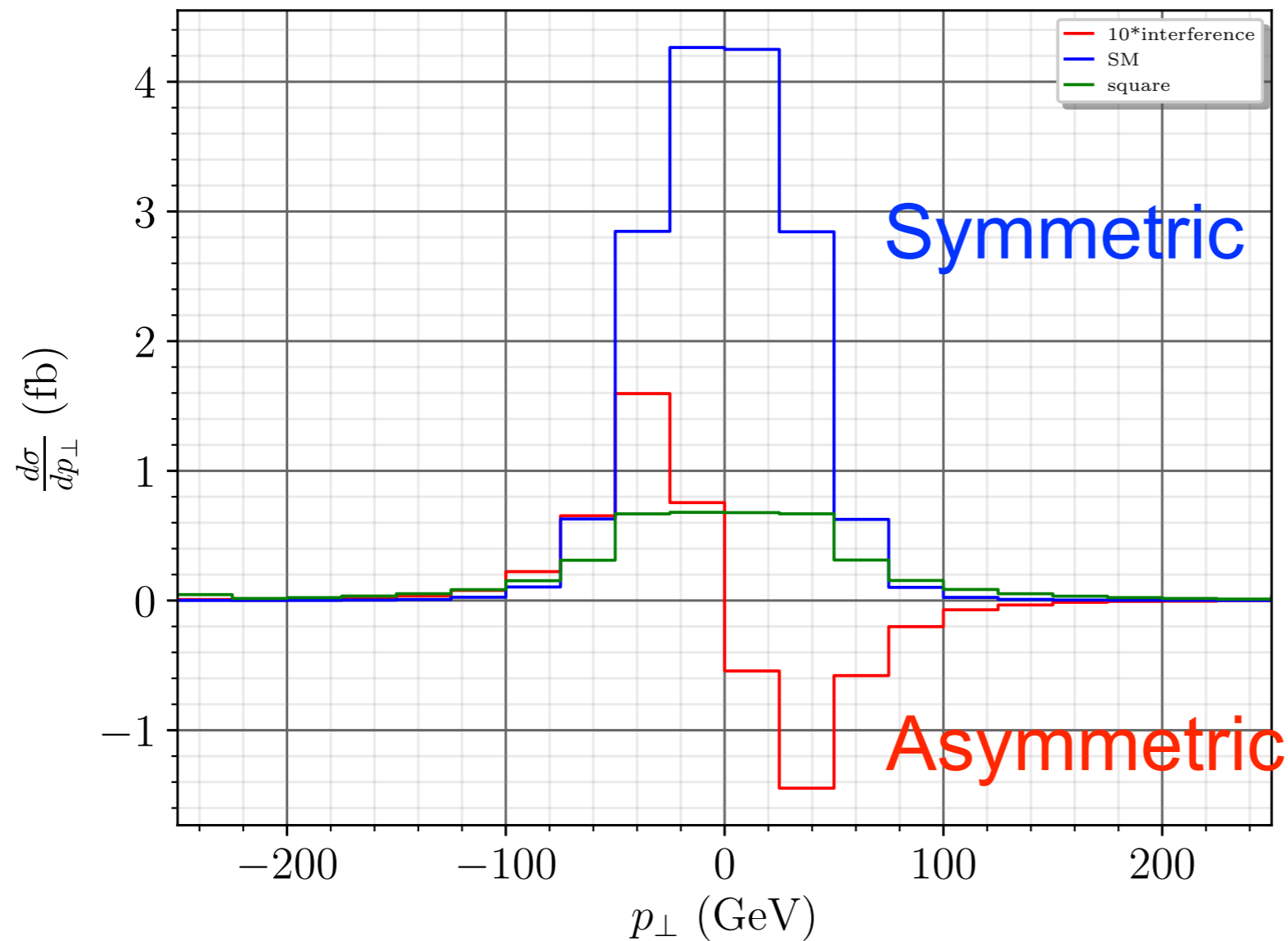
Suppressed  
from phase space

largely available

$$C = 1, \Lambda = 1\text{TeV}$$

# Towards asymmetries

$p p \rightarrow \mu^- \mu^+ e^+ \nu_e$  for  $C_{WW\tilde{W}} = 1$  and  $\Lambda = 1\text{TeV}$  at 13 TEV



$$\vec{p}_e \cdot \frac{(\vec{p}_q \times \vec{p}_Z)}{|\vec{p}_q \times \vec{p}_Z|}$$

# Comparison with other variable

Process	$W^+Z \rightarrow \mu^- \mu^+ e^+ \nu_e$		
Operators	$SM$	$\mathcal{O}_{\tilde{W}WW}$	$\mathcal{O}_{\phi\tilde{W}B}$
$\Delta p_{\perp}(p_e, p_q)$	-0.04(2)	-1.612(4)	-0.3888(7)
$\Delta p_{\perp}(p_e, p_{\Sigma}^z)$	-0.02(2)	-0.628(4)	-0.1207(7)
$\Delta p_{\perp}(p_e, p_e^z)$	0.0(2)	-0.535(4)	-0.1173(7)
$\Delta p_{\perp}(p_e, p_Z^z)$	-0.01(2)	-0.527(4)	-0.0874(7)
$\Delta \sin \phi_{WZ}$	-0.03(2)	-0.321(4)	0.0031(7)
$\Delta (\Delta \phi_{eZ})$	0.07(2)	0.196(4)	0.0688(7)
SM stat err 30 fb <sup>-1</sup>	0.7		
SM stat err 100 fb <sup>-1</sup>	0.4		
SM stat err 3000 fb <sup>-1</sup>	0.07		
Process	$W^-Z \rightarrow \mu^- \mu^+ e^- \tilde{\nu}_e$		
Operators	$SM$	$\mathcal{O}_{\tilde{W}WW}$	$\mathcal{O}_{\phi\tilde{W}B}$
$\Delta p_{\perp}(p_e, p_q)$	-0.08(1)	1.006(3)	0.2522(4)
$\Delta p_{\perp}(p_e, p_{\Sigma}^z)$	-0.03(1)	-0.331(3)	0.0810(4)
$\Delta p_{\perp}(p_e, p_e^z)$	-0.01(1)	0.295(3)	0.0514(4)
$\Delta p_{\perp}(p_e, p_Z^z)$	0.00(1)	0.295(3)	0.0627(4)
$\Delta \sin \phi_{WZ}$	-0.02(1)	-0.190(3)	0.0013(4)
$\Delta (\Delta \phi_{eZ})$	-0.05(1)	0.022(3)	0.0109(4)
SM stat err 30 fb <sup>-1</sup>	0.6		
SM stat err 100 fb <sup>-1</sup>	0.3		
SM stat err 3000 fb <sup>-1</sup>	0.06		

knowing the quark direction

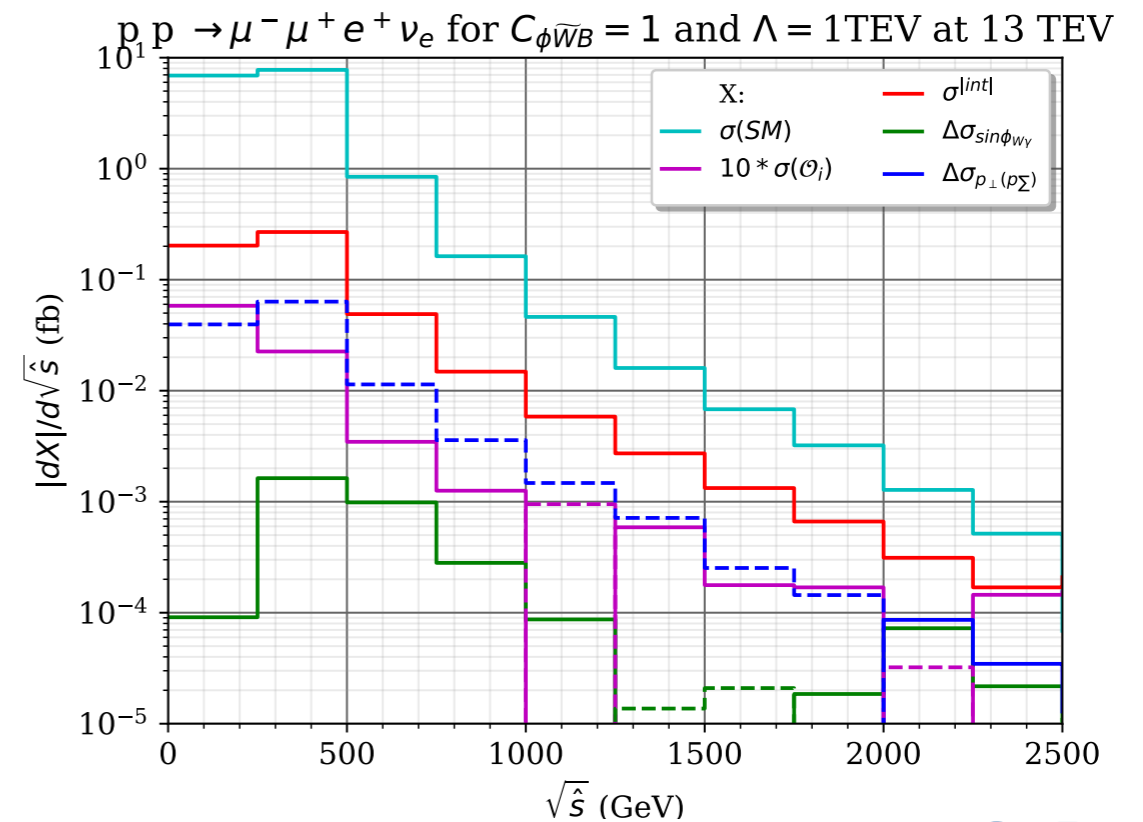
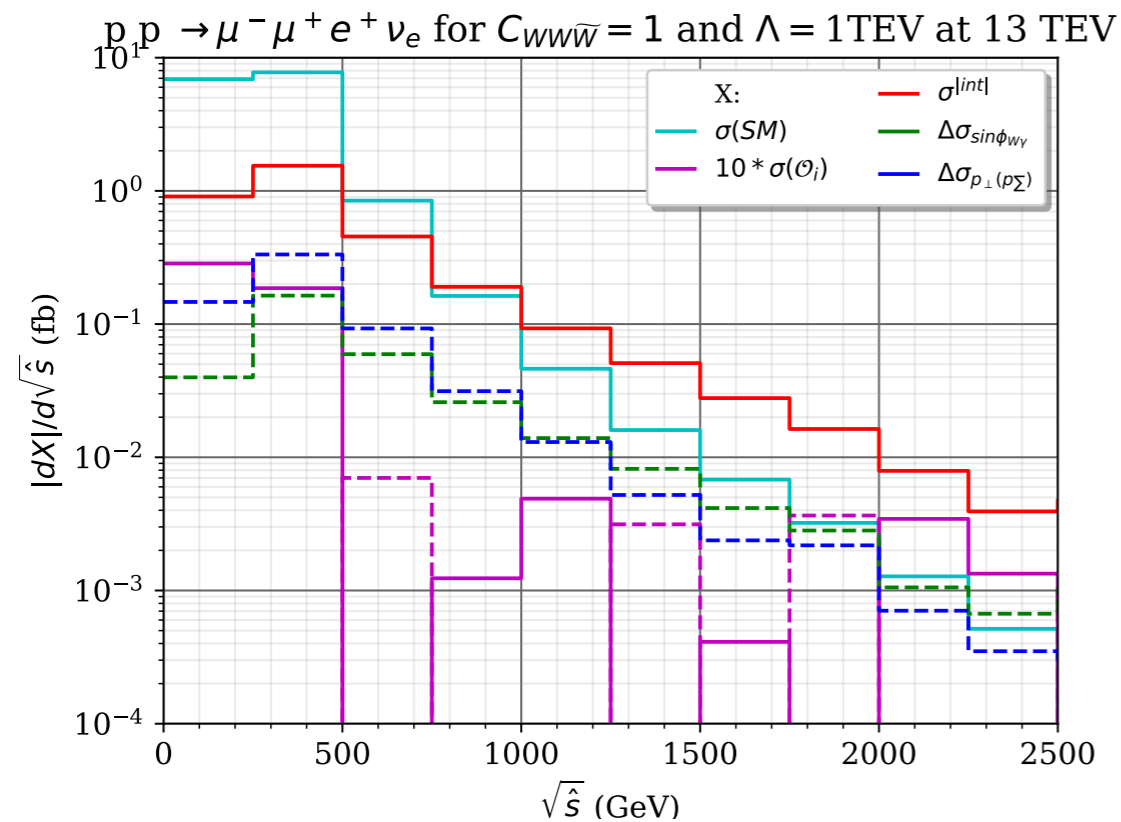
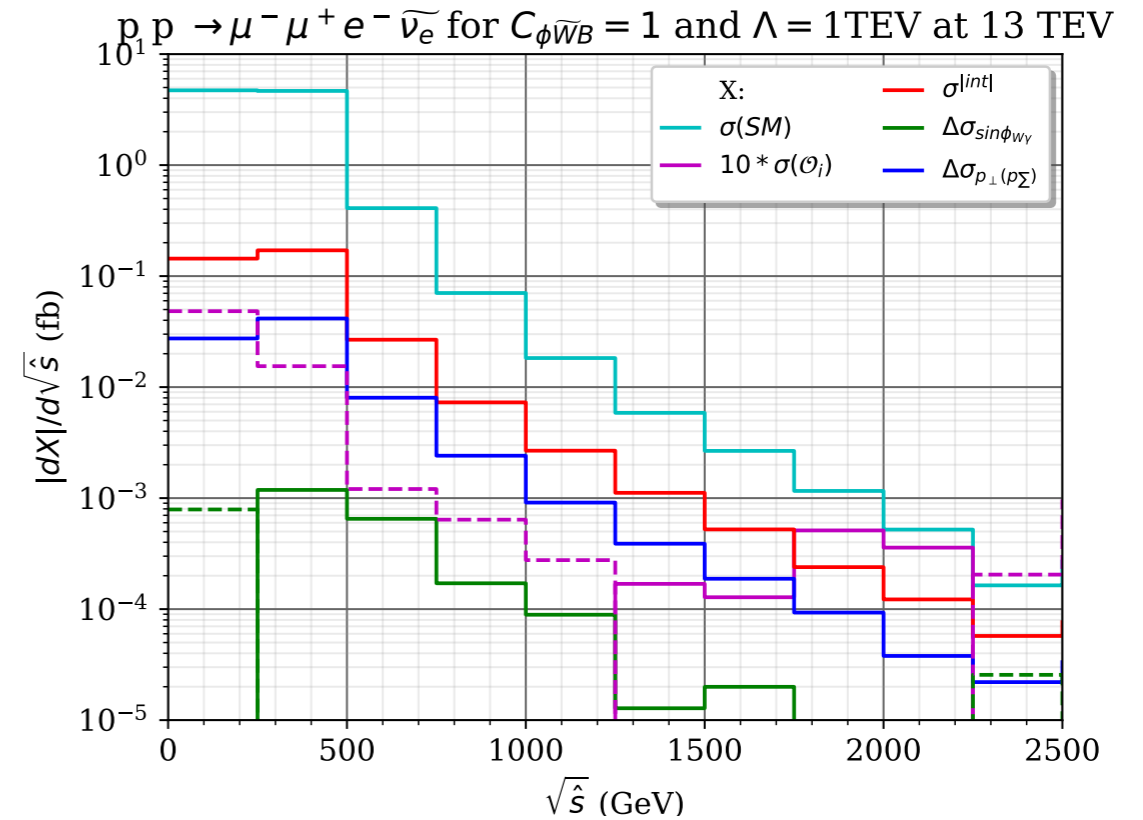
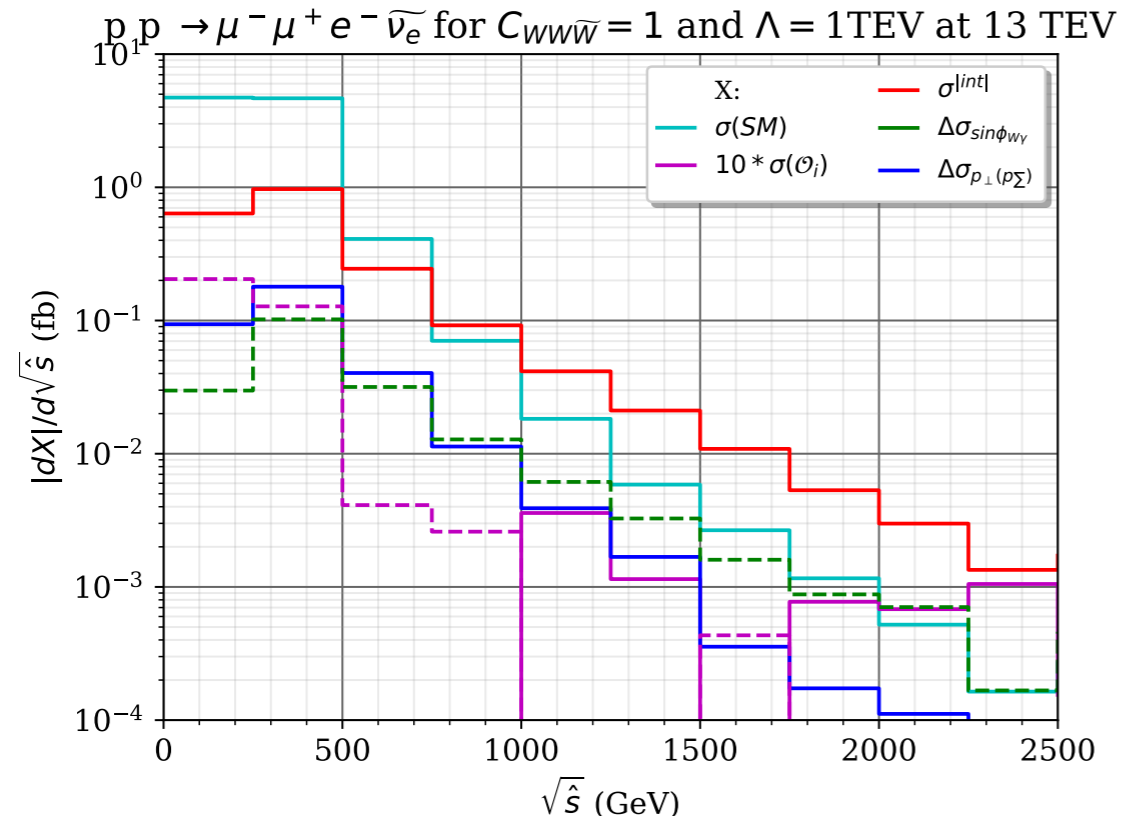
50-70% efficiency

80-90% in  $W\gamma$

Better than HE observables

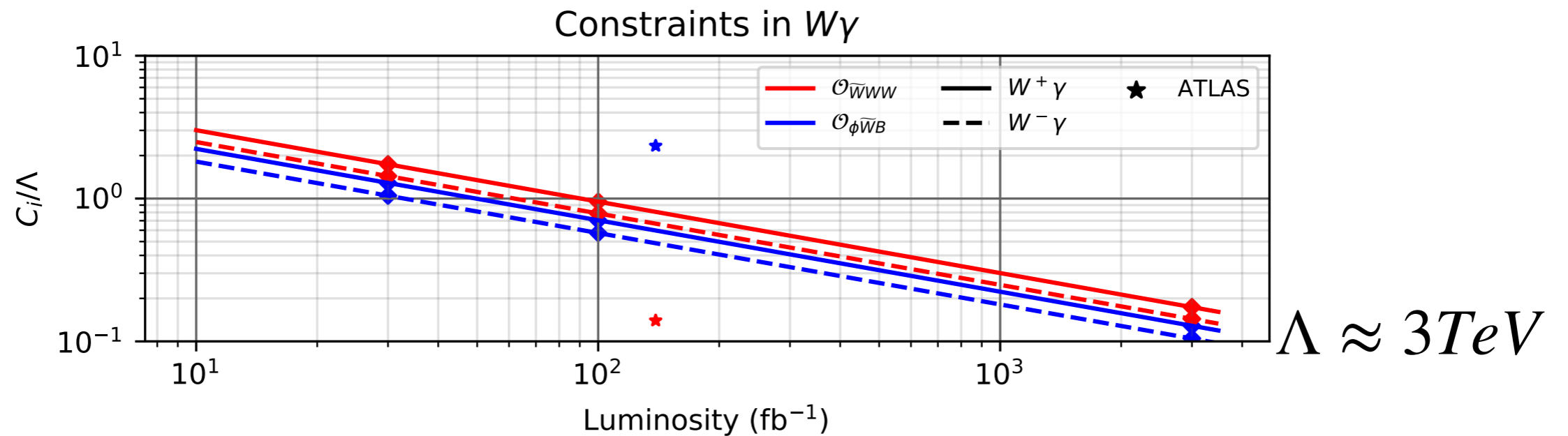
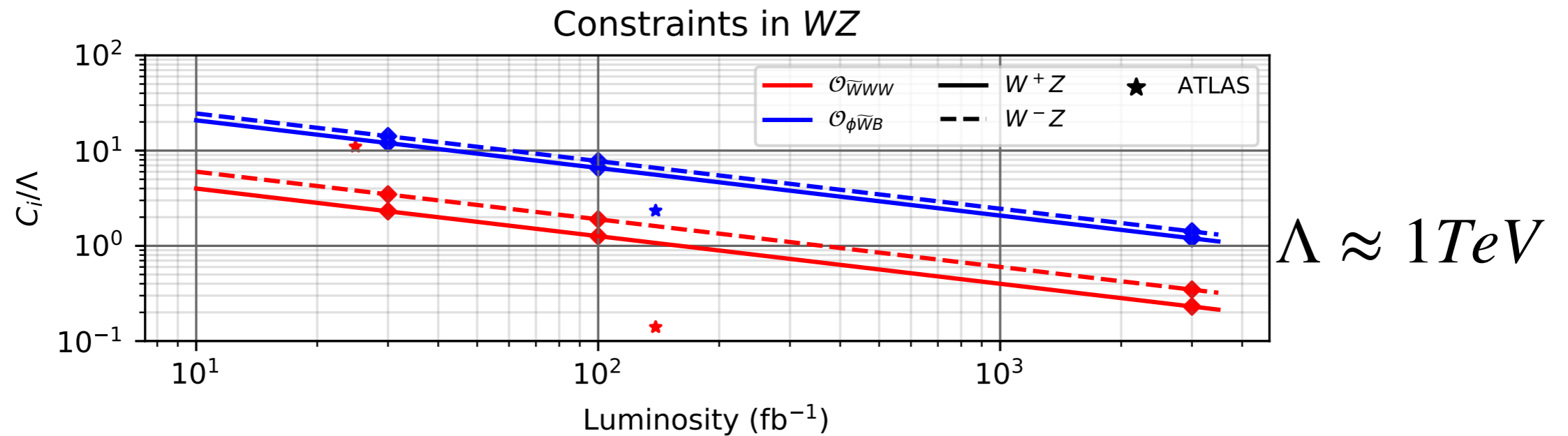
$\approx 0$

# HE behaviour





# Constraints



EFT validity & Errors  $\sim (0.2\text{TeV}/1\text{TeV})^2 \sim 4\%$

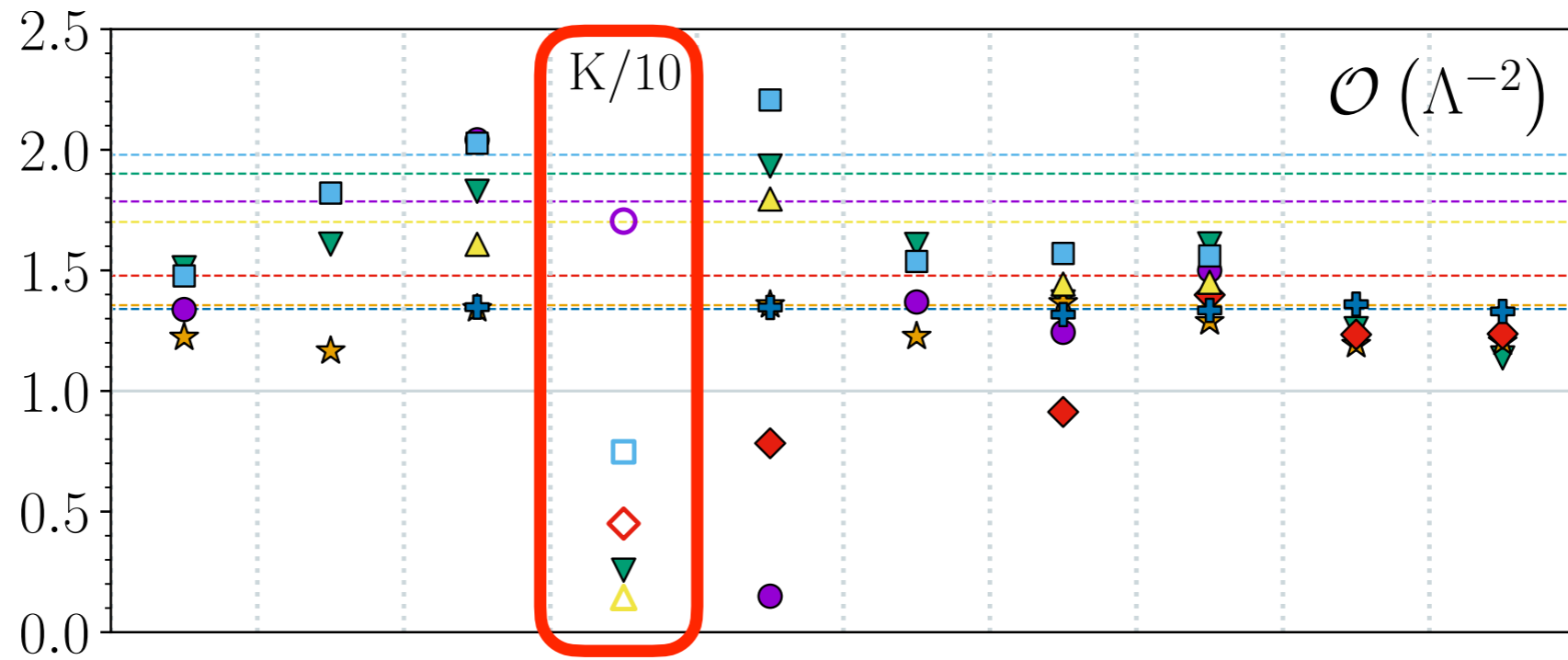
Bulk vs small HE tail

Keeping uncertainties under control

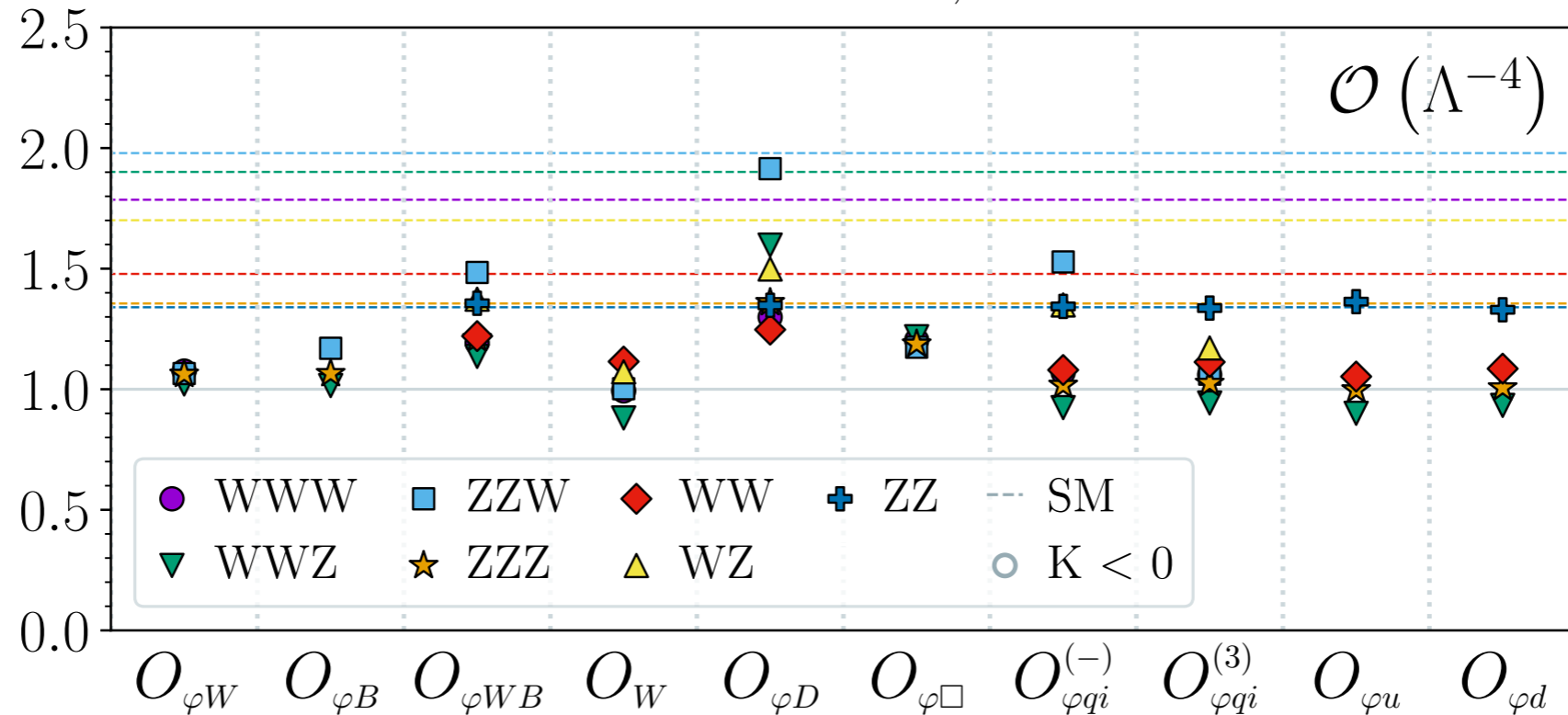
# EW bosons production

Large  
negative  
K-factors

Converge?

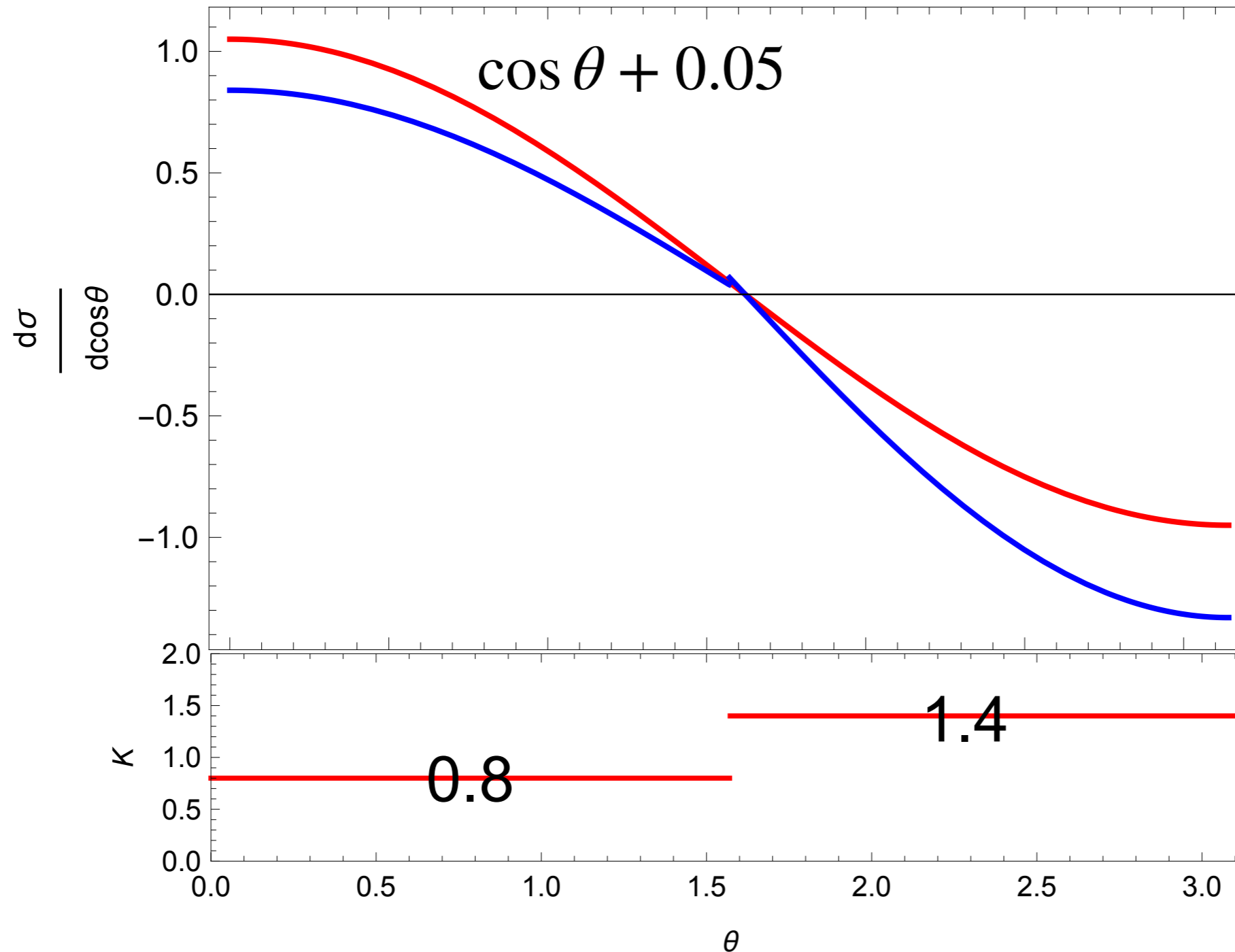


Multi-boson K-factors, LHC 13 TeV



SMEFT@NLO  
2008.11743

# Large/small K-factor



$$\sigma_{int}^{LO} = 0.16$$

$$\sigma_{int}^{NLO} = -0.43$$

$$K_{\sigma} \approx -3$$

Uncertainty

$\sigma$  is not the right variable to probe the interference

# Interference revival: toy example

$$A = d\sigma(\cos \theta > 0) - d\sigma(\cos \theta < 0)$$

$$A_{int}^{LO} = 2 \qquad \gg \sigma_{int}^{LO} = 0.16$$

$$A_{int}^{NLO} = 2.15$$

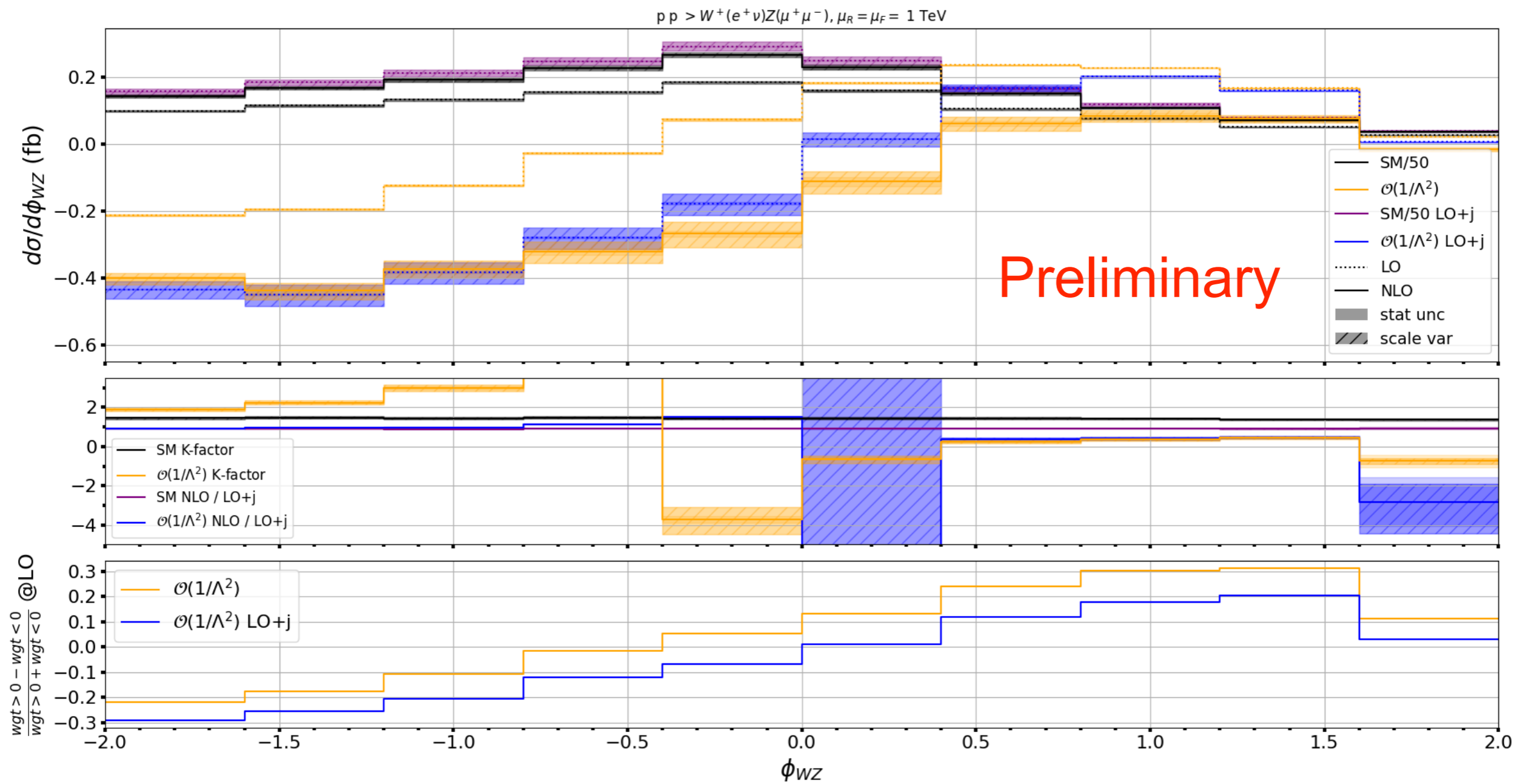
$$K_A = 1.1$$

No/little cancellation

(Much) larger sensitivity

Less sensitive to corrections (smaller errors)

# O<sub>www</sub>



with M. Maltoni

Dim-8 in diboson

# dim-8 operators

$$\mathcal{O}_1 = iB^\mu{}_\nu B^\nu{}_\lambda (\bar{d}_{Rp} \gamma^\lambda \overleftrightarrow{D}_\mu d_{Rr}),$$

$$\mathcal{O}_2 = iB^\mu{}_\nu B^\nu{}_\lambda (\bar{u}_{Rp} \gamma^\lambda \overleftrightarrow{D}_\mu u_{Rr}),$$

$$\mathcal{O}_3 = iB^\mu{}_\nu B^\nu{}_\lambda (\bar{q}_{Lp} \gamma^\lambda \overleftrightarrow{D}_\mu q_{Lr}),$$

$$\mathcal{O}_4 = iW^{I\mu}{}_\lambda B^{\nu\lambda} (\bar{q}_{Lp}^i \gamma_\nu (\tau^I)_i{}^j \overleftrightarrow{D}_\mu q_{Lrj}),$$

$$\mathcal{O}_5 = iW^{I\mu}{}_\lambda \tilde{B}^{\nu\lambda} (\bar{q}_{Lp}^i \gamma_\nu (\tau^I)_i{}^j \overleftrightarrow{D}_\mu q_{Lrj}),$$

$$\mathcal{O}_6 = iW^{I\nu}{}_\lambda B^{\mu\lambda} (\bar{q}_{Lp}^i \gamma_\nu (\tau^I)_i{}^j \overleftrightarrow{D}_\mu q_{Lrj}),$$

$$\mathcal{O}_7 = iW^{I\nu}{}_\lambda \tilde{B}^{\mu\lambda} (\bar{q}_{Lp}^i \gamma_\nu (\tau^I)_i{}^j \overleftrightarrow{D}_\mu q_{Lrj}),$$

$$\mathcal{O}_8 = iW^{I\mu}{}_\nu W^{I\nu}{}_\lambda (\bar{d}_{Rp} \gamma^\lambda \overleftrightarrow{D}_\mu d_{Rr}),$$

$$\mathcal{O}_9 = iW^{I\mu}{}_\nu W^{I\nu}{}_\lambda (\bar{u}_{Rp} \gamma^\lambda \overleftrightarrow{D}_\mu u_{Rr}),$$

$$\mathcal{O}_{10} = iW^{I\mu}{}_\nu W^{I\nu}{}_\lambda (\bar{q}_{Lr} \gamma^\lambda \overleftrightarrow{D}_\mu q_{Lp}),$$

$$\mathcal{O}_{11} = i\epsilon^{IJK} W^{I\mu}{}_\nu W^{J\nu}{}_\lambda (\bar{q}_{Lp}^i \gamma^\lambda (\tau^K)_i{}^j \overleftrightarrow{D}_\mu q_{Lrj}),$$

$$\mathcal{O}_{12} = i\epsilon^{IJK} \tilde{W}^{I\mu}{}_\nu W^{J\nu}{}_\lambda (\bar{q}_{Lp}^i \gamma^\lambda (\tau^K)_i{}^j \overleftrightarrow{D}_\mu q_{Lrj}),$$

$$\mathcal{O}_{13} = i\epsilon^{IJK} W^{I\mu}{}_\nu \tilde{W}^{J\nu}{}_\lambda (\bar{q}_{Lp}^i \gamma^\lambda (\tau^K)_i{}^j \overleftrightarrow{D}_\mu q_{Lrj}),$$

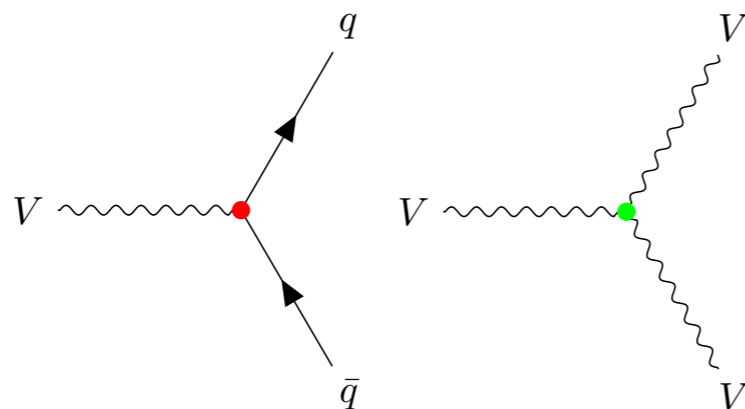
$$\mathcal{O}_{14} = i (\bar{u}_{Rr} \gamma^\lambda \overleftrightarrow{D}_\mu u_{Rp}) (D_\lambda H^\dagger D^\mu H),$$

$$\mathcal{O}_{15} = i (\bar{d}_{Rr} \gamma^\lambda \overleftrightarrow{D}_\mu d_{Rp}) (D_\lambda H^\dagger D^\mu H),$$

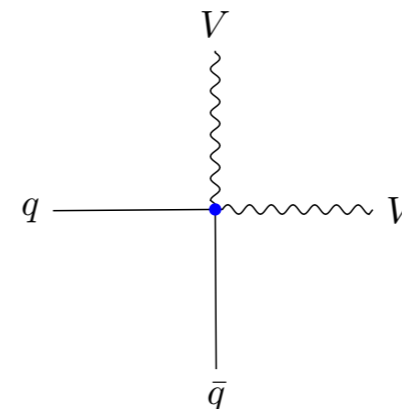
$$\mathcal{O}_{16} = i (\bar{q}_{Lr} \gamma^\lambda \overleftrightarrow{D}_\mu q_{Lp}) (D_\lambda H^\dagger D^\mu H),$$

$$\mathcal{O}_{17} = i (\bar{q}_{Lp} \gamma^\lambda \tau^K \overleftrightarrow{D}_\mu q_{Lr}) (D_\lambda H^\dagger \tau^K D^\mu H),$$

$$\mathcal{O}_{18} = i (\bar{u}_{Rp} \gamma^\mu \overleftrightarrow{D}^\nu d_{Rr}) \epsilon^{ij} (D^\mu H_i D^\nu H_j),$$



(a) dim-6 vertex corrections



(b) dim-8 contact corrections

CD, H.-L. Li, [2303.10493](#)



# Interference behaviour

Operator	$2 \text{Re}(\mathcal{A}^{\text{SM}} \mathcal{A}^{\text{NP}*})$	$2 \int d\Omega \text{Re}(\mathcal{A}^{\text{SM}} \mathcal{A}^{\text{NP}*})$
$\mathcal{O}_8$	$d\bar{d} : b_8 S + c_8$	0
$\mathcal{O}_9$	$\bar{u}u : b_9 S + c_9$	0
$\mathcal{O}_{10}$	$u\bar{u}/d\bar{d} : a_{10} \cdot S^2 + b_{10} \cdot S + c_{10}$	$u\bar{u}/d\bar{d} : \bar{a}_{10} \cdot S^2 + \bar{b}_{10} \cdot S + \bar{c}_{10}$
$\mathcal{O}_{11}$	0	0
$\mathcal{O}_{12}$	$u\bar{u} : a_{12}^u S^2 + b_{12}^u S + c_{12}^u$	$u\bar{u} : \bar{a}_{12}^u S^2 + \bar{b}_{12}^u S + \bar{c}_{12}^u + \bar{D}_{12}^u \log S$
	$d\bar{d} : a_{12}^d S^2 + b_{12}^d S + c_{12}^d$	$d\bar{d} : \bar{a}_{12}^d S^2 + \bar{b}_{12}^d S + \bar{c}_{12}^d + \bar{D}_{12}^d \log S$
$\mathcal{O}_{13}$	$u\bar{u} : a_{13}^u S^2 + b_{13}^u S + c_{13}^u$	$u\bar{u} : \bar{a}_{13}^u S^2 + \bar{b}_{13}^u S + \bar{c}_{13}^u + \bar{D}_{13}^u \log S$
	$d\bar{d} : a_{13}^d S^2 + b_{13}^d S + c_{13}^d$	$d\bar{d} : \bar{a}_{13}^d S^2 + \bar{b}_{13}^d S + \bar{c}_{13}^d + \bar{D}_{13}^d \log S$
$\mathcal{O}_{14}$	$u\bar{u} : a_{14} S^2 + b_{14} S + c_{14}$	0
$\mathcal{O}_{15}$	$d\bar{d} : a_{15} S^2 + b_{15} S + c_{15}$	0
$\mathcal{O}_{16}$	$u\bar{u} : a_{16}^u S^2 + b_{16}^u S + c_{16}^u$	$u\bar{u} : \bar{b}_{16}^u S + \bar{c}_{16}^u + \bar{D}_{16}^u \log S$
	$d\bar{d} : a_{16}^d S^2 + b_{16}^d S + c_{16}^d$	$d\bar{d} : \bar{b}_{16}^d S + \bar{c}_{16}^d + \bar{D}_{16}^d \log S$
$\mathcal{O}_{17}$	$u\bar{u} : a_{17}^u S^2 + b_{17}^u S + c_{17}^u$	$u\bar{u} : \bar{b}_{17}^u S + \bar{c}_{17}^u + \bar{D}_{17}^u \log S$
	$d\bar{d} : a_{17}^d S^2 + b_{17}^d S + c_{17}^d$	$d\bar{d} : \bar{b}_{17}^d S + \bar{c}_{17}^d + \bar{D}_{17}^d \log S$

CPV

Asymmetric

**Table 2:** Scaling of  $q\bar{q} \rightarrow WW$  interference amplitude after summing and averaging over spins and helicities.

# Interference by helicity ( $\mathcal{O}_8$ )

$(h_{W^+}, h_{W^-})$	$\mathcal{A}_{h_i}^8 / \frac{C_8}{\Lambda^4}$	$\mathcal{A}_{h_i}^{\text{SM}}$	
$-, +$	$S^2 S \sin^2\left(\frac{\theta}{2}\right) \sin(\theta) (S - 2M_W^2) \delta_{ab}$	0	$S^0$
$-, -$	$S S \sin(\theta) \cos(\theta) M_W^2 \delta_{ab}$	$\frac{4\pi\alpha \sin(\theta) M_Z^2 \delta_{ab} \sqrt{1 - \frac{4M_W^2}{S}}}{3(S - M_Z^2)}$	$S^{-1}$
$-, 0$	$S^{3/2} \frac{\sin^2\left(\frac{\theta}{2}\right) (2\cos(\theta) + 1) M_W^2 \delta_{ab}}{\sqrt{2}M_W}$	$\frac{4\pi\alpha \sin^2\left(\frac{\theta}{2}\right) M_Z^2 \delta_{ab} \sqrt{2S - 8M_W^2}}{3SM_W - 3M_W M_Z^2}$	$S^{-1/2}$
$+, +$	$S S \sin(\theta) \cos(\theta) M_W^2 \delta_{ab}$	$\frac{4\pi\alpha \sin(\theta) M_Z^2 \delta_{ab} \sqrt{1 - \frac{4M_W^2}{S}}}{3(S - M_Z^2)}$	$S^{-1}$
$+, -$	$S^2 2S \sin\left(\frac{\theta}{2}\right) \cos^3\left(\frac{\theta}{2}\right) \delta_{ab} (S - 2M_W^2)$	0	$S^0$
$+, 0$	$S^{3/2} \frac{\cos^2\left(\frac{\theta}{2}\right) (2\cos(\theta) - 1) M_W^2 \delta_{ab}}{\sqrt{2}M_W}$	$\frac{4\pi\alpha \cos^2\left(\frac{\theta}{2}\right) M_Z^2 \delta_{ab} \sqrt{2S - 8M_W^2}}{3SM_W - 3M_W M_Z^2}$	$S^{-1/2}$
$0, +$	$S^{3/2} \frac{\sin^2\left(\frac{\theta}{2}\right) (2\cos(\theta) + 1) M_W^2 \delta_{ab}}{\sqrt{2}M_W}$	$\frac{4\sqrt{2}\pi\alpha \sin^2\left(\frac{\theta}{2}\right) M_Z^2 \delta_{ab} \sqrt{S - 4M_W^2}}{3M_W M_Z^2 - 3SM_W}$	$S^{-1/2}$
$0, -$	$S^{3/2} \frac{\cos^2\left(\frac{\theta}{2}\right) (1 - 2\cos(\theta)) M_W^2 \delta_{ab}}{\sqrt{2}M_W}$	$\frac{4\sqrt{2}\pi\alpha \cos^2\left(\frac{\theta}{2}\right) M_Z^2 \delta_{ab} \sqrt{S - 4M_W^2}}{3M_W M_Z^2 - 3SM_W}$	$S^{-1/2}$
$0, 0$	$S -S \sin 2\theta M_W^2 \delta_{ab}$	$\frac{2\pi\alpha \sin(\theta) M_Z^2 \delta_{ab} (2M_W^2 + S) \sqrt{1 - \frac{4M_W^2}{S}}}{3M_W^2 (M_Z^2 - S)}$	$S^0$

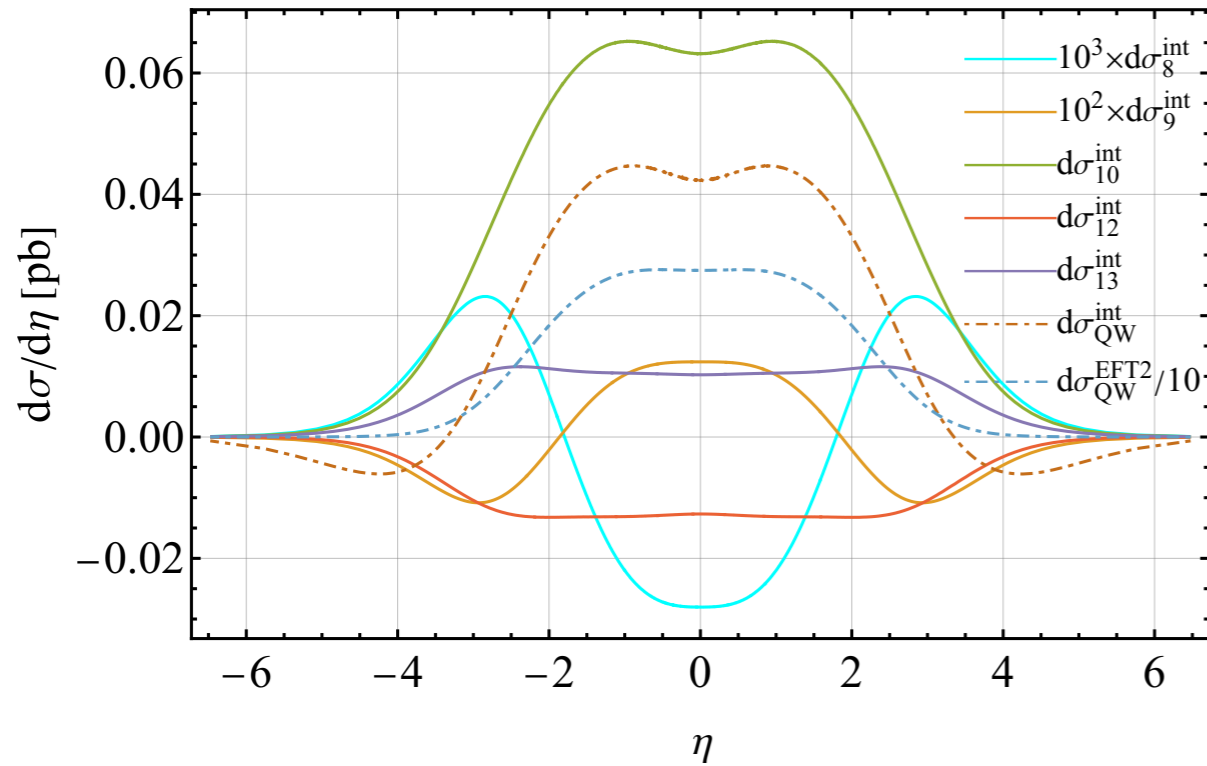
**Table 3:** Helicity amplitudes for  $d\bar{d} \rightarrow WW$  for  $h_d = 1$  and  $h_{\bar{d}} = -1$ , where  $\mathcal{A}_{h_i}^8$  is generated by  $\mathcal{O}_8$ .

# Interference by helicity ( $O_{15}$ )

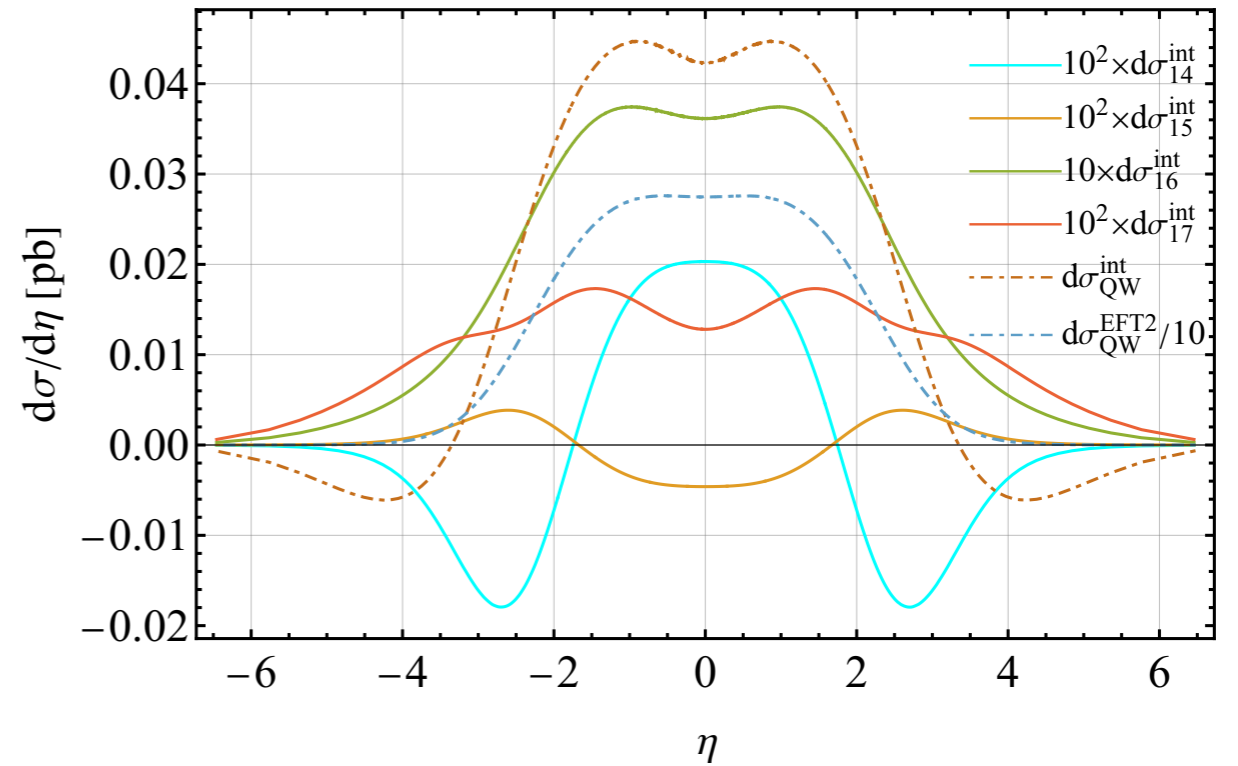
$(h_{W^+}, h_{W^-})$	$\mathcal{A}_{h_i}^{15} / \frac{C_{15}}{\Lambda^4}$	$\mathcal{A}_{h_i}^{\text{SM}}$	
$-, +$	$S \sin^2\left(\frac{\theta}{2}\right) \sin(\theta) M_W^2 \delta_{ab}$	0	
$-, -$	$S - S \sin^2\left(\frac{\theta}{2}\right) \sin(\theta) M_W^2 \delta_{ab}$	$\frac{4\pi\alpha \sin(\theta) M_Z^2 \delta_{ab} \sqrt{1 - \frac{4M_W^2}{S}}}{3(S - M_Z^2)}$	$S^{-1}$
$-, 0$	$S^{3/2} \frac{\sin^2\left(\frac{\theta}{2}\right) \cos(\theta) M_W \delta_{ab}}{\sqrt{2}}$	$\frac{4\pi\alpha \sin^2\left(\frac{\theta}{2}\right) M_Z^2 \delta_{ab} \sqrt{2S - 8M_W^2}}{3SM_W - 3M_W M_Z^2}$	$S^{-1/2}$
$+, +$	$S \sin(\theta) \cos^2\left(\frac{\theta}{2}\right) M_W^2 \delta_{ab}$	$\frac{4\pi\alpha \sin(\theta) M_Z^2 \delta_{ab} \sqrt{1 - \frac{4M_W^2}{S}}}{3(S - M_Z^2)}$	$S^{-1}$
$+, -$	$S - S \sin(\theta) \cos^2\left(\frac{\theta}{2}\right) M_W^2 \delta_{ab}$	0	
$+, 0$	$S^{3/2} \frac{\cos^2\left(\frac{\theta}{2}\right) \cos(\theta) M_W \delta_{ab}}{\sqrt{2}}$	$\frac{4\pi\alpha \cos^2\left(\frac{\theta}{2}\right) M_Z^2 \delta_{ab} \sqrt{2S - 8M_W^2}}{3SM_W - 3M_W M_Z^2}$	$S^{-1/2}$
$0, +$	$S^{3/2} \frac{-\sin^2(\theta) M_W \delta_{ab}}{2\sqrt{2}}$	$\frac{4\sqrt{2}\pi\alpha \sin^2\left(\frac{\theta}{2}\right) M_Z^2 \delta_{ab} \sqrt{S - 4M_W^2}}{3M_W M_Z^2 - 3SM_W}$	$S^{-1/2}$
$0, -$	$S^{3/2} \frac{\sin^2(\theta) M_W \delta_{ab}}{2\sqrt{2}}$	$\frac{4\sqrt{2}\pi\alpha \cos^2\left(\frac{\theta}{2}\right) M_Z^2 \delta_{ab} \sqrt{S - 4M_W^2}}{3M_W M_Z^2 - 3SM_W}$	$S^{-1/2}$
$0, 0$	$S^2 - \frac{1}{8} S^2 \sin(2\theta) \delta_{ab}$	$\frac{2\pi\alpha \sin(\theta) M_Z^2 \delta_{ab} (2M_W^2 + S) \sqrt{1 - \frac{4M_W^2}{S}}}{3M_W^2 (M_Z^2 - S)}$	$S^0$

# Distributions

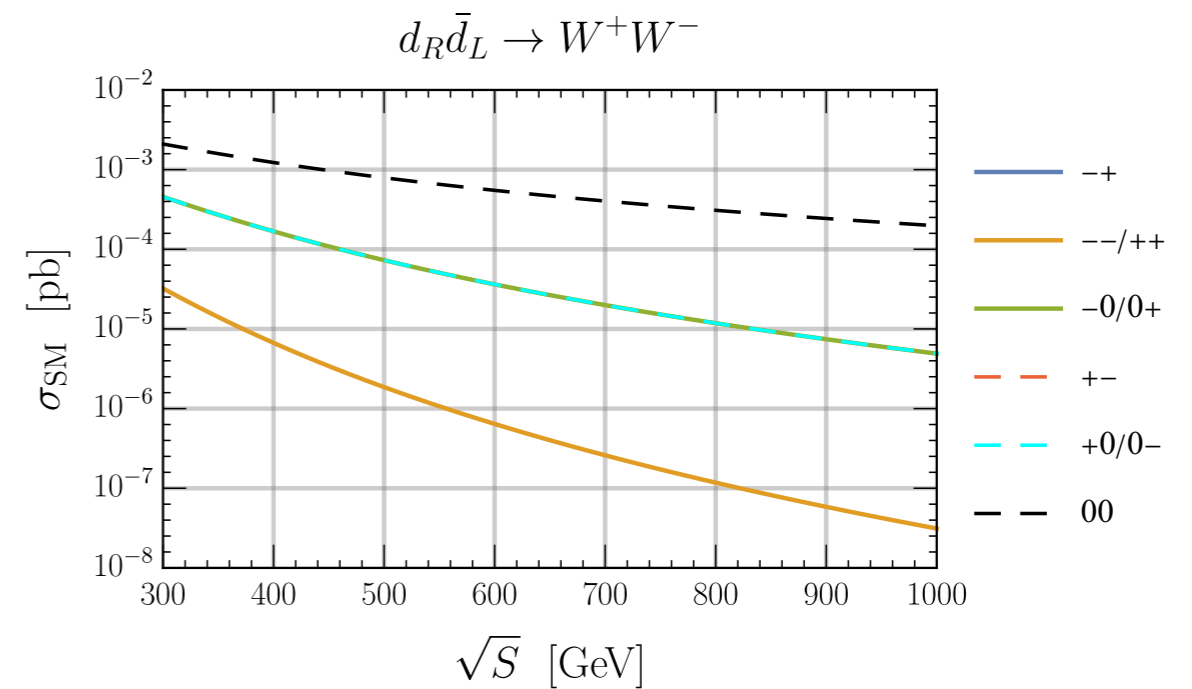
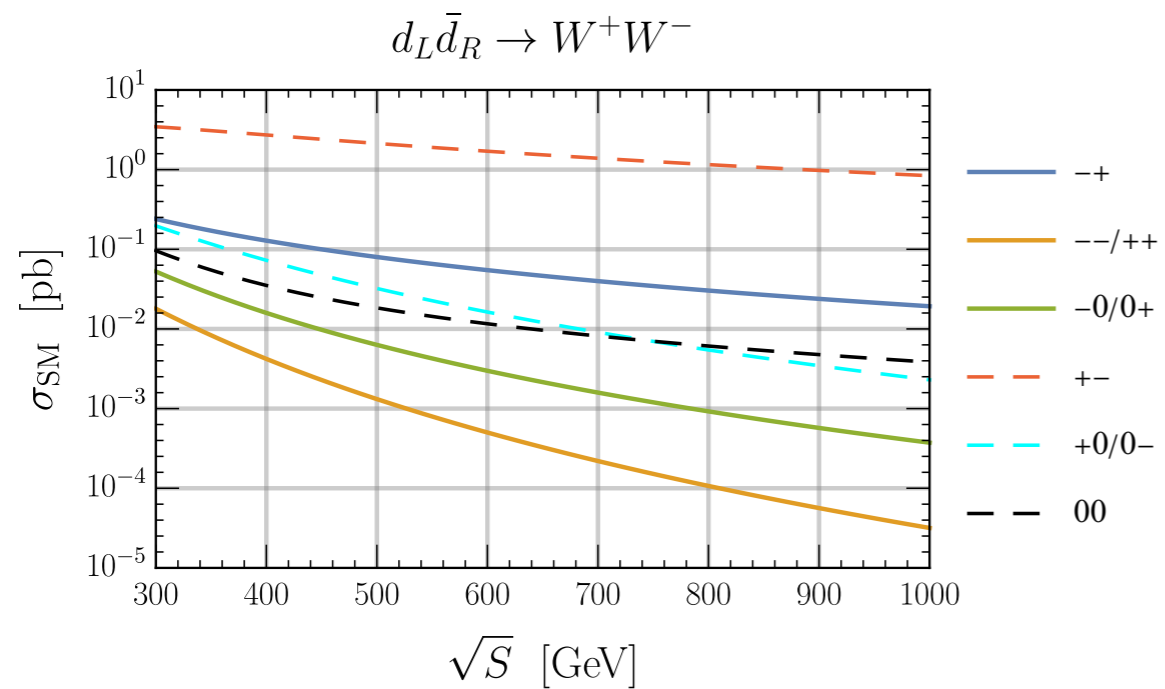
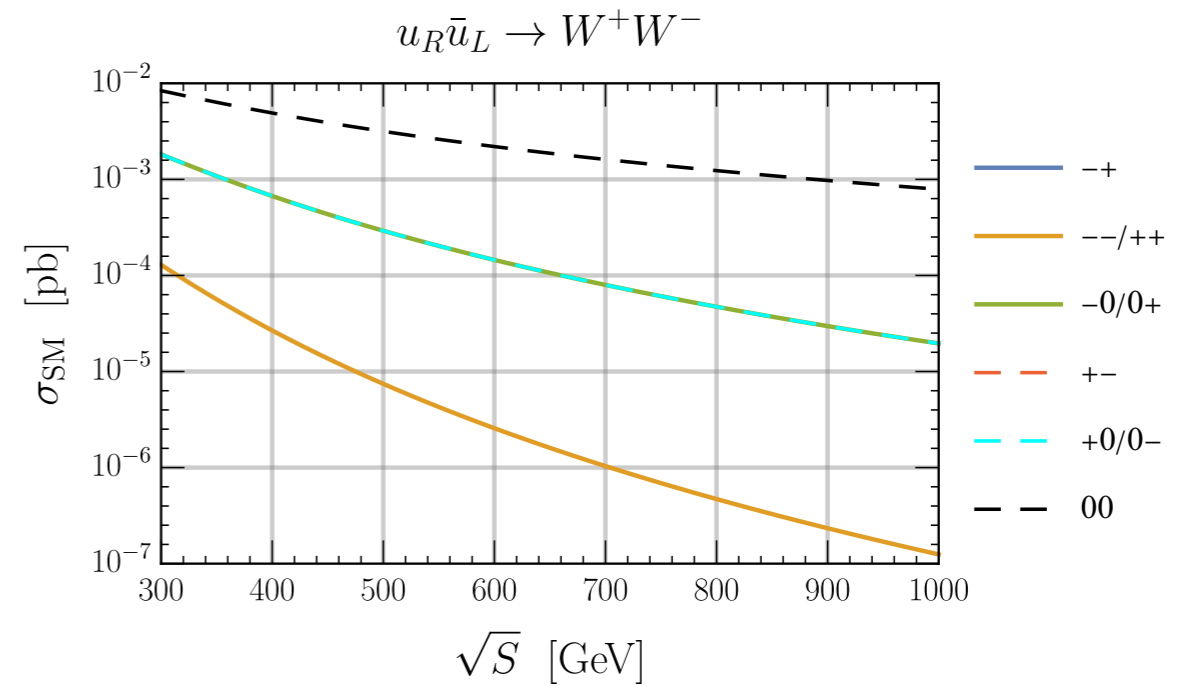
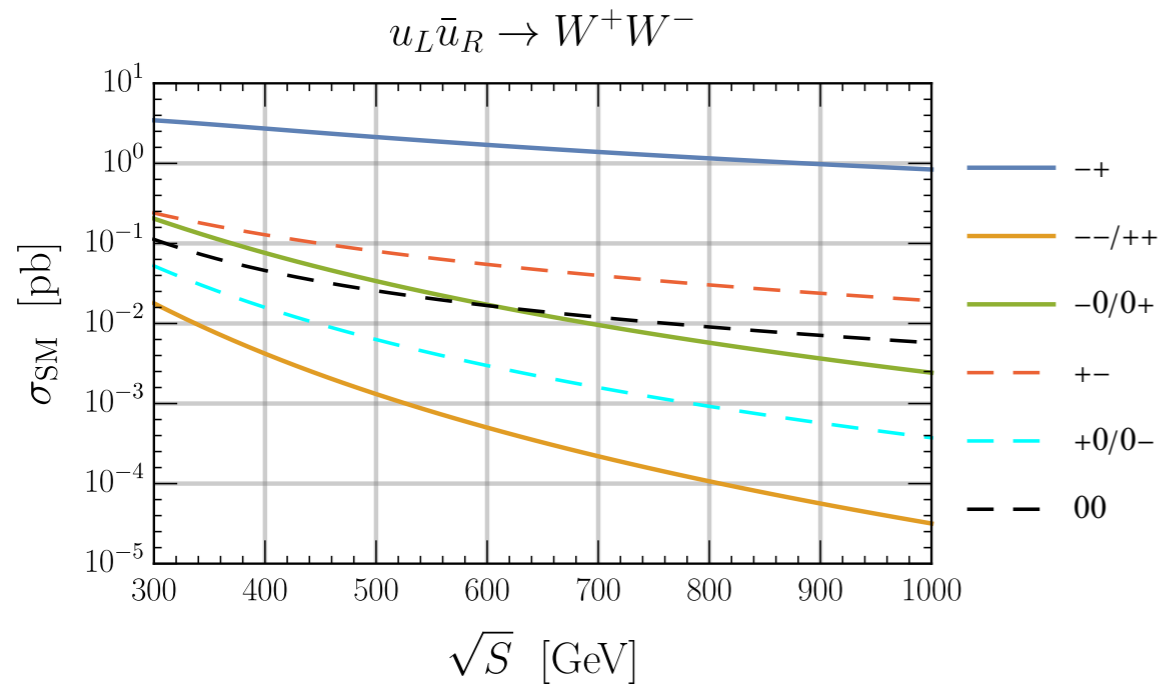
$pp \rightarrow W^+W^-$ ,  $s=14$  TeV,  $\Lambda=1$  TeV,  $C_i=1$   
 $\hat{s}_{\min}=300$  GeV,  $\hat{s}_{\max}=700$  GeV



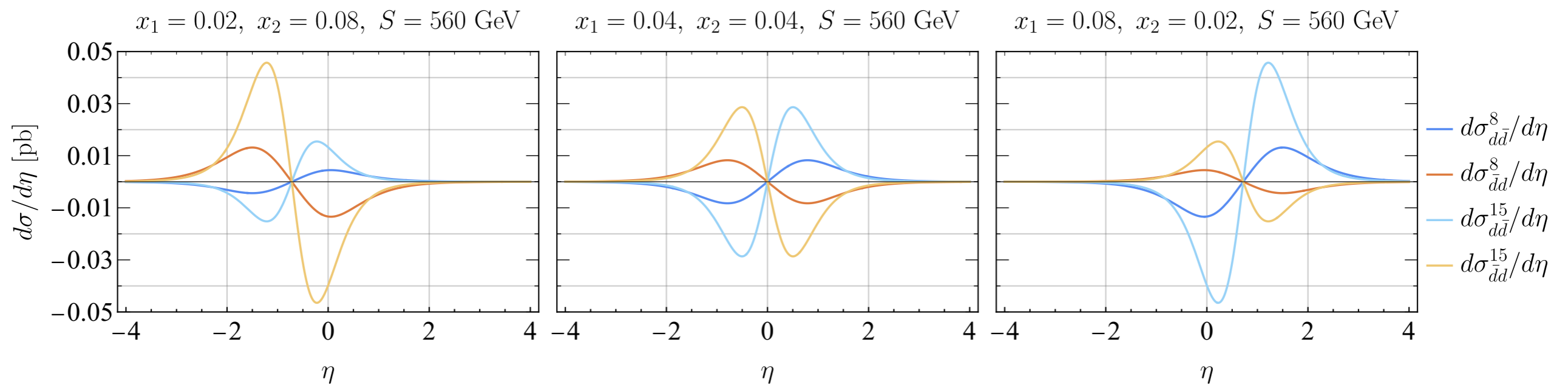
$pp \rightarrow W^+W^-$ ,  $s=14$  TeV,  $\Lambda=1$  TeV,  $c_i=1$   
 $\hat{s}_{\min}=300$  GeV,  $\hat{s}_{\max}=700$  GeV



# SM Parton level

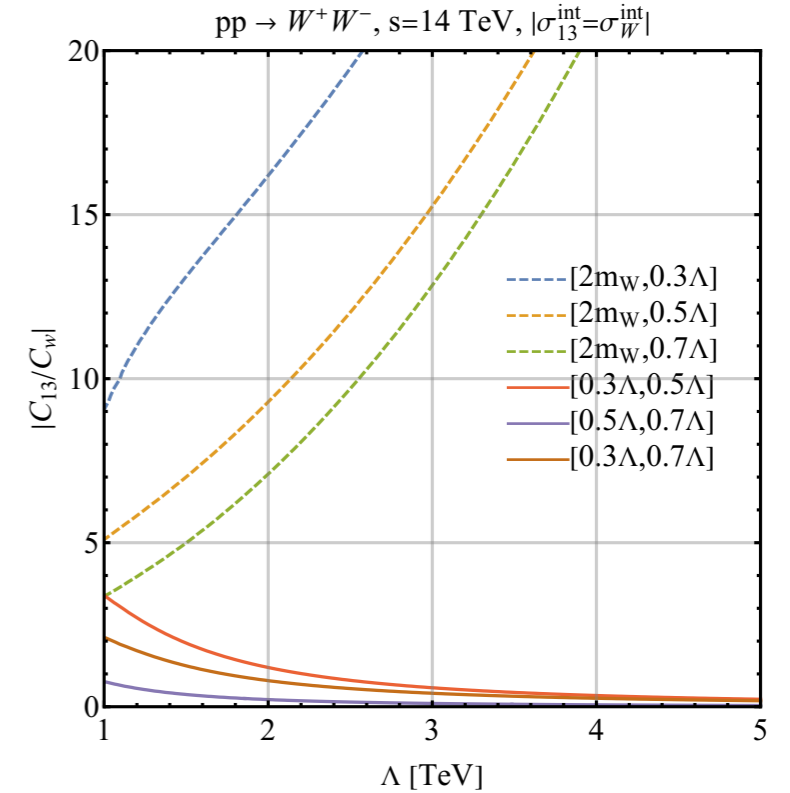
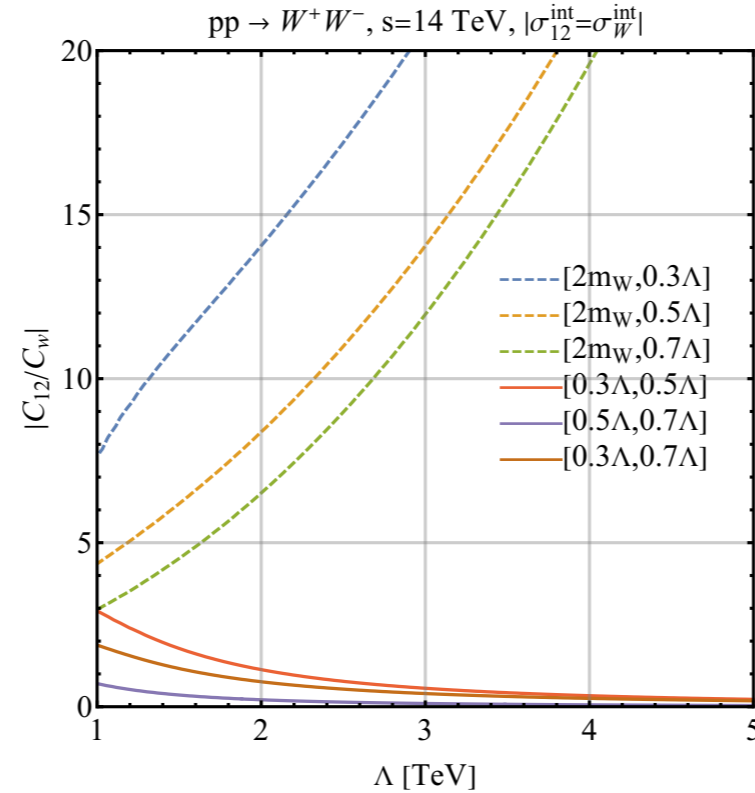
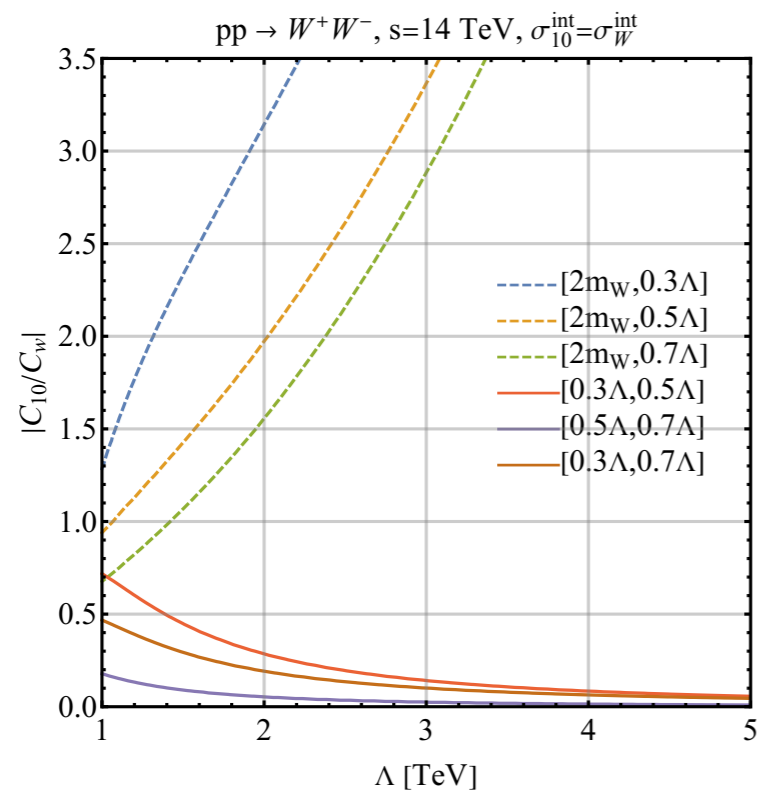
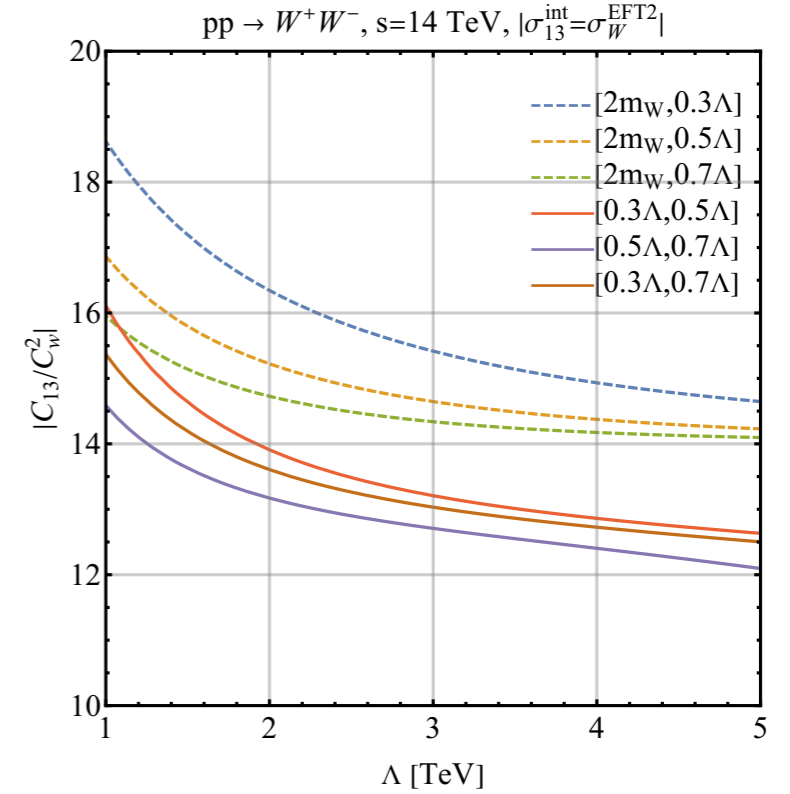
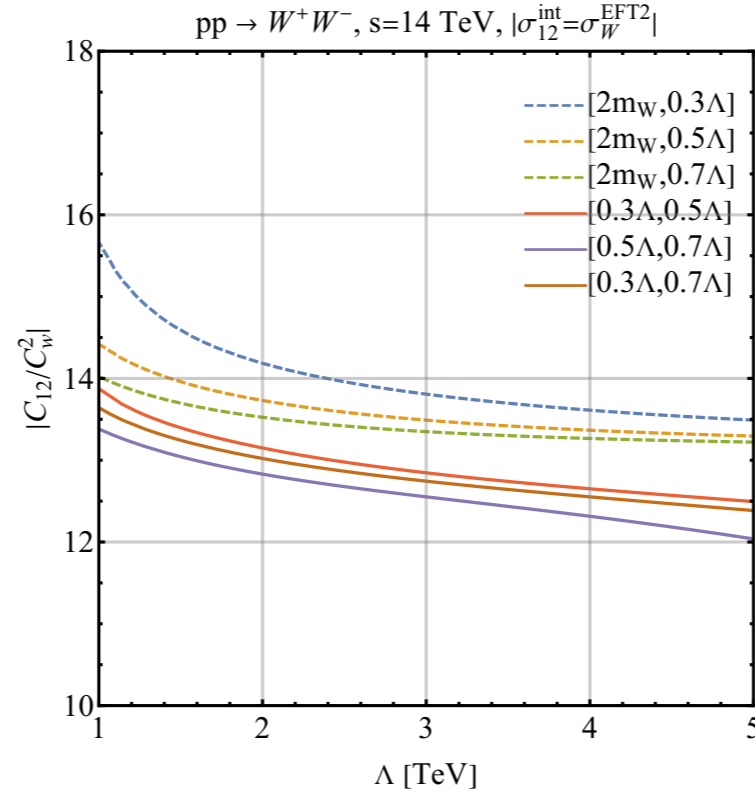
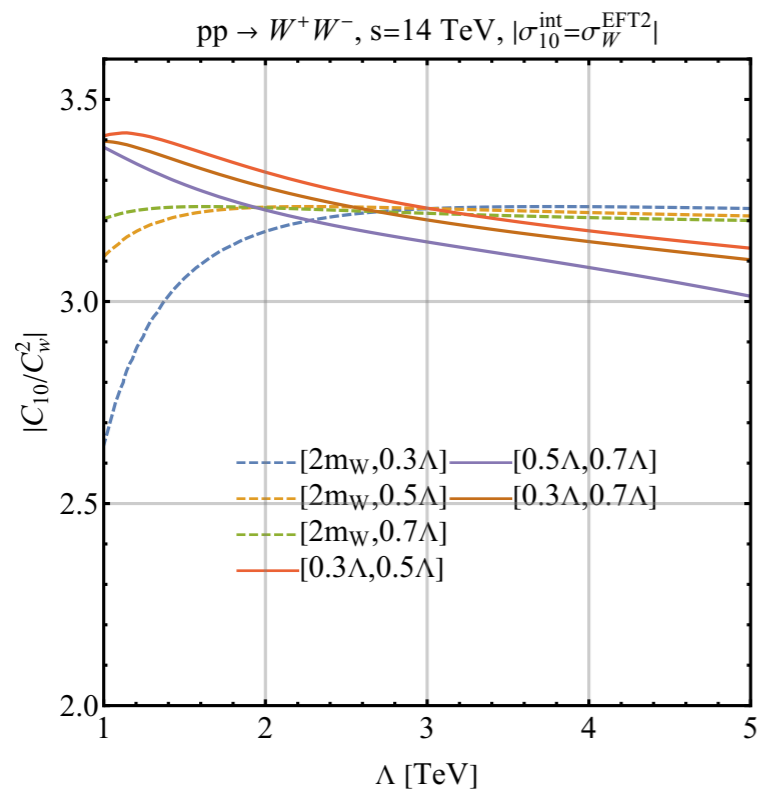


# LHC symmetry cancellation

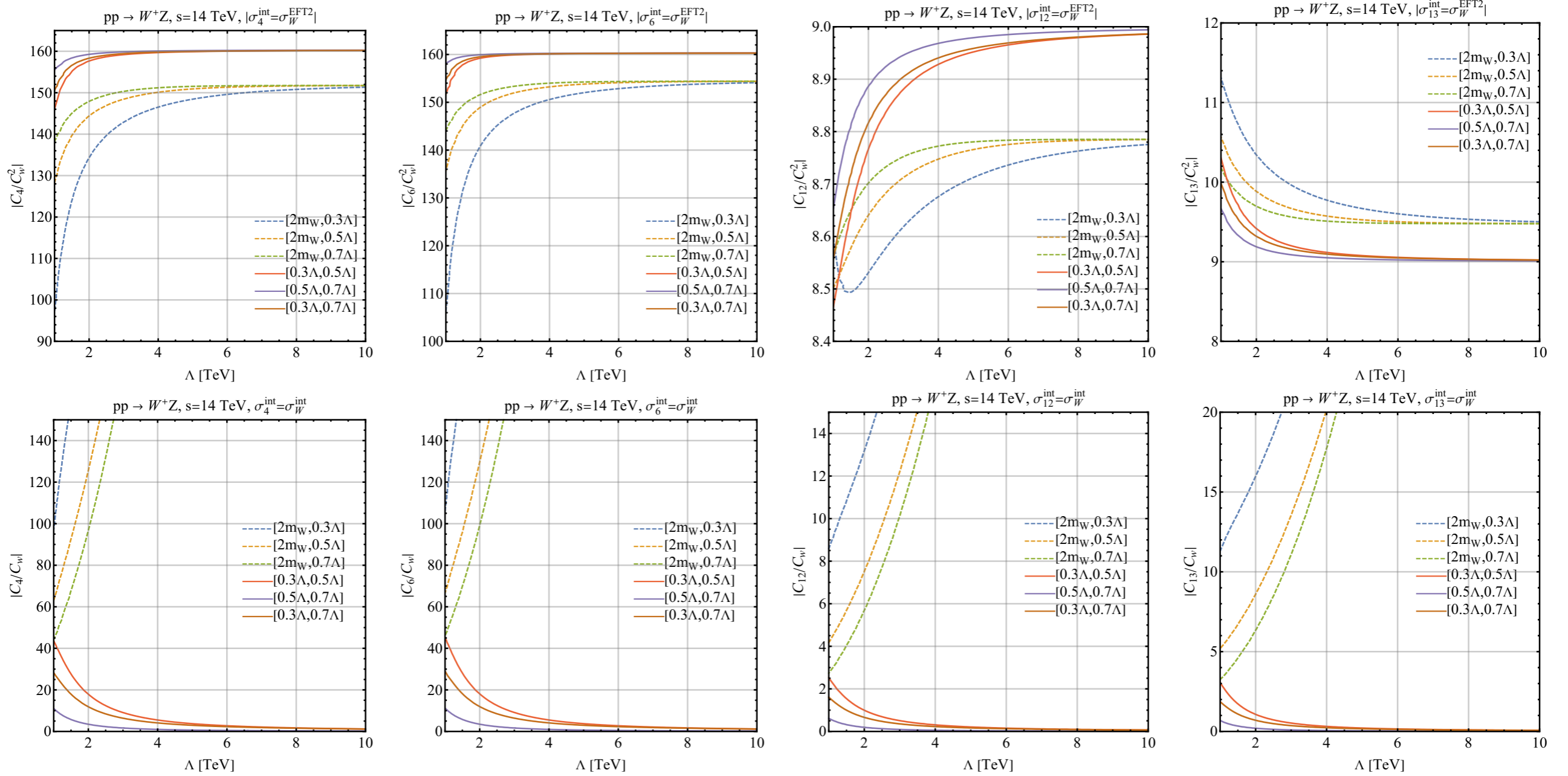


Not present at lepton colliders

# Comparison to dim6



# WZ





Further comments

# Comments

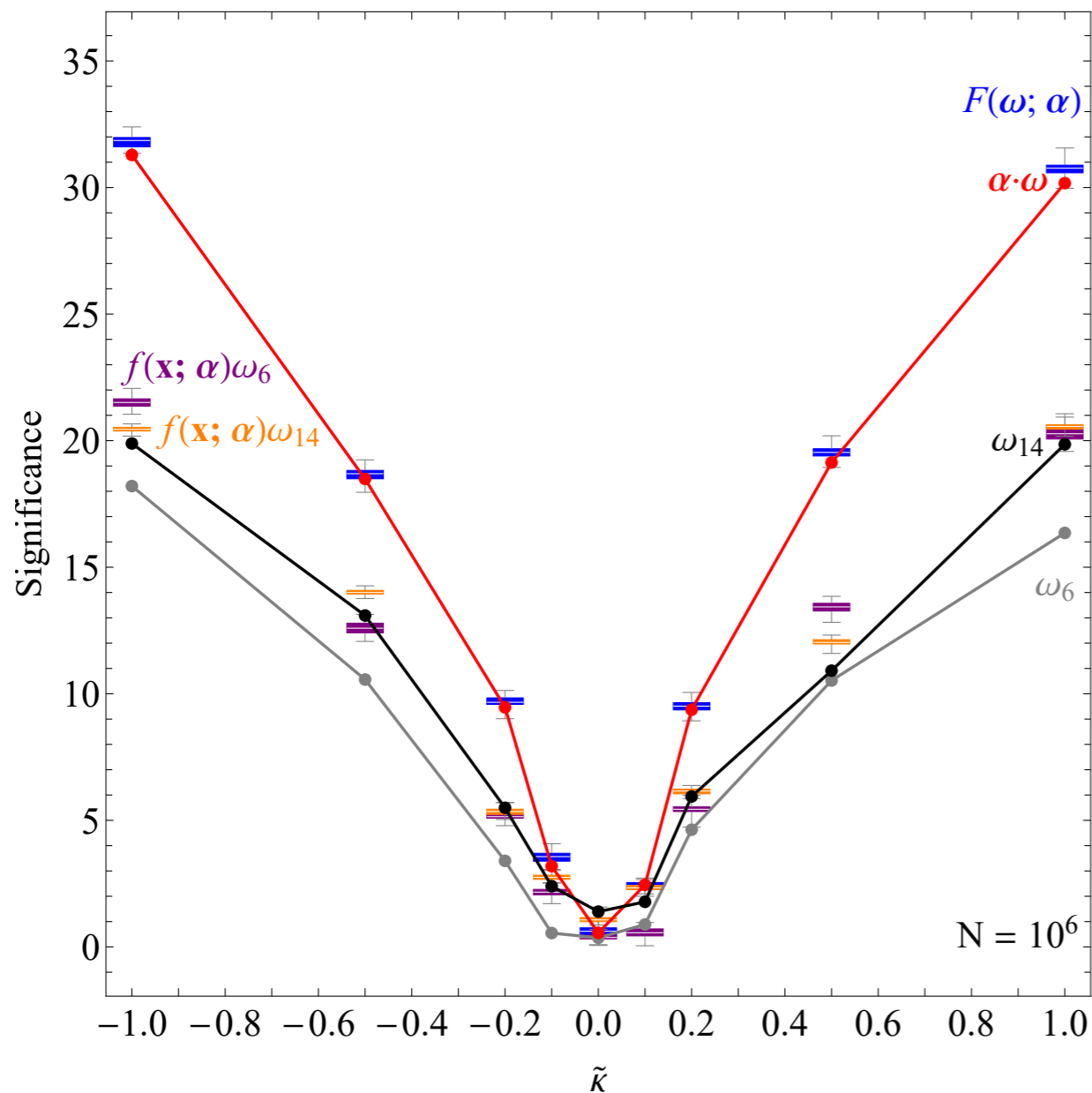
- ME/ML trained vs Observable



- Efficient observables
  - more sensitive
  - smaller errors
- Both CP and dim8 encourage more differential measurements

# Observables vs ML trained on model

Faroughy, Bortolato, Kamenik, Kosnik Smolkovic,  
Symmetry 13 (2021) no.7, 1129



Neural network

Linear combination

$$\omega_{14} \sim [(\mathbf{p}_{e^-} \times \mathbf{p}_{e^+}) \cdot (\mathbf{p}_b - \mathbf{p}_{\bar{b}})][(\mathbf{p}_b - \mathbf{p}_{\bar{b}}) \cdot (\mathbf{p}_{e^-} - \mathbf{p}_{e^+})]$$

$$\omega_6 \sim [(\mathbf{p}_{e^-} \times \mathbf{p}_{e^+}) \cdot (\mathbf{p}_b + \mathbf{p}_{\bar{b}})][(\mathbf{p}_{e^-} - \mathbf{p}_{e^+}) \cdot (\mathbf{p}_b + \mathbf{p}_{\bar{b}})]$$

# Comments

- ME/ML trained vs Observable



- Efficient observables
  - more sensitive
  - smaller errors
- Both CP and dim8 encourage more differential measurements

# CPV in WW

Preliminary

$$C_{11} = 1, \Lambda = 1\text{TeV}$$

w+/w- helicities	x-sect. in fb (LHC13)
--	0.0705
-0	0.0865
-+	0
0-	0.0784
00	0
0+	-0.0849
+-	0
+0	-0.0785
++	-0.0684

$$A \propto s^0$$

$$\sigma_{10} \approx -1\text{pb}$$

$$C_{10} = 1, \Lambda = 1\text{TeV}$$

$$A = 0.4\text{fb}$$