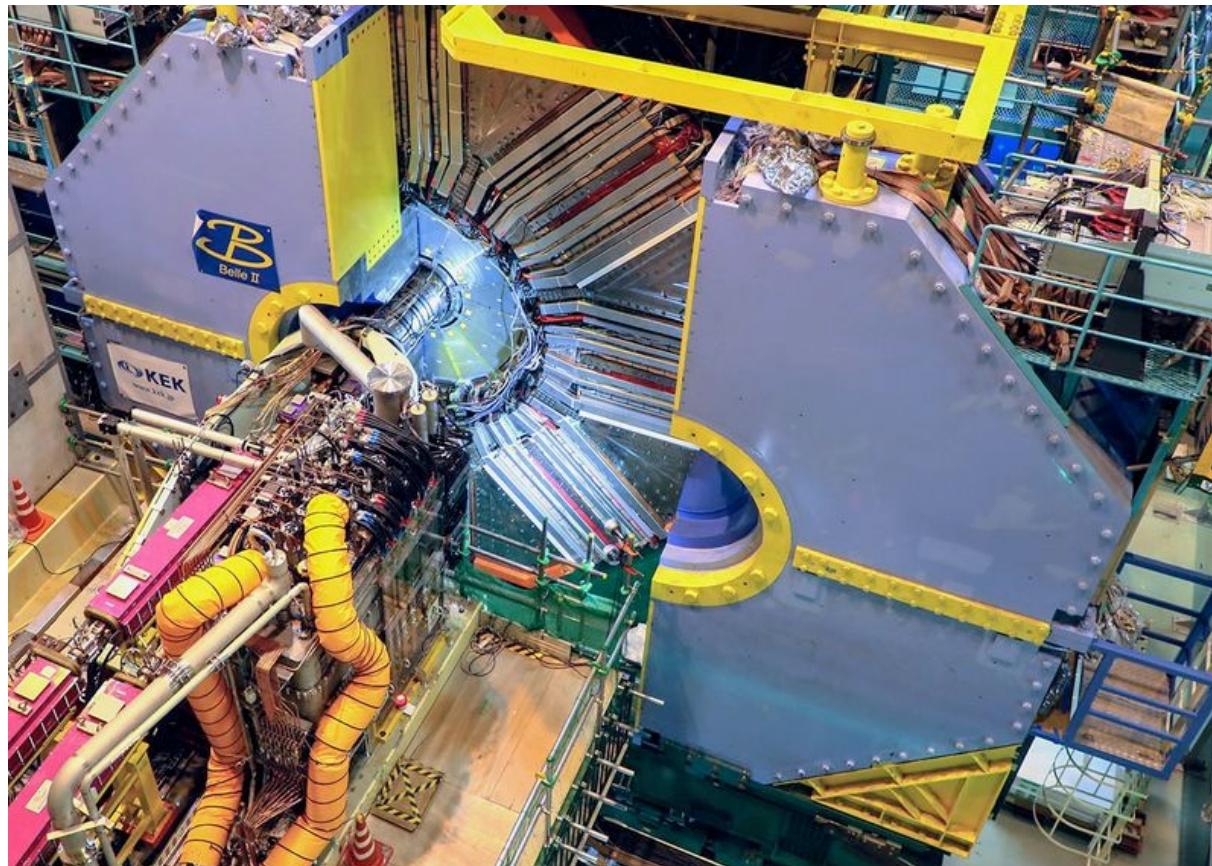




# *Charm lifetimes at Belle II: recent results*

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**11th International Workshop  
on Charm Physics  
(CHARM 2023)**  
University of Siegen  
Siegen, Germany  
17 July 2023



- motivation
- overview of *Belle II*
- measurements
  - mesons:  $D^0, D^+, D_s^+$
  - baryons:  $\Lambda_c^+, \Omega_c^0$
- comparison with theory
- future

# Why measure charm lifetimes?

Lenz, IJMP A30 (2015)  
 Lenz et al., JHEP 12 (2020) 199  
 King, Lenz et al., JHEP 08 (2022) 241  
 Gratrex et al., JHEP 07 (2022) 058

Theory:

- **qualitatively understood in terms of simple diagrams,**  
e.g.,  $c \rightarrow s e^+ \nu$  partial width gives  $G_F^2 m_c^5 |V_{cs}|^2 / (192\pi^3)$  dependence. Long  $D^+$  lifetime can be understood as arising from destructive interference between spectator and color-suppressed amplitudes. But this doesn't include QCD...
- **to include QCD:** calculate using the Heavy Quark Expansion

$$\Gamma(D) = \frac{1}{2m_D} \sum_X \int_{\text{PS}} (2\pi)^4 \delta^{(4)}(p_D - p_X) |\langle X(p_X) | \mathcal{H}_{\text{eff}} | D(p_D) \rangle|^2,$$

$\Sigma X$  is sum over final states

$$\rightarrow \frac{1}{2m_D} \text{Im} \langle D | \mathcal{T} | D \rangle \quad \text{where} \quad \mathcal{T} = i \int d^4x T \{ \mathcal{H}_{\text{eff}}(x), \mathcal{H}_{\text{eff}}(0) \}$$

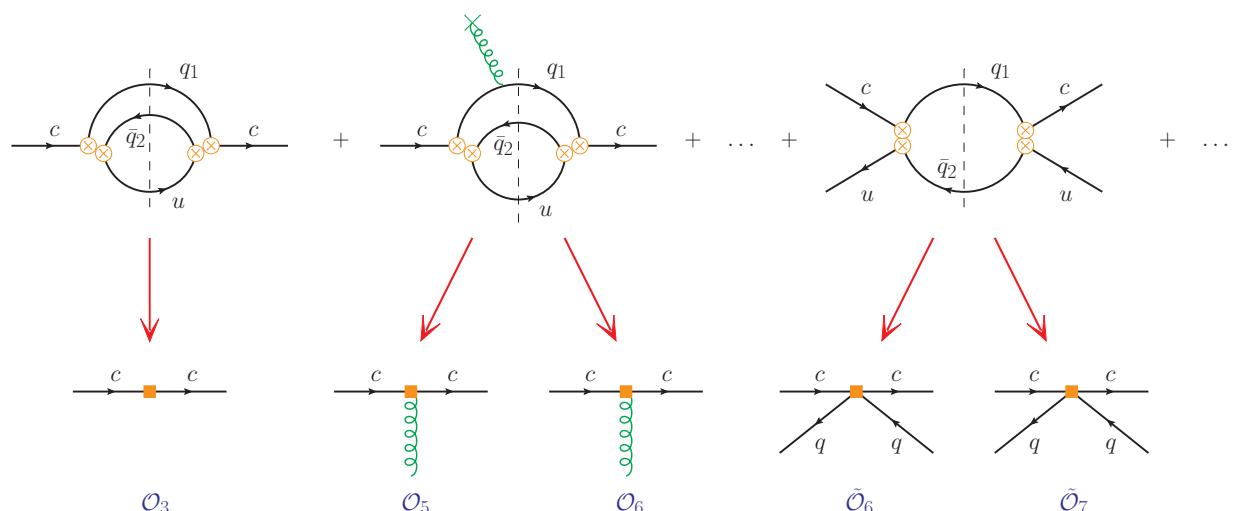
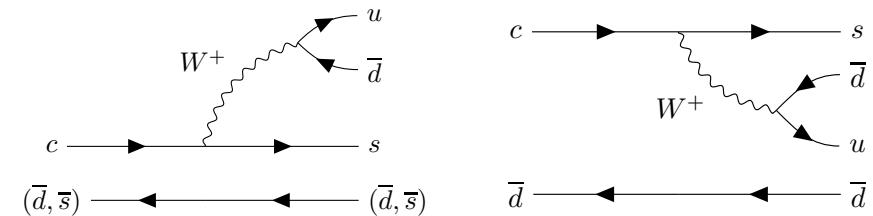
via optical theorem

$$\rightarrow \Gamma_3 + \Gamma_5 \frac{\langle \mathcal{O}_5 \rangle}{m_c^2} + \Gamma_6 \frac{\langle \mathcal{O}_6 \rangle}{m_c^3} + \dots + 16\pi^2 \left( \tilde{\Gamma}_6 \frac{\langle \tilde{\mathcal{O}}_6 \rangle}{m_c^3} + \tilde{\Gamma}_7 \frac{\langle \tilde{\mathcal{O}}_7 \rangle}{m_c^4} + \dots \right)$$

via Heavy Quark Expansion

Wilson coefficients  $\Gamma_i$  are expanded in powers of  $\alpha_s$  and calculated perturbatively

⇒ comparing lifetime calculations with measurements tests/improves our understanding of QCD

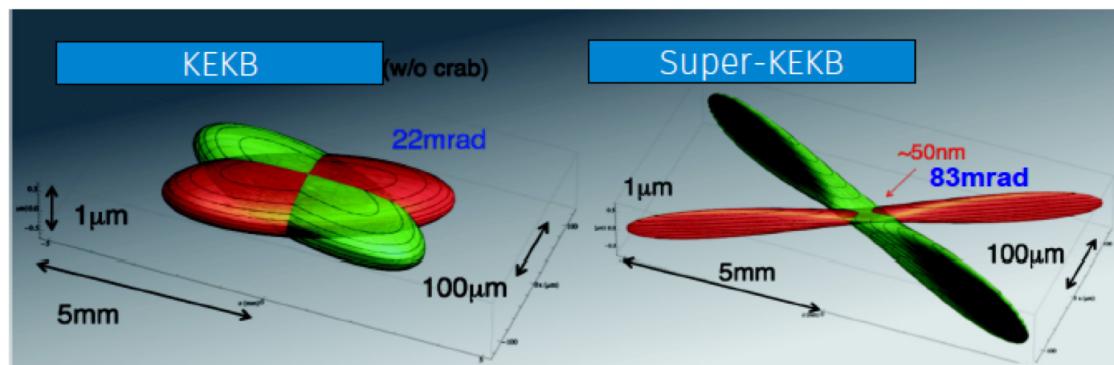
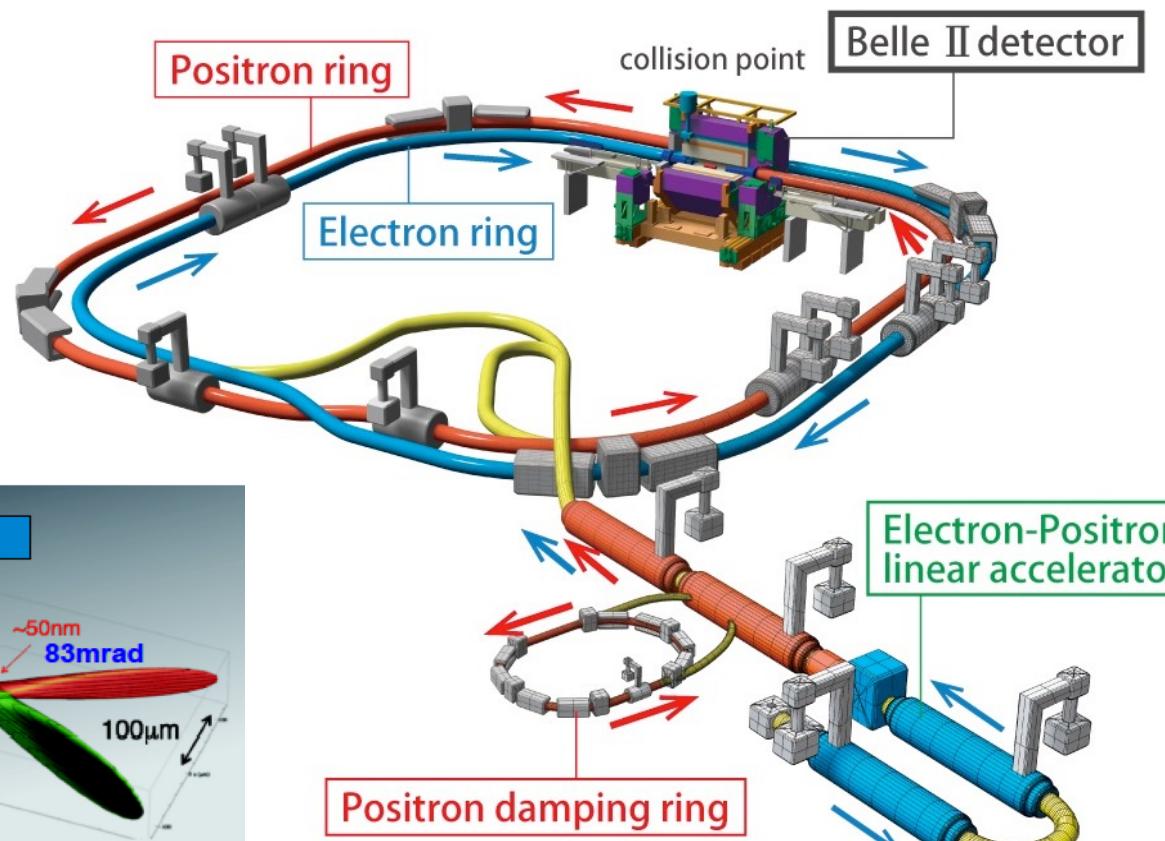


# Major accelerator upgrade (KEKB → SuperKEKB)

$e^+e^-$  collider running at the Upsilon(4S) [and Upsilon (5S)] resonances with 7 GeV ( $e^-$ ) on 4 GeV( $e^+$ ) beams.  
 New  $e^+$  damping ring, new  $e^+$  storage ring, new IR optics, Superconducting FF, new RF

**beam size:**  
 $100 \mu\text{m}(H) \times 2 \mu\text{m}(V)$   
 $\rightarrow 10 \mu\text{m}(H) \times 59 \text{ nm}(V)$

**Belle-II Goal:**  
 $30 \times \text{Belle} = \sim 6 \times 10^{35}$

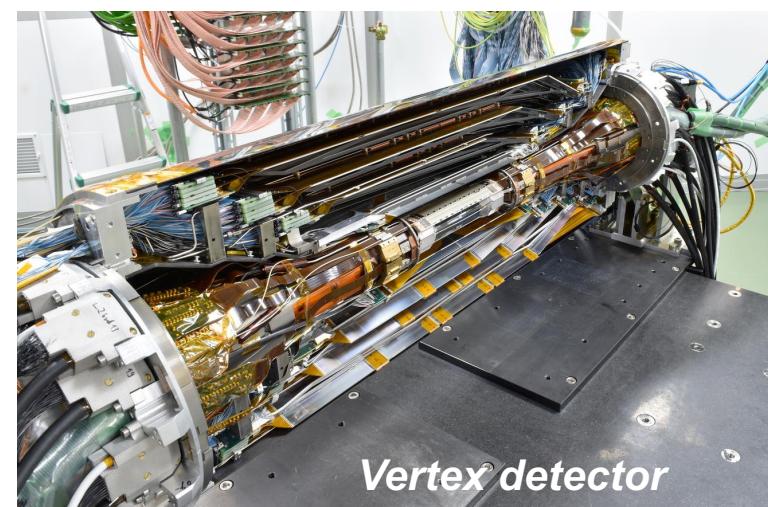
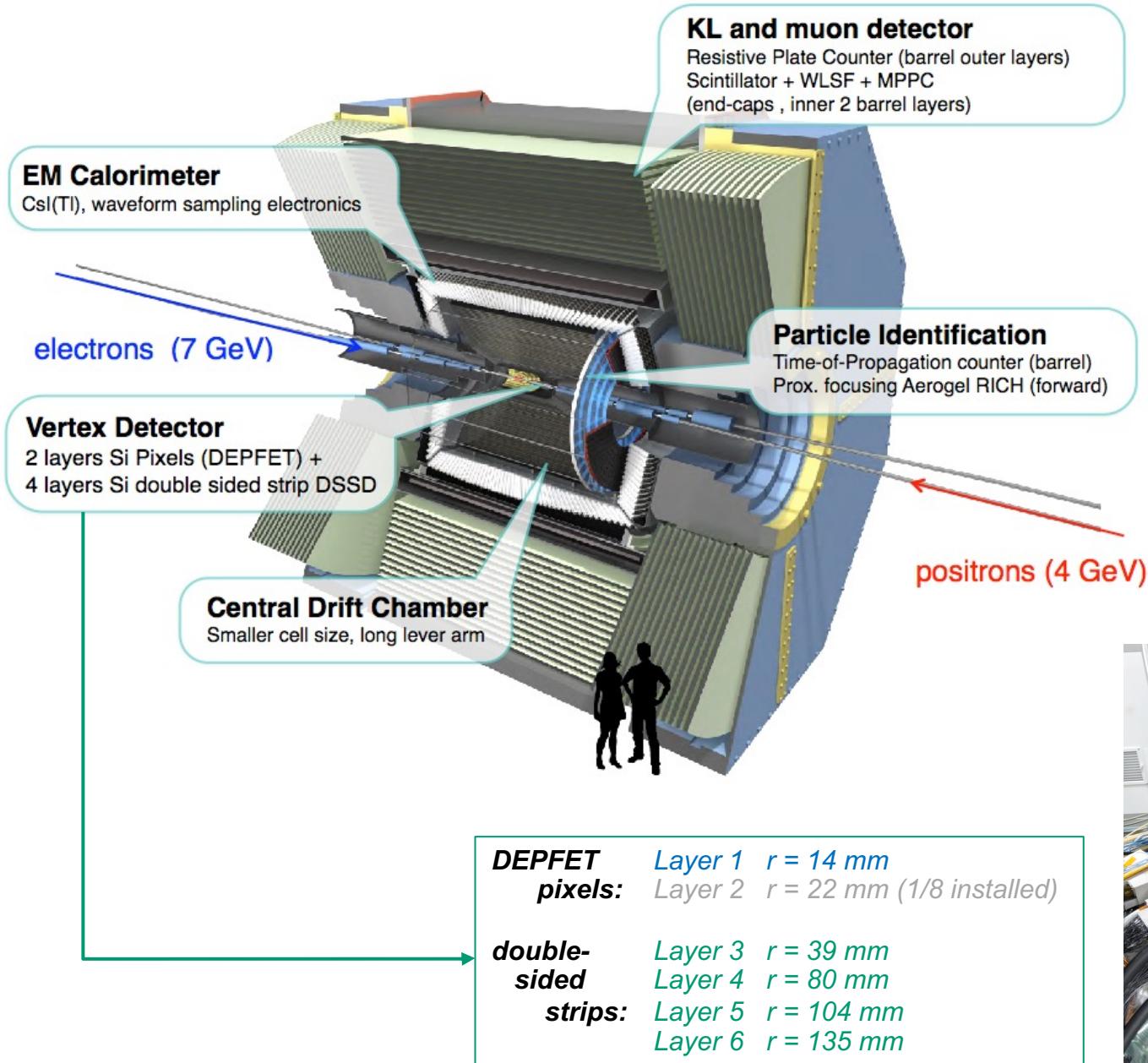


	E (GeV) LER/HER	$\beta^*_y$ (mm) LER/HER	$\beta^*_x$ (cm) LER/HER	$\phi$ (mrad)	I (A) LER/HER	L ( $\text{cm}^{-2}\text{s}^{-1}$ )
KEKB	3.5/8.0	5.9/5.9	120/120	11	1.6/1.2	$2.1 \times 10^{34}$
SuperKEKB	4.0/7.0	0.27/0.30	3.2/2.5	41.5	3.6/2.6	$80 \times 10^{34}$

factor 20

factor 2-3

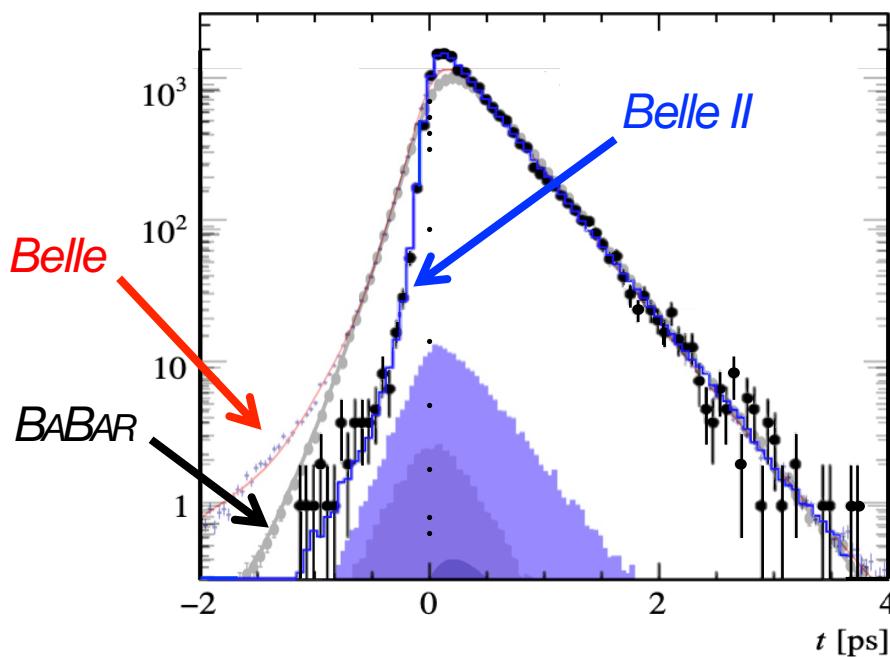
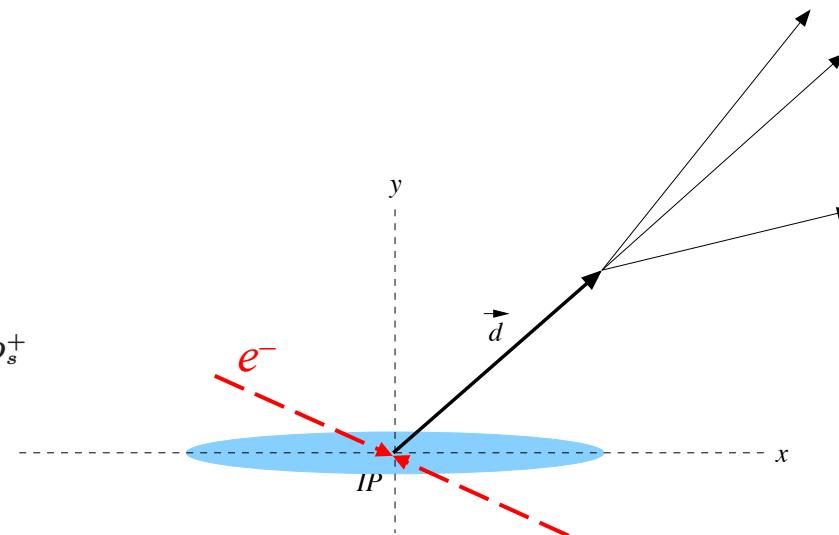
# The Belle II Experiment



# Charm lifetimes: measurement @ Belle II

Determine lifetime by measuring vertex displacement and momentum:

$$t = \left( \frac{\vec{d} \cdot \vec{p}}{p^2} \right) m_{D_s^+}$$



- IP is measured every 30 minutes using  $e^+e^- \rightarrow \mu^+\mu^-$  events
- Uncertainty on  $t$  ( $\sigma_t$ ) is calculated event-by-event by propagating uncertainties  $\delta d_x$ ,  $\delta d_y$ ,  $\delta d_z$ ,  $\delta p_x$ ,  $\delta p_y$ ,  $\delta p_z$  and their correlations.
- The uncertainty  $\sigma_t$  is used as the width of a Gaussian resolution function used to fit the  $t$  distribution
- decay time resolution is > 2 times better than Belle/Babar:  
80-90 fs vs. 200 fs

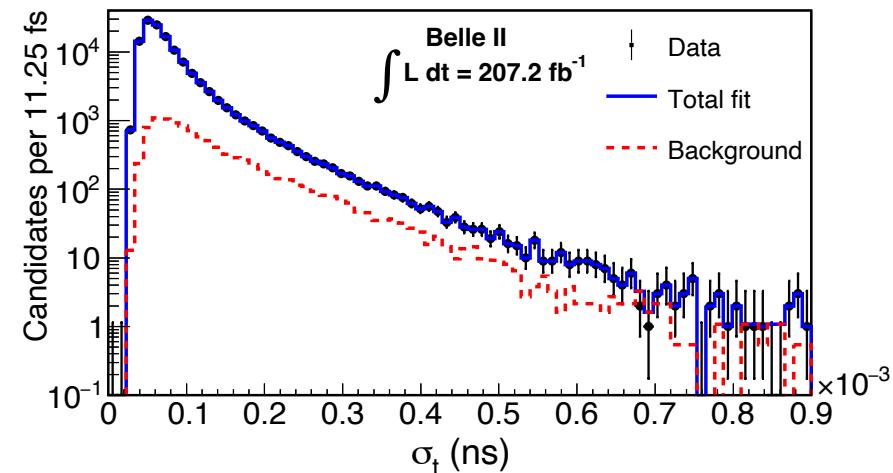
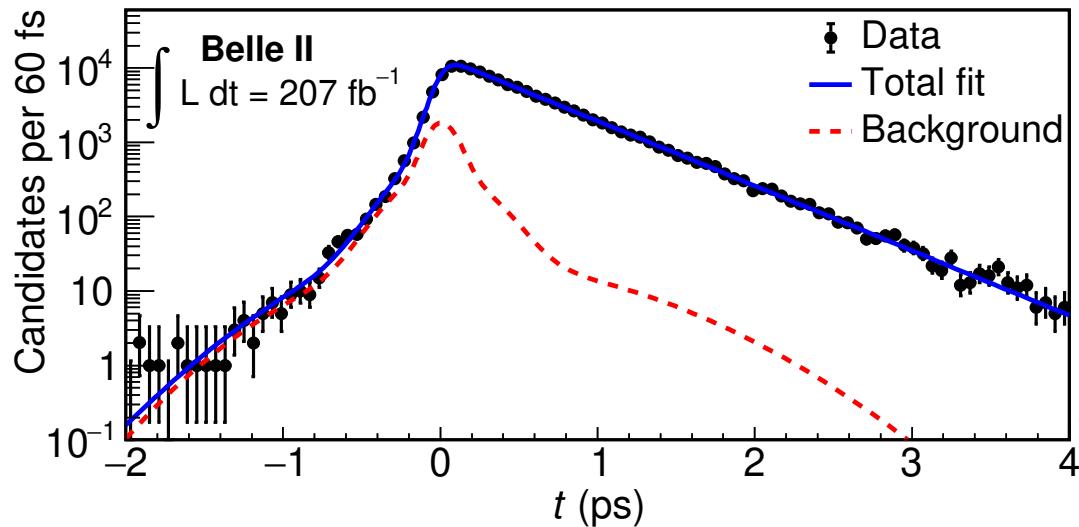
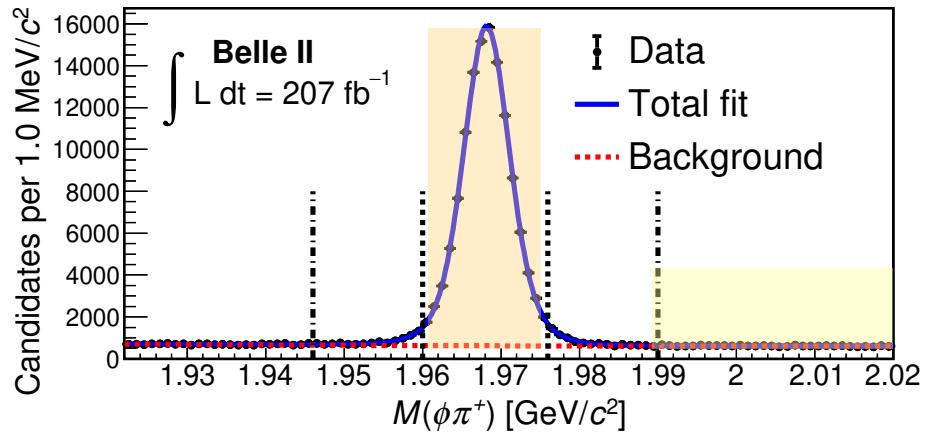
# $D_s^+$ lifetime (207 $\text{fb}^{-1}$ )

arXiv:2306.00365, submitted to PRL

- Select  $D_s^+ \rightarrow \phi \pi^+$  ( $\phi \rightarrow K^+K^-$ ) (low background)
- $p_{CM}(D_s^+) > 2.5 \text{ GeV}/c$  to eliminate  $B \rightarrow D_s^+ X$  decays (preserves 2/3 of  $e^+e^- \rightarrow \bar{c}c$  events)
- require  $M(\phi\pi^+) \in [1.960, 1.976] \text{ GeV}/c^2$ ; unbinned ML fit give 116k signal, 92% purity. Background from random combinations of  $\phi$  and  $\pi^+$
- lifetime determined from unbinned ML fit to  $t$ . Likelihood function for event  $i$ :

$$\mathcal{L}(\tau|t^i, \sigma_t^i) = f_{\text{sig}} P_{\text{sig}}(t^i|\tau, \sigma_t^i) P_{\text{sig}}(\sigma_t^i) + (1 - f_{\text{sig}}) P_{\text{bkg}}(t^i|\tau, \sigma_t^i) P_{\text{bkg}}(\sigma_t^i)$$

(to avoid bias: Punzi,  
arXiv:physics/0401045)



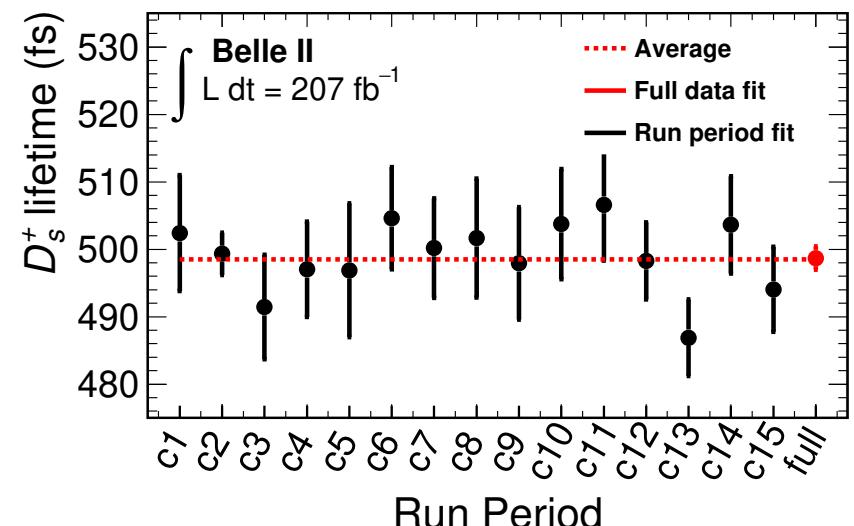
- PDF for signal  $D_s^+$  decays:

$$P_{\text{sig}}(t^i|\tau, \sigma_t^i) = \frac{1}{\tau} \int e^{-t'/\tau} R(t^i - t'; \mu, s, \sigma_t^i) dt'$$

- resolution function  $R$  is a single Gaussian with mean  $\mu$  and per-candidate standard deviation  $s \times \sigma_t^i$ ;  $\mu$  and scaling parameter  $s$  are floated
- PDF for background is taken from fitting  $M(\phi\pi^+)$  upper sideband [1.990, 2.020] GeV/c $^2$
- Result:  $\tau_{D_s^+} = (498.7 \pm 1.7^{+1.1}_{-0.8})$  fs

- Systematic uncertainties:

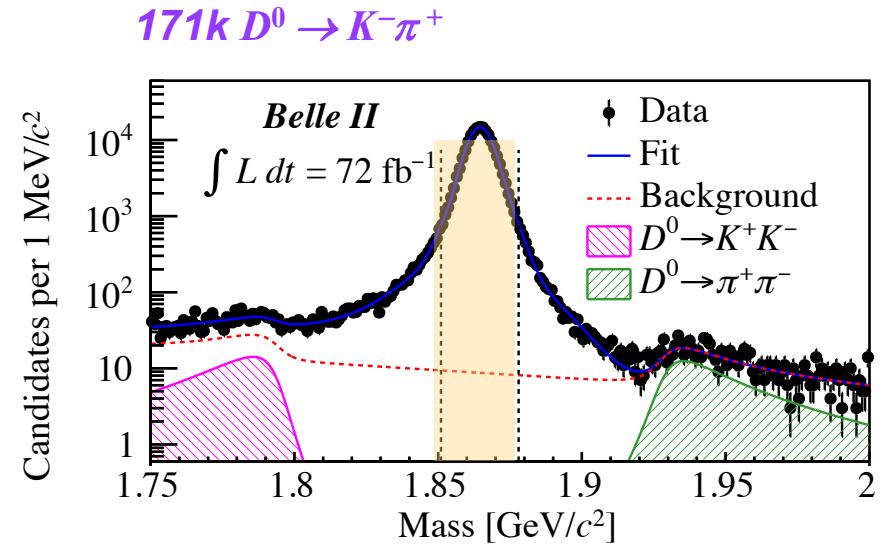
Source	Uncertainty (fs)
Resolution function	+0.85
Background ( $t, \sigma_t$ ) distribution	$\pm 0.40$
Binning of $\sigma_t$ histogram PDF	$\pm 0.10$
Imperfect detector alignment	$\pm 0.56$
Sample purity	$\pm 0.09$
Momentum scale factor	$\pm 0.28$
$D_s^+$ mass	$\pm 0.02$
Total	$^{+1.14}_{-0.76}$



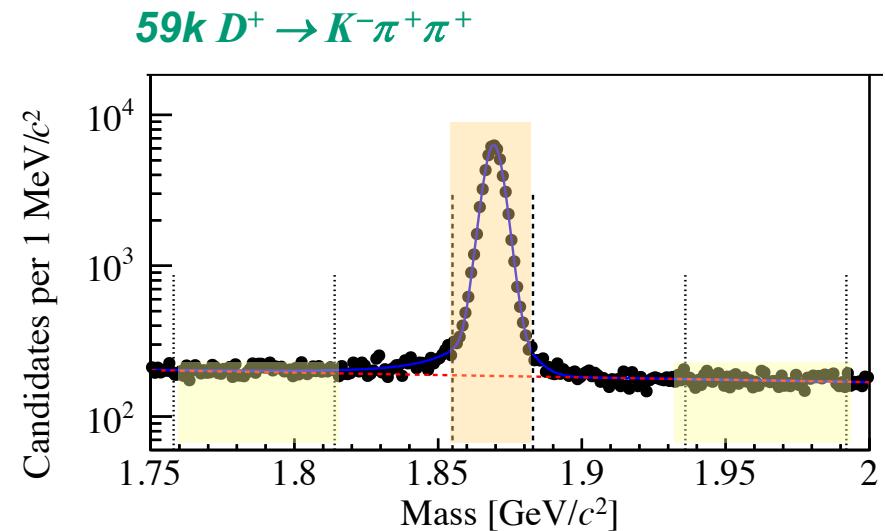
# $D^0$ and $D^+$ lifetimes ( $72 \text{ fb}^{-1}$ )

Abudinen et al., PRL 127, 211801 (2021)  
 [arXiv:2108.03216]

- Select  $D^{*+} \rightarrow D^0 \pi_s^+$  ( $D^0 \rightarrow K^- \pi^+$ ) decays ( $\sim$ no background)
- $p_{CM}(D^{*+}) > 2.5 \text{ GeV}/c$  to eliminate  $B \rightarrow D^{*+} X$  decays
- require  $M(K^- \pi^+) \in [1.851, 1.878] \text{ GeV}/c^2$  and  $M(K^- \pi^+ \pi_s^+) - M(K^- \pi^+) \in [144.94, 145.90] \text{ MeV}/c^2$ ; binned  $\chi^2$  fit give 171k signal, 99.8% purity



- Select  $D^{*+} \rightarrow D^+ \pi^0$  ( $D^+ \rightarrow K^- \pi^+ \pi^+$ ) decays (low background), where  $\pi^0 \rightarrow \gamma\gamma$  and  $m(\gamma\gamma) \in [120, 145] \text{ MeV}/c^2$
- $p_{CM}(D^{*+}) > 2.6 \text{ GeV}/c$  to eliminate  $B \rightarrow D^{*+} X$  decays
- require  $M(K^- \pi^+) \in [1.855, 1.883] \text{ GeV}/c^2$  and  $\Delta M \in [138, 143] \text{ MeV}/c^2$ ; binned  $\chi^2$  fit give 59k signal, 91% purity



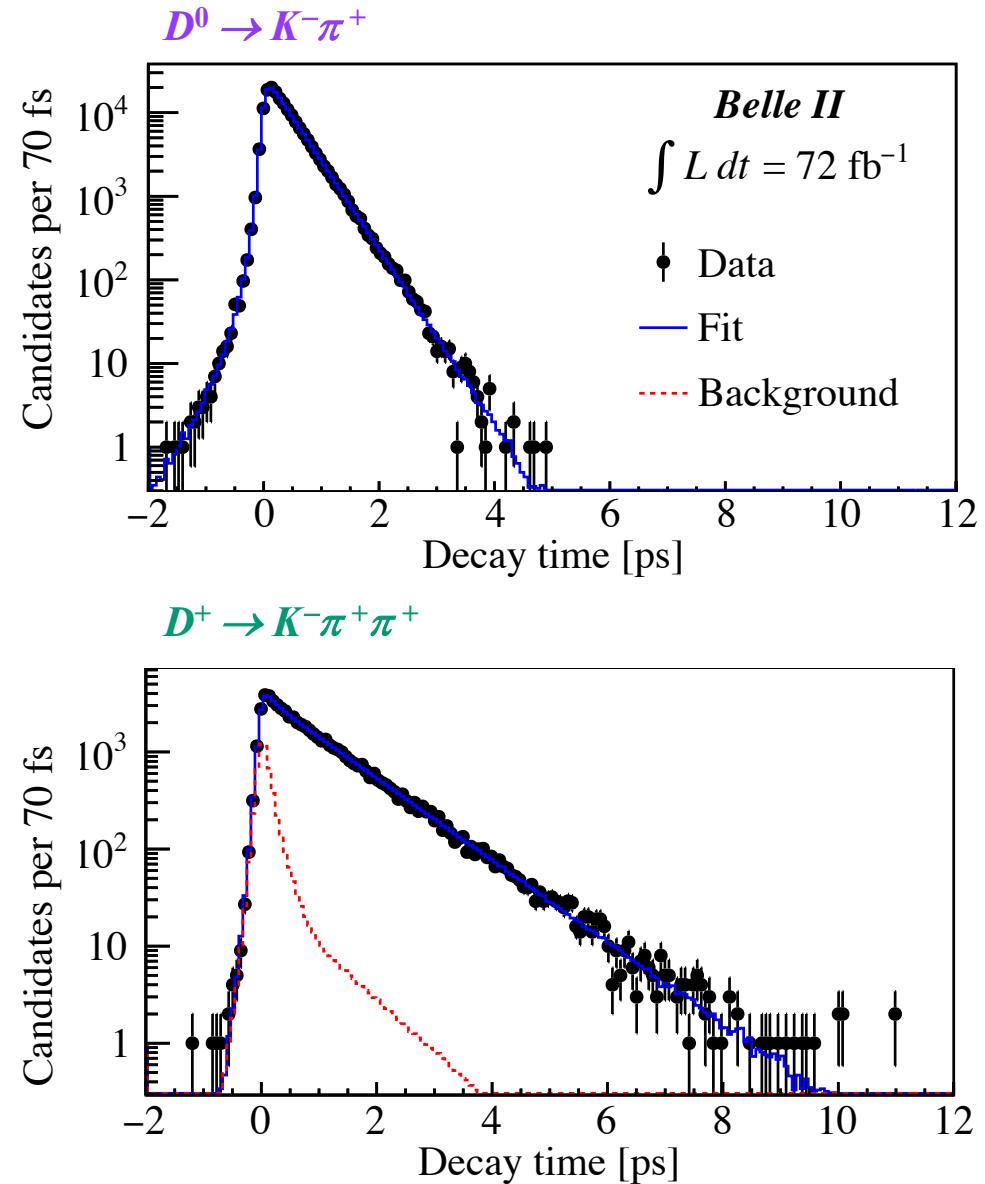
# $D^0$ and $D^+$ lifetimes ( $72 \text{ fb}^{-1}$ )

Abudinen et al., PRL 127, 211801 (2021)  
 [arXiv:2108.03216]

- lifetime determined from unbinned ML fit to  $(t, \sigma_t)$
- resolution function  $R$  is a double Gaussian for  $D^0$  (single Gaussian for  $D^+$ ) with mean  $\mu$  and per-candidate standard deviation  $s \times \sigma_t^i$ ;  $\mu$  and scaling parameter  $s$  are floated
- PDF for  $D^+$  background is taken from fitting  $M(K^-\pi^+\pi^+)$  sidebands [1.758, 1.814] and [1.936, 1.992]  $\text{GeV}/c^2$ .  $D^0$  background is neglected, with a systematic included
- Results:
 

$\tau_{D^0} = (410.5 \pm 1.1 \pm 0.8) \text{ fs}$   
 $\tau_{D^+} = (1030.4 \pm 4.7 \pm 3.1) \text{ fs}$
- Systematic uncertainties:

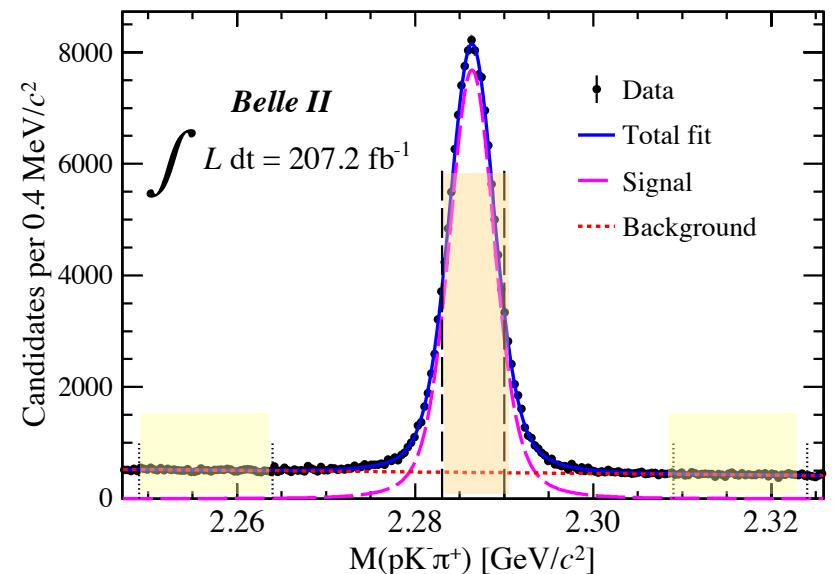
Source	$\tau(D^0)$ (fs)	$\tau(D^+)$ (fs)
Resolution model	0.16	0.39
Backgrounds	0.24	2.52
Detector alignment	0.72	1.70
Momentum scale	0.19	0.48
Total	0.80	3.10



# $\Lambda_c^+ \text{ lifetime } (207 \text{ fb}^{-1})$

Abudinen et al., PRL 130, 071802 (2023)  
 [arXiv:2206.15227]

- Select  $\Lambda_c^+ \rightarrow pK^-\pi^+$  decays (low background)
- $p_{CM}(\Lambda_c^+) > 2.5 \text{ GeV}/c$  to eliminate  $B \rightarrow \Lambda_c^+ X$  decays
- require  $M(pK^-\pi^+) \in [2.283, 2.290] \text{ GeV}/c^2$ ; binned  $\chi^2$  fit gives 116k signal, 93% purity
- lifetime determined from unbinned ML fit to  $(t, \sigma_t)$ . Background  $(t, \sigma_t)$  distribution is determined from sidebands  $M(pK^-\pi^+) \in [2.249, 2.264] \text{ GeV}/c^2$  and  $[2.309, 2.324] \text{ GeV}/c^2$
- Resolution function  $R(t, \sigma_t)$  is a single Gaussian with mean  $\mu$  and standard deviation  $s \times \sigma_t$ ;  $\mu$  and  $s$  are floated
- problematic background from  $\Xi_c^0 \rightarrow \Lambda_c^+\pi^-$ ,  $\Xi_c^+ \rightarrow \Lambda_c^+\pi^0$  decays:  $\tau(\Xi_c^0) = 153 \text{ fs}$ ,  $\tau(\Xi_c^+) = 456 \text{ fs}$ .
  - $\Xi$  contamination in  $\Lambda_c^+$  sample is estimated by fitting distribution of  $\Lambda_c^+$  vertex displacement in plane transverse to the beam. Result: 374 events (0.003% of  $\Lambda_c^+$  candidates).
  - To reduce, impose vetos:  
 $M(pK^-\pi^+) - M(pK^-\pi^+) \notin [183.4, 186.4] \text{ MeV}/c^2$   
 $M(pK^-\pi^0) - M(pK^-\pi^+) \notin [175.3, 187.3] \text{ MeV}/c^2$   
 This reduces  $\Xi$  decays by 40%.
  - Effect of remaining decays is estimated via MC simulation; bias of 0.34 fs is subtracted from fitted  $\tau(\Lambda_c^+)$



# $\Lambda_c^+ \text{ lifetime } (207 \text{ fb}^{-1})$

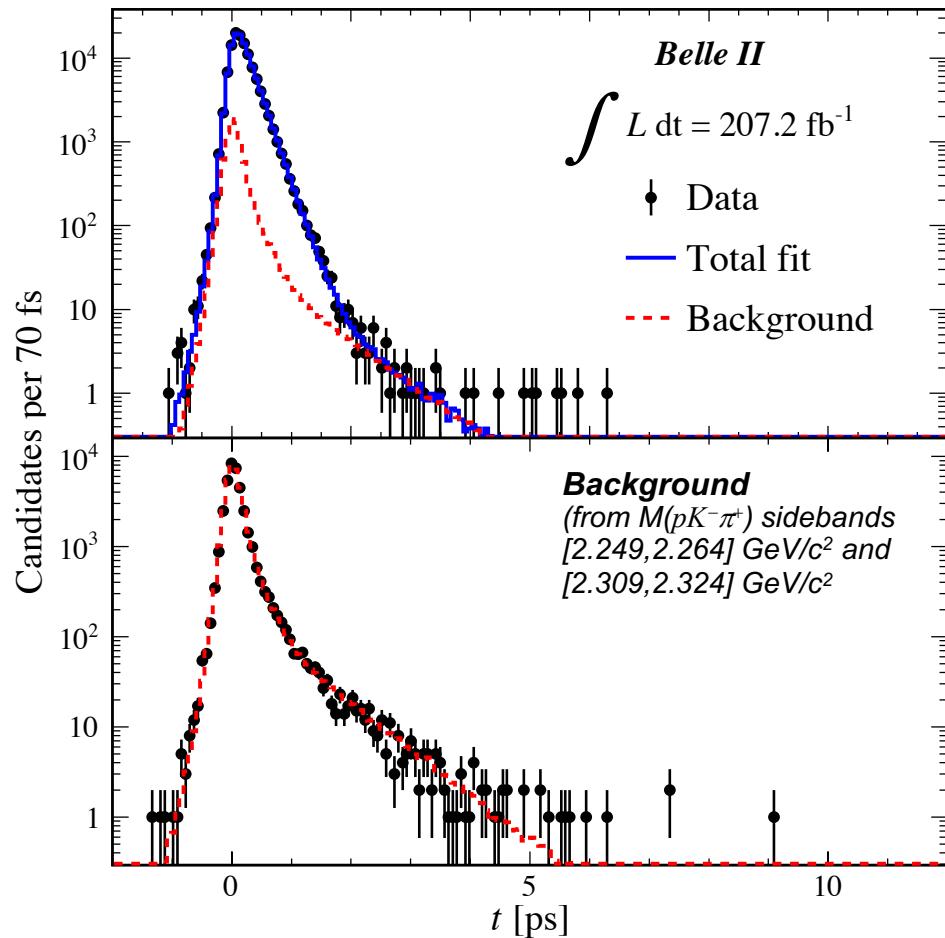
Abudinen et al., PRL 130, 071802 (2023)  
 [arXiv:2206.15227]

- PDF for background is sum of two exponentials and a  $\delta$  function, all convolved with resolution functions having floated parameters  $\mu_b, s_b$
- Result:

$$\tau_{\Lambda_c^+} = (203.20 \pm 0.89 \pm 0.77) \text{ fs}$$

- Systematic uncertainties:

Source	Uncertainty [fs]
$\Xi_c$ contamination	0.34
Resolution model	0.46
Non- $\Xi_c$ backgrounds	0.20
Detector alignment	0.46
Momentum scale	0.09
Total	0.77



# $\Omega_c^0$ lifetime (207 fb $^{-1}$ )

Abudinen et al., PRD 107, L031103 (2023)  
 [arXiv:2208.08573]

Theory expectation:  
 (& E687, WA89)

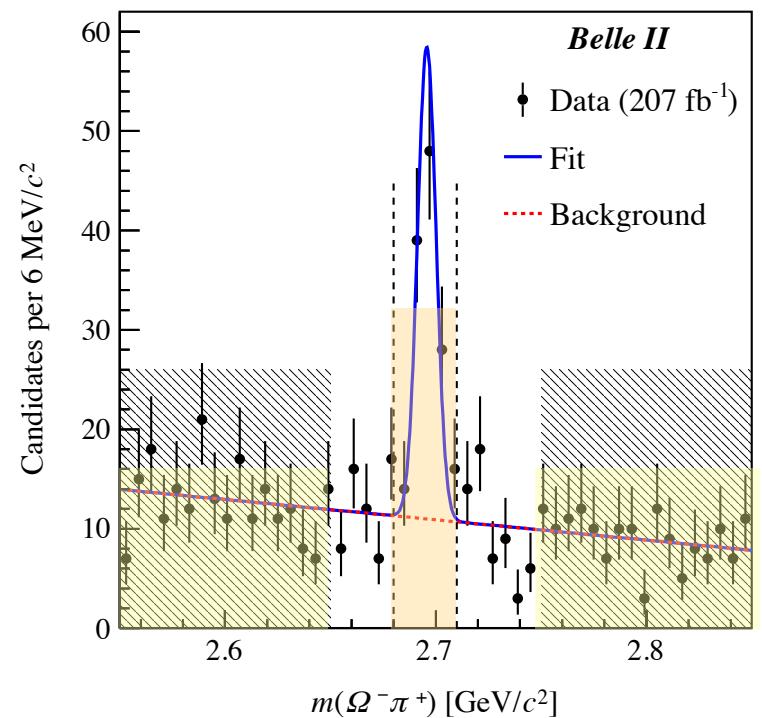
$$\tau(\Omega_c) < \tau(\Xi_c^0) < \tau(\Lambda_c^+) < \tau(\Xi_c^+)$$

LHCb measurement:  
 (2018, 2022)

$$\tau(\Xi_c^0) < \tau(\Lambda_c^+) < \tau(\Omega_c) < \tau(\Xi_c^+)$$

⇒ Belle II can confirm this  
 (useful to have another experiment confirm)

- Select  $\Omega_c \rightarrow \Omega^- \pi^+$ ,  $\Omega^- \rightarrow \Lambda K^-$ ,  $\Lambda \rightarrow p \pi^-$  decays (large CF branching fractions)
- $p_{CM}(\Omega_c)/p_{max} > 0.6$  to eliminate  $B \rightarrow \Omega_c X$  decays, where  $p_{max} = \sqrt{[E_{beam}^{CM}]^2 - m(\Omega\pi)^2}$
- require  $M(\Omega^- \pi^+) \in [2.68, 2.71] \text{ GeV}/c^2$ ; unbinned ML fit gives 132 signal decays, 67% purity
- lifetime determined from unbinned ML fit to  $(t, \sigma_t)$ . Background  $(t, \sigma_t)$  distribution determined from sidebands  $M(\Omega^- \pi^+) \in [2.55, 2.65] \text{ GeV}/c^2$  and  $[2.75, 2.85] \text{ GeV}/c^2$
- Resolution function  $R(t, \sigma_t)$  is a single Gaussian with mean  $\mu$  and standard deviation  $s \times \sigma_t$ ;  $\mu$  and  $s$  are floated



# $\Omega_c^0$ lifetime ( $207 \text{ fb}^{-1}$ )

Abudinen et al., PRD 107, L031103 (2023)  
 [arXiv:2208.08573]

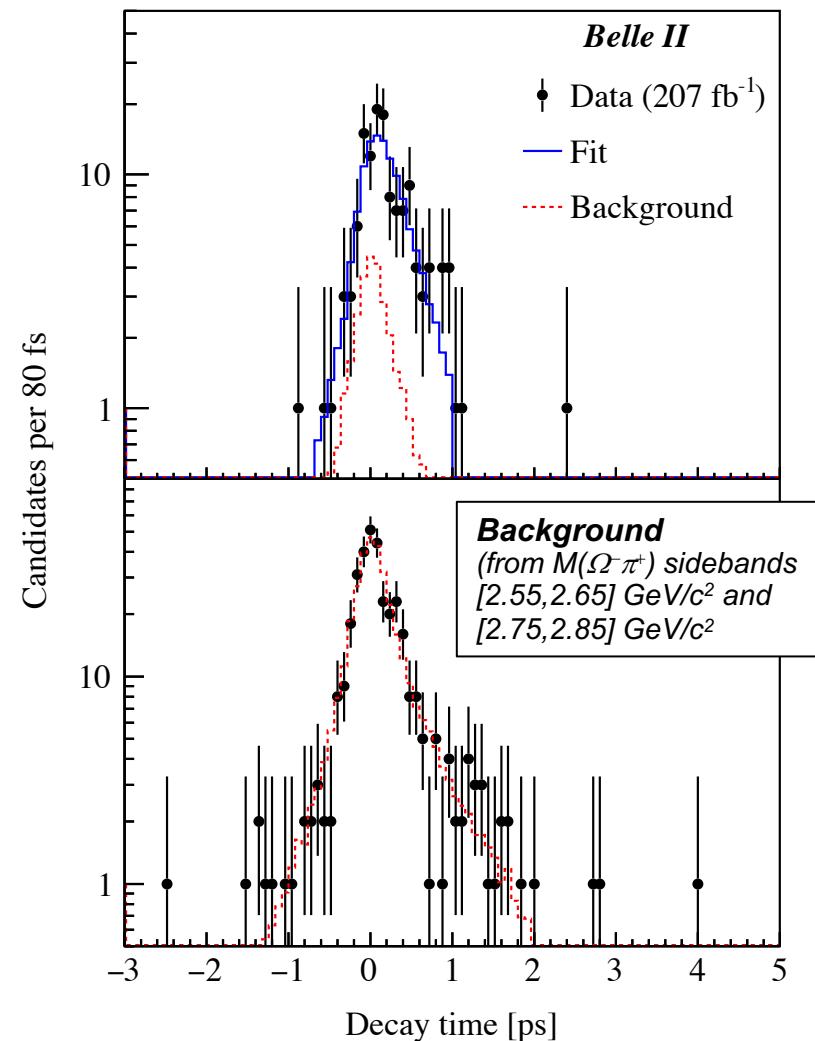
- PDF for background is sum of an exponential and a  $\delta$  function, both convolved with a Gaussian resolution function having floated parameters  $\mu_b$  and  $s_b$

- Result:

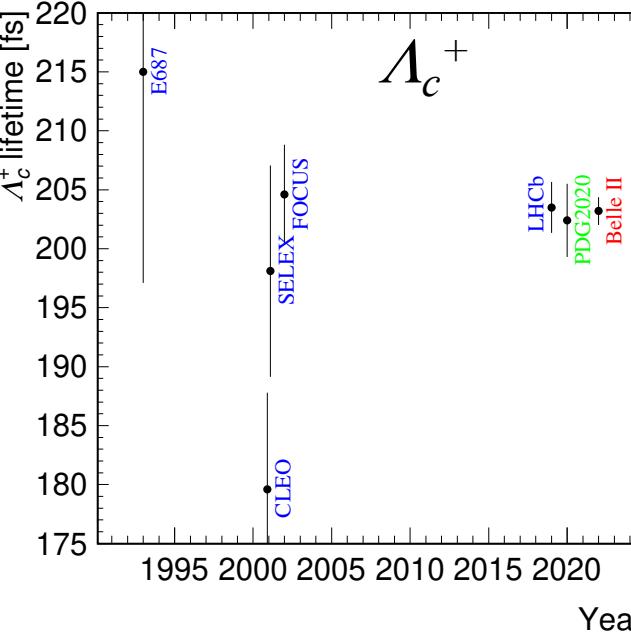
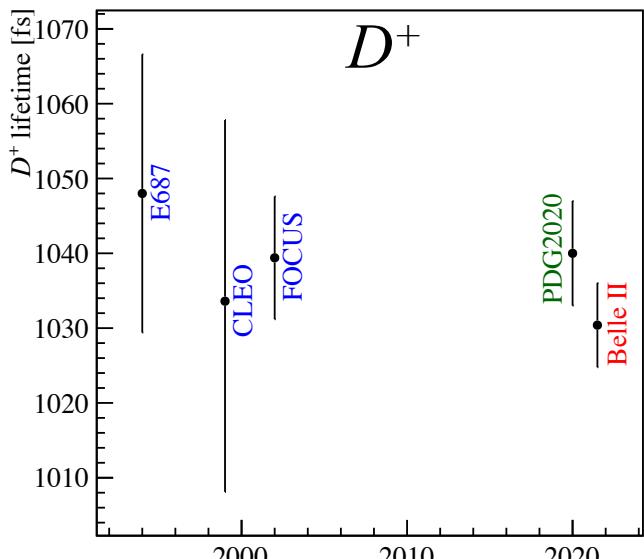
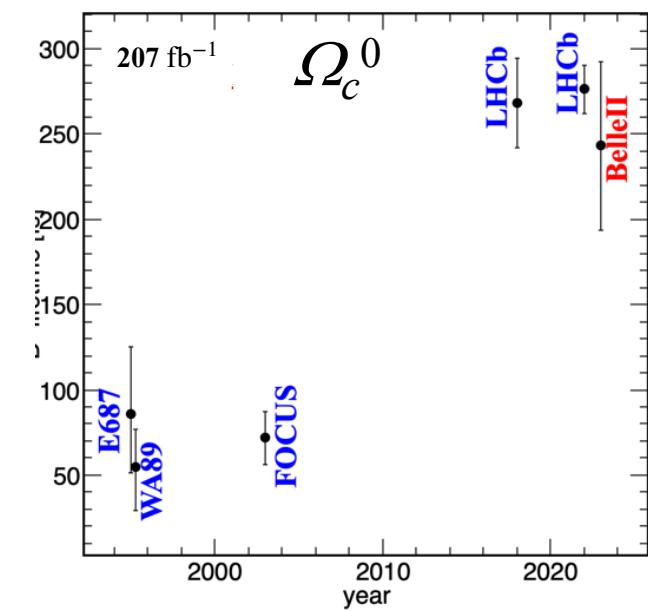
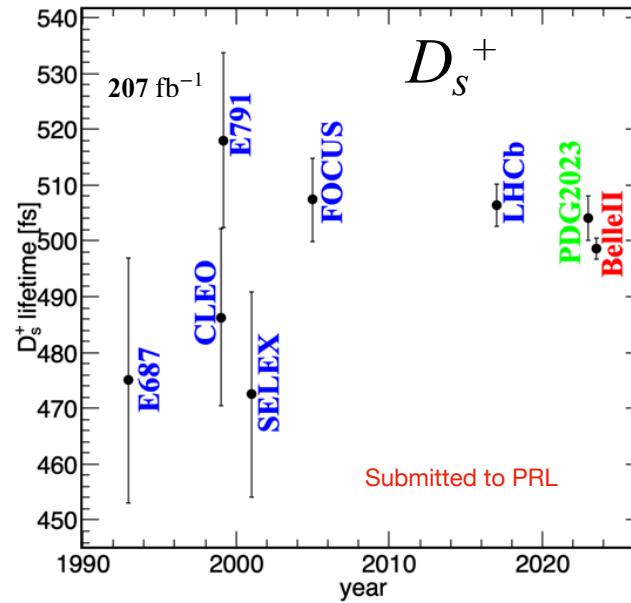
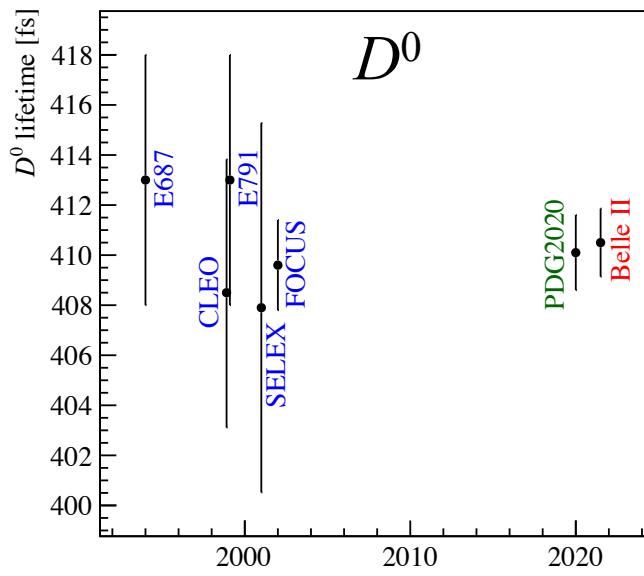
$$\tau_{\Omega_c^0} = (243 \pm 48 \pm 11) \text{ fs}$$

- Systematic uncertainties:

Source	Uncertainty (fs)
Fit bias	3.4
Resolution model	6.2
Background model	8.3
Detector alignment	1.6
Momentum scale	0.2
Input $\Omega_c^0$ mass	0.2
Total	11.0



# Summary I



- In all cases except for  $\Omega_c^0$ , Belle II has made the world's highest precision measurement (in some cases after 20 years)
- For  $\Omega_c^0$ , the Belle II measurement confirms the longer lifetime observed by LHCb (in contrast to older experiments and theory expectations)



# Summary II

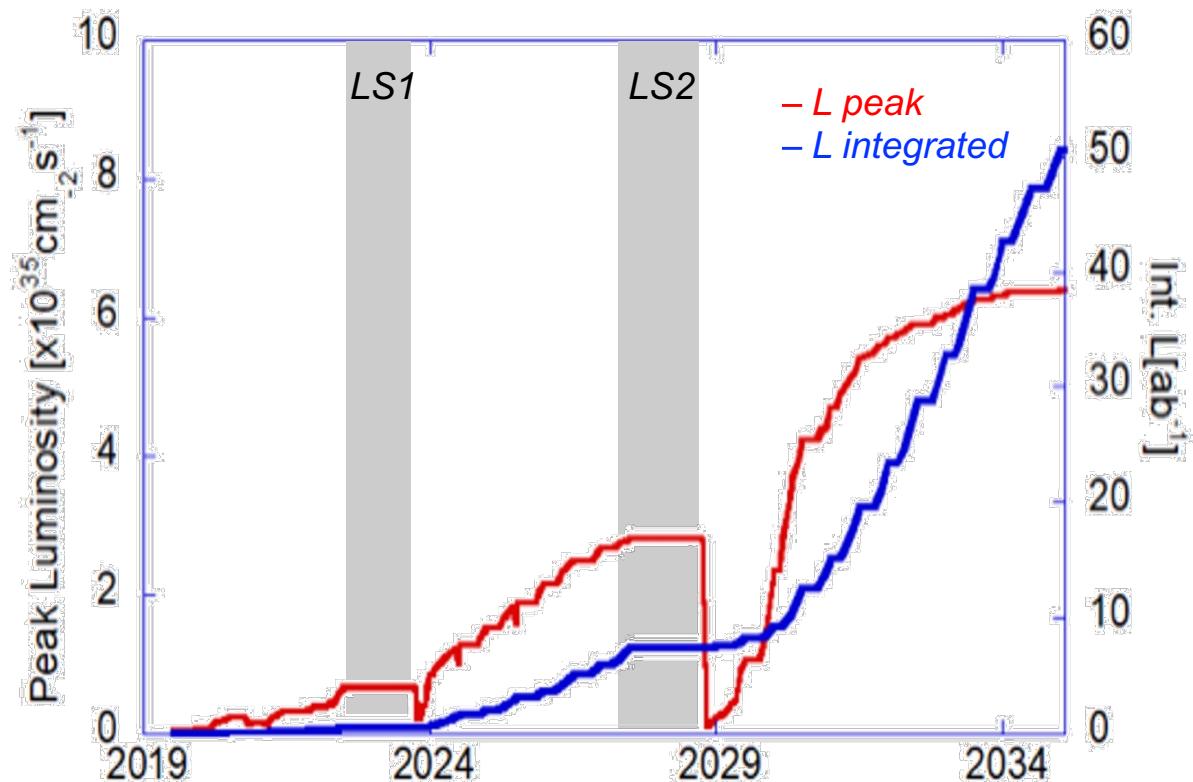
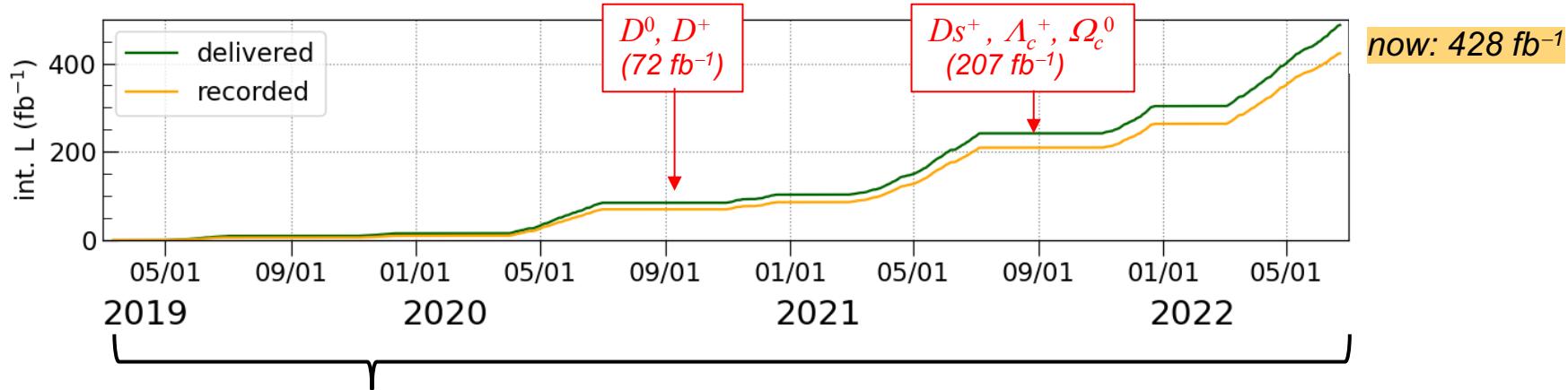
Comparisons with theory:

Quantity	Belle II	King et al. JHEP 08 (2022) 241 (Table 15)	Gratrex et al. JHEP 07 (2022) 058 (Tables 10, 14, MSR)
$\tau(D^0)$	$410.5 \pm 1.1 \pm 0.8$	$629^{+296}_{-167}$	$595^{+344}_{-166}$
$\tau(D^+)$	$1030.4 \pm 4.7 \pm 3.1$	$> 897$ (90% CL)	$> 1260$ (90% CL)
$\tau(D_s^+)$	$498.7 \pm 1.7^{+1.1}_{-0.8}$	$637^{+381}_{-190}$	$599^{+459}_{-180}$
$\tau(D^+)/\tau(D^0)$	2.510	$2.80 \pm 0.90$	$2.89 \pm 0.82$
$\tau(D_s^+)^*/\tau(D^0)$	1.215	$1.01 \pm 0.15$	$1.00 \pm 0.22$
$\tau(A_c^+)$	$203.20 \pm 0.89 \pm 0.77$		$312^{+128}_{-96}$
$\tau(\Omega_c^0)$	$243 \pm 48 \pm 11$		$237^{+111}_{-75}$
$\tau(\Omega_c^0)/\tau(A_c^+)$	$1.20 \pm 0.24$		$0.83^{+0.30}_{-0.18}$

(\*subtracting  $B(D_s^+ \rightarrow \tau^+ \nu) = 5.32\%$ )

- Experimental precision is much greater than theory precision (large theory uncertainties)
- Even with large theory uncertainties, a few predictions differ from experiment by  $> 1\sigma$  (but less than  $2\sigma$ ). In the future when theory errors are reduced, such differences could become interesting – stay tuned.

# The future



- Goal is to ultimately accumulate  $50 \text{ ab}^{-1}$
- However: a huge amount of physics will be done with  $\sim 5\text{-}10 \text{ ab}^{-1}$ , possibly uncovering new physics (the amount of physics done with  $< 0.5 \text{ ab}^{-1}$  is surprising)